Insights into molecular states and novel constraints for strange meson-baryon interactions with correlations at LHC

V. Mantovani Sarti (TUM) HHIQCD2024 – 21-25 October YITP, Kyoto





Thanks Akira.



From Kyoto...to Kyoto. In memory of Akira.

International Molecule-type Workshop "Hadron Interactions and Polarization from Lattice, Quark Model and High-Energy Collisions" YITP Kyoto 2019

Multi-strange meson-baryon systems and exotic states

- Interactions between mesons and baryons involving strangeness
 - Possibility to study nature and properties of exotic states
- Presence of a rich coupled-channel dynamics
 - Systems sharing same quantum numbers (B,S,Q), relatively close in mass
 - On- and off-shell processes from one channel to the other
- Several candidates for exotic states with molecular nature
 - Typically observed close to channel thresholds
 - Main example given by the two-pole Λ(1405) state
 J. M.M. Hall et al. PRL 114 (2015) 13
 U. G. Meißner Symmetry 12 (2020) 6, 981

Today we will focus on strange molecular states!



1.45

M. Mai EPJST 230 (2021) 6

1.35

Re _{WCMs} [GeV]



TIM Strange molecular states and where to find them

Y. Kamiya Mo. 21 Oct

Interactions with rich coupled-channel dynamics → Typically observed close to channel thresholds





IIII Strange molecular states and where to find them

Y. Kamiya Mo. 21 Oct

Interactions with rich coupled-channel dynamics → Typically observed close to channel thresholds



Need for high-precision data close to $\overline{K}N$ threshold!!



IIII Strange molecular states and where to find them

Y. Kamiya Mo. 21 Oct

Interactions with rich coupled-channel dynamics \rightarrow Typically observed close to channel thresholds



Need for experimental constraints on as many channels as possible!



More strange molecular states and where to find them

- Scattering experiments challenging with increasing strangeness
 - $\Xi(1620)$ lying across the $\overline{K}\Lambda$ threshold as molecular candidate, poorly known
- Intensive searches via spectroscopy measurements with different production mechanism





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Accessing the interaction between the constituents



Investigating exotic states with correlations

• Accessing interaction between the constituents with correlation functions measured in pp collisions *M.Lisa, S. Pratt et al, ARNPS. 55 (2005), 357-402, L. Fabbietti, VMS and O. Vazquez Doce ARNPS 71 (2021), 377-402*

$$C(k^*) = \mathcal{N}(k^*) \frac{N_{\text{same}}(k^*)}{N_{\text{mixed}}(k^*)} = \int S(\vec{r}^*) \left| \psi(\vec{k}^*, \vec{r}^*) \right|^2 d^3 \vec{r}^*$$





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Finite set of the set of th

What ranges of inter-particle distances are we probing at LHC?



Small and large colliding systems at LHC: from pp to Pb-Pb

By changing the colliding system

- Probe source sizes ranging from 1 fm up to 10 fm
- Interparticle distances from 2 to roughly 20 fm



How does the signal in the correlation function changes with the source size?



Small and large colliding systems at LHC: from pp to Pb-Pb



ALICE Coll. PLB 811 (2020) 135849



$$C(k^*) = \int S(\vec{r}^*) |\psi(\vec{k}^*, \vec{r}^*)|^2 d^3 \vec{r}^*$$

Fixing the source \rightarrow Very well known interaction from a pair we can easily produce at LHC!







$$C(k^*) = \int S(\vec{r}^*) |\psi(\vec{k}^*, \vec{r}^*)|^2 d^3 \vec{r}^*$$

Fixing the source \rightarrow Very well known interaction from a pair we can easily produce at LHC!



- 2. Modeling the source U. A. Wiedemann, U. W. Heinz, Phys.Rept. 319, 145-230 (1999)
 - Primary particles from common Gaussian core source
 - Observed scaling with the transverse pair mass $m_{\rm T}$





$$C(k^*) = \int S(\vec{r}^*) |\psi(\vec{k}^*, \vec{r}^*)|^2 d^3 \vec{r}^*$$

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- 2. Modeling the sourceU. A. Wiedemann, U. W. Heinz, Phys.Rept. 319, 145-230 (1999)
 - Primary particles from common Gaussian core source
 - Observed scaling with the transverse pair mass $m_{\rm T}$
 - Depending only on the mass of the pair
 - Strongly decaying resonances with $c\tau \sim 1-2$ fm ($\Delta \rightarrow p\pi$)
 - Tail at large r^* , effect. enlarging the source
 - Depending on the particles in the pair

Let's test our source hypothesis on the data!



Similar results obtained in Mihaylov, Gonzalez EPJC 83 (2023)

Interesting studies using a dynamical source on pq CF: Kuroki, Hirano arXiv:2410.01204

to the dataset properties (e.g. multiplicity)





Observation of a common emitting source for hadrons in pp collisions

Similar approach tested on p-p correlations in Pb-Pb by ALICE will become available soon!!



Coupled-channels dynamics in femtoscopy



Coupled-channels dynamics in femtoscopy



Coupled-channels dynamics in femtoscopy



High-precision data on S=-1 sector above threshold



$\square \square Accessing the \Xi^{-}K^{+} system with femtoscopy$

- Most precise data at low momenta on the interaction between Ξ and kaons
 - Input also for heavy Λ^* and Σ^* resonances
- Modeled assuming Lednicky-Lyuboshits wavefunction with Coulomb (S-wave only) R. Lednicky, Phys.Part.Nucl.40:307-352,2009
 - Coulomb + strong repulsive interaction well in agreement with the data
- Determination of scattering length from best fit

 $\Re f_0 = -0.61_{\pm 0.02(stat)}^{\pm 0.02(stat)}$ $\Im f_0 = 0.41_{\pm 0.04(stat)}^{\pm 0.04(stat)}$





ALI-PREL-574336

Accessing the S=-2 meson-baryon interaction

- Extending previous Pb–Pb femtoscopic measurements to pp collisions ALICE Coll. PRC 103 (2021)
- Several structures present in the measured correlation





 $C(k^*)$

\square Accessing the S=-2 meson-baryon interaction



First experimental evidence of $\Xi(1620)$ decay into ΛK^-



\mathbb{T} K⁻A correlations and the S=-2 meson-baryon sector



Can we use these femtoscopic data to constrain effective QCD models and investigate the $\Xi(1620)$ nature?



1.2

1.1

99<mark>9999999999999</mark>99

150

200

ALICE Coll. PLB 845 (2023) 138145

250

300

350

400

*k** (MeV/*c*)

100

50

TIM Femtoscopy era in the S=-2 meson-baryon sector

 First combined effort in constraining the low-energy constants (and subtraction constants) of an effective chiral lagrangian to correlation data

$$C(k^{*}) = \int S_{1}(\vec{r}^{*}) \left| \psi_{1 \to 1}(\vec{k}^{*}, \vec{r}^{*}) \right|^{2} d^{3}r^{*} + \sum_{j \neq 1} \omega_{j}^{prod} \int S_{j}(\vec{r}^{*}) \left| \psi_{j \to 1}(\vec{k}_{j}^{*}, \vec{r}^{*}) \right|^{2} d^{3}r^{*}$$

- Wavefunctions obtained in a coupled-channel approach
 - State-of-the-art NLO effective lagrangian in UxPT A. Feijoo et al., PLB 841 (2023)

```
 \mathcal{L}_{\phi B}^{(1)} = i \langle \bar{B} \gamma_{\mu} [D^{\mu}, B] \rangle - M_0 \langle \bar{B} B \rangle - \frac{1}{2} D \langle \bar{B} \gamma_{\mu} \gamma_5 \{ u^{\mu}, B \} \rangle 
 - \frac{1}{2} F \langle \bar{B} \gamma_{\mu} \gamma_5 [u^{\mu}, B] \rangle ,
```

 $\mathcal{L}_{\phi B}^{(2)} = b_D \langle \bar{B} \{ \chi_+, B \} \rangle + b_F \langle \bar{B} [\chi_+, B] \rangle + b_0 \langle \bar{B} B \rangle \langle \chi_+ \rangle$ $+ d_1 \langle \bar{B} \{ u_\mu, [u^\mu, B] \} \rangle + d_2 \langle \bar{B} [u_\mu, [u^\mu, B]] \rangle$ $+ d_3 \langle \bar{B} u_\mu \rangle \langle u^\mu B \rangle + d_4 \langle \bar{B} B \rangle \langle u^\mu u_\mu \rangle .$

- Data-driven estimate of ω_j^{prod} and emitting source ALICE Coll. Eur.Phys.J.C 83 (2023), VMS, A. Feijoo et al. arXiv: 2309.08756
- $\Xi(1620)$ and $\Xi(1690)$ properties overall in line with PDG and previous measurements
 - $\Gamma_{\Xi(1620)}$ = 24.7 MeV, tension with Belle's results



Work in collaboration with: Dr. A. Feijoo, Dr. I. Vidana, Prof. A. Ramos, Prof. F. Giacosa, Prof. T. Hyodo and Dr. Y. Kamiya

TIM Femtoscopy era in the S=-2 meson-baryon sector





TIP Femtoscopy era in the S=-2 meson-baryon sector





TIP The $\Xi^-\pi^+$ correlation in pp collisions

- Most precise data for $\Xi^-\pi^+$ down to threshold
- Observation of ±(1620) and ±(1690), in agreement with Belle spectroscopy data
 - Mass and widths in line with previous spectroscopic measurements
- Evidence of shallow strong attraction

 $\Re f_0 = 0.089^{\pm 0.007(stat)}_{\pm 0.009(syst)}$ $\Im f_0 = 0.007^{\pm 0.003(stat)}_{\pm 0.005(syst)}$

Novel high-precision data available to constrain this multi-strange meson-baryon sector!





Towards a new femtoscopy-spectroscopy alliance!

• Moving towards studies on the corresponding available spectroscopy data



Conclusions and outlooks

- Most precise data on ΞK and $\Xi \pi$ at low momenta available
 - Novel high-precision constraints on S=-1 and S=-2 baryon interactions available with correlation data
 - Input for low-energy effective chiral lagrangians
- Femtoscopy as a complementary tool to provide important input for searches and studies of exotic states



Many experimental and theoretical activities...

ALICE Collaboration:

PRC 99 (2019) 2, 024001 PLB 797 (2019) 134822 PRL 123 (2019) 112002 PRL 124 (2020) 09230 PLB 805 (2020) 135419 PLB 811 (2020) 135849 Nature 588 (2020) 232-238 PRL 127 (2021), 172301 PLB 822 (2021), 136708 PRC 103 (2021) 5, 055201 PLB 833 (2022), 137272 PLB 829 (2022), 137060 PRD 106 (2022), 5, 05201 PL B 844 (2023) 137223 EPJA 59 (2023) 145 EPJC 83 (2023) 4, 340 PLB 845 (2023) 138145 EPJA (2023) 59:298 arXiv: 2311.14527 [hep-ph] arXiv: 2401.13541 [nucl-ex] arXiv:2308.16120 [nucl-ex]

STAR Collaboration:

Nature 527 (2015) 345-348 PRL 114 (2015), 022301 PLB 790 (2019) 490-497

HADES Collaboration:

PRC 82 (2010) 021901 PRC 94 (2016) 2, 025201

Latest theoretical studies on exotics and correlations:

Liu et al. Phys.Rev.D 107 (2023) 7, 074019 Albaladejo et al. Phys.Rev.D 108 (2023) 1, 014020 Kemchandani et al. arXiv:2312.11811 Ikeno et al. Phys.Lett.B 847 (2023) 138281 Torres-Rincon et al. Phys.Rev.D 108 (2023) 9, 096008 Kamiya et al. Eur.Phys.J.A 58 (2022) 7, 131 Vidaña, Feijoo et al. Phys.Lett.B 846 (2023) 138201 Albaladejo, Feijoo et al. arXiv:2307.09873 Liu et al. Phys.Rev.D 108 (2023) 3, L031503 Feijoo et al. Phys.Rev.D 109 (2024) 1, 016014 Liu et al. Phys.Rev.D 109 (2024) 1, 016014 M. Z. Liu et al. arXiv: 2404.06399 [hep-ph] Li et al. arXiv: 2311.14365 [hep-ph] Molina et al. Phys.Rev.D 109 (2024) 5, 054002 Krein Few Body Syst. 64 (2023) 3, 42



Three-body dynamics: pd, ppp, ppΛ, ppK[±]

pd: ALICE Coll. PRX 14 (2024) 3, 031051 ppp,ppA: ALICE Coll. EPJA 59, 145 (2023) ppK: ALICE Coll. EPJA 59,12 (2023)

Theoretical papers:

M. Viviani et al, Phys.Rev.C 108 (2023) 6, 064002 A. Kievsky, et al., Phys.Rev.C 109 (2024) 3, 034006

E. Garrido et al., arXiv: 2408.01750 (2024)





Additional slides



III Basics of femtoscopy – Experimental definition



TIT Basics of femtoscopy – Experimental definition



The emitting source in pp collisions



The source function - Effect of short-lived resonances



- For Ξ^{-} and Ω^{-} no contributions!
- Average mass and average ct determined by the weighted average values of all resonances

Particle	M _{res} [MeV]	$ au_{ m res}$ [fm]
p	1361.52	1.65
Λ	1462.93	4.69
Σ^0	1581.73	4.28



Genuine and not genuine...that is (not) the problem!

ALICE Coll. PRC 99 (2019) no.2, 024001



Unfortunately in our p-p pairs sample we do not have only **primary produced protons** undergoing the **genuine interaction** we aim at measuring



- These residual correlations dilute the signal, need to be constrained as much as possible (modeling interaction when possible, e.g. pΛ)
- 2. Each contribution is weighted taking into account **purity** and origin of the particles in the pair

 $\lambda_i = P_{i,1} f_{i,1} \cdot P_{i,2} f_{i,2}$

3. Both the purities and the fractions of particles coming from primary, secondaries, etc. can be determined using using Monte Carlo simulated data

Moving to K⁻Λ correlations...

Correlations measured in Pb-Pb collisions

 → No particular cusps or structure visible
 → First measurements of ΛK̄ scattering parameters!

 How does the correlation look like in pp collisions?

Can we shed light on the nature of $\Xi(1620)$ and $\Xi(1690)$ states with correlations?





TIM Fixing the source in AK correlations

- Core-halo resonance model anchored to p-p CF
 - $r_{core} = 1.11 \pm 0.04 \ (< m_T >_{\Lambda K} = 1.35 \ GeV/c^2)$
- Long-lived strongly decaying resonances feeding to Λ
 - fit with effective double gaussian

 $S_{tot} (r) = \lambda_s [\omega_S \cdot S(r_1) + (1 - \omega_S) \cdot S(r_2)]$

Parameter	Value
$r_{\rm core} [{\rm fm}]$	$1.11\substack{+0.04\\-0.04}$
$r_{1,\text{eff}} \text{ [fm]}$	$1.202^{+0.043}_{-0.042}$
$r_{2,\mathrm{eff}} \; \mathrm{[fm]}$	$2.330\substack{+0.050\\-0.045}$
ω	$0.7993^{+0.0037}_{-0.0027}$
λ	$0.9806\substack{+0.0006\\-0.0008}$







Modeling the correlation function



- Residual background due to initial parton scattering ٠
 - → Typically observed in meson-baryon correlations ALICE Coll. Phys. Rev. Lett. 124 (2020)
 - \rightarrow Modeled using Monte-carlo simulations
- Addition of Ω , Ξ^* resonances observed in the CF modeled with BW ٠ \rightarrow Values of (M, Γ) to be extracted with fit to the data



*k** (MeV/*c*)

ΛK^{-} correlation: including the $\Xi(1620)$ resonance



$$C_{model}(k^*) = \lambda_{gen} C_{gen}(k^*) + \lambda_{\Xi K} C_{\Xi K}(k^*) + \lambda_{flat}$$

Modeled with Lednicky-Lyuboshits analytical formula

$$C_{gen}(k^st) = w C_{non-res}(k^st) + (1-w) C_{res}(k^st)$$

- $C_{non-res} \rightarrow LL$ with ERE scatt. amplitude
- $C_{res} \rightarrow LL$ with Flattè-like scatt. amplitude (<u>F. Giacosa et al. Eur.Phys.J.A 57 (2021) 12, 336</u>)

$$f(k^*) = \frac{-2\tilde{\Gamma}_2}{E^2 - M^2 + i\tilde{\Gamma}_1\sqrt{E^2 - E_{thr.1}^2} + i\tilde{\Gamma}_2\sqrt{E^2 - E_{thr.2}^2}} \qquad \begin{array}{c} \text{ch. 1 = } \pi\Xi \\ \text{ch. 2 = } \Lambda K^2 \end{array}$$



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Thanks to Prof. F. Giacosa for the discussion

Modeling the correlation function



Genuine correlation of interest \rightarrow Modeled with the Lednicky-Lyuboshits formula^[2]



Contributions from secondaries, impurities, etc.. • \rightarrow Modeled when possible^[4] or assumed flat



100

C(k*)

1.6

1.5

1.4H

1.2

1.1

0

50



ALICE Coll. PLB 845 (2023) 138145

ALICE pp $\sqrt{s} = 13 \text{ TeV}$

 \circ $\Lambda - \mathsf{K}^{-} \oplus \overline{\Lambda} - \mathsf{K}^{+}$

Background

Non resonant

and the second s

150

200

250

300

350

400

*k** (MeV/*c*)

--- Resonant

High Mult. (0-0.17% INEL > 0)

TIM Scattering parameters for ΛK^-

Indication of an attractive non-resonant interaction

 \rightarrow In agreement with ALICE Pb-Pb results^[1]

• Available models far from converging on similar results

 \rightarrow Parameters fixed based on SU(3) flavour symmetry, isospin symmetry

- \rightarrow Mainly anchored to πN or $\overline{K}N$ data
- \rightarrow $\Xi(1620)$ typically lying below threshold



UxPT at LO: Ramos et al. PRL 89 (2002), Nishibuchi et al. EPJ Web Conf 271 (2022) xPT at NLO: Liu et al. PRD 75 (2007), Mai et al. PRD 80 (2009)



Overview on S=-2 meson-baryon sector

- Poorly constrained experimentally
 → Effective lagrangians anchored to S=-1 sector^[1]
- Ξ(1620) and Ξ(1690)^[2] dynamically generated states within coupled-channel models

 → Ξ(1620) observed by Belle in πΞ decay but currently only 1 star in PDG, J^P = ??, B.R. not quantit. known.

$$M = 1610.4 \pm 6.0^{+6.1}_{-4.2} \text{ MeV},$$

 $\Gamma = 59.9 \pm 4.8^{+2.8}_{-7.1} \text{ MeV}.$



[2] LHCb [3] A. Feijo

[1] A. Ramos er al. PRL 89 (2002)
 [2] LHCb coll. Sci.Bull. 66 (2021)
 [3] A. Feijoo et al. PLB 841 (2023)

LO xPT calculations: C. Garcia-Recio et al. PLB 582 (2004) D. Gamermann et al. PRD 84 (2011) T. Sekihara PTEP 2015 (9) (2015) T. Nishibuchi and T. Hyodo, EPJ Web Conf 271 (2022) valentina.mantovani-sarti@tum.de

TIP Overview on S=-2 meson-baryon sector

Belle Coll. PRL 122 (2019)

- Poorly constrained experimentally \rightarrow Effective lagrangians anchored to S=-1 sector^[1]
- Ξ(1620) and Ξ(1690)^[2] dynamically generated states within coupled-channel models

 → Ξ(1690) observed by LHCb in ΛK decay, currently 3 star in PDG, J^P = ?[?], B.R. not quantit. known.

$$M = 1692.0 \pm 1.3^{+1.2}_{-0.4} \text{ MeV},$$

$$\Gamma = 25.9 \pm 9.5^{+14.0}_{-13.5} \text{ MeV}.$$



• Recent development of chiral calculations at NLO^[3]



A. Ramos er al. PRL 89 (2002)
 LHCb coll. Sci.Bull. 66 (2021)
 A. Feijoo et al. PLB 841 (2023)

LO _XPT calculations: C. Garcia-Recio et al. PLB 582 (2004) D. Gamermann et al. PRD 84 (2011) T. Sekihara PTEP 2015 (9) (2015) T. Nishibuchi and T. Hyodo, EPJ Web Conf 271 (2022) valentina.mantovani-sarti@tum.de

Constraining effective QCD lagrangians with correlations





Constraining the S=-2 meson-baryon sector

- State-of-the-art U_XPT at NLO available^[1]
 - Low energy constants (LECs) fixed to S=-1 sector^[2]
 - Two sets of subtraction constants (SCs) values
 - Widths of Ξ(1620) too large wrt to Belle's results^[3]

Use the high-precision femtoscopic data to fix LECs and SCs!

Work in collaboration with: Dr. A. Feijoo, Dr. I. Vidana, Prof. A. Ramos, Prof. F. Giacosa, Prof. T. Hyodo and Dr. Y. Kamiya [1] A. Feijoo et al., PLB 841 (2023)

Table 3: Comparison of the pole positions between the models: Model I and Model II (in MeV) with their couplings g_i and the corresponding modulus found in $J^P = \frac{1}{2}^-$, $(I, S) = (\frac{1}{2}, -2)$.

Model I	Ξ(1620)		Ξ(1690)	
M [MeV]	1599.95		1683.04	
Γ [MeV]	158.88		11.51	
	g_i	$ g_i $	g_i	$ g_i $
$\pi \Xi$	2.09 + i1.00	2.32	-0.30 - i0.12	0.33
$ar{K}\Lambda$	-2.11 - i0.09	2.11	-0.49 + i0.05	0.50
$ar{K}\Sigma$	-0.90 + i0.34	0.97	1.57 <i>– i</i> 0.24	1.59
$\eta \Xi$	-0.23 + i0.13	0.26	0.74 <i>– i</i> 0.11	0.74
Model II	Ξ(1620)		Ξ(1690)	
M [MeV]	1608.51		1686.17	
Γ [MeV]	170.00		29.72	
	g_i	$ g_i $	g_i	$ g_i $
$\pi \Xi$	2.11 + i1.07	2.37	-0.36 - i0.24	0.43
$ar{K}\Lambda$	-2.10 - i0.09	2.10	-0.81 + i0.02	0.81
$ar{K}\Sigma$	-0.86 + i0.38	0.94	2.26 + i0.03	2.26
_	0.10 10.10	0.00	1.04 .007	1 0 4

[2] A.Feijoo et al PRC 99 (2019)[3] Belle coll. PRL 122 (2019)



Extension to S=-2 and Q=-1 sector

- The interaction kernel for the S=-2, Q=-1 sector can be built from the S=-2, Q=0 employing isospin symmetry arguments: $V_{ij}(S = -2, Q = O) \rightarrow V_{ij}(I = 1/2), V_{ij}(I = 3/2) \rightarrow V_{ij}(S = -2, Q = -1)$
- Once again, the Bethe-Salpetter equation is solved in the same footing to get the T-matrix:

$$V_{ij} = V_{ij}^{WT} + V_{ij}^{D} + V_{ij}^{C} + V_{ij}^{NLO} \Longrightarrow T = (1 - VG)^{-1}V \Longrightarrow T_{ij}$$

 ΛK^- CF data available \longrightarrow unprecedented opportunity to fit a model for the first time in this sector

$$C(k) \simeq 1 + \int_0^\infty 4\pi r^2 dr S_{12}(r) \Big[\sum_\beta \omega_\beta |\Psi_{\alpha\beta}(r)|^2 - |j_0(kr)|^2 \Big]$$
$$\Psi_{\alpha\beta}(r) = \delta_{\alpha\beta} j_l(k_\alpha r) + \frac{1}{\pi} \int j_l(qr) dq q^2 \frac{1}{E - E_1^\beta(q) - E_2^\beta(q) + i\epsilon} T_{\alpha\beta;l}(q, k_\alpha; E)$$



TIT Fantastic LECs and SCs and where to find them



$$\mathcal{L}_{\phi B}^{(1)} = i \langle \bar{B} \gamma_{\mu} [D^{\mu}, B] \rangle - M_0 \langle \bar{B} B \rangle - \frac{1}{2} D \langle \bar{B} \gamma_{\mu} \gamma_5 \{ u^{\mu}, B \} \rangle$$

$$- \frac{1}{2} F \langle \bar{B} \gamma_{\mu} \gamma_5 [u^{\mu}, B] \rangle ,$$

$$\mathcal{L}_{\phi B}^{(2)} = b_D \langle \bar{B} \{ \chi_+, B \} \rangle + b_F \langle \bar{B} [\chi_+, B] \rangle + b_0 \langle \bar{B} B \rangle \langle \chi_+ \rangle + d_1 \langle \bar{B} \{ u_\mu, [u^\mu, B] \} \rangle + d_2 \langle \bar{B} [u_\mu, [u^\mu, B]] \rangle + d_3 \langle \bar{B} u_\mu \rangle \langle u^\mu B \rangle + d_4 \langle \bar{B} B \rangle \langle u^\mu u_\mu \rangle .$$



TIT Fantastic LECs and SCs and where to find them



$$\mathcal{L}_{\phi B}^{(1)} = i \langle \bar{B} \gamma_{\mu} [D^{\mu}, B] \rangle - M_0 \langle \bar{B} B \rangle - \frac{1}{2} D \langle \bar{B} \gamma_{\mu} \gamma_5 \{ u^{\mu}, B \} \rangle$$

$$- \frac{1}{2} F \langle \bar{B} \gamma_{\mu} \gamma_5 [u^{\mu}, B] \rangle ,$$

$$\mathcal{L}_{\phi B}^{(2)} = b_D \langle \bar{B} \{ \chi_+, B \} \rangle + b_F \langle \bar{B} [\chi_+, B] \rangle + b_0 \langle \bar{B} B \rangle \langle \chi_+ \rangle + d_1 \langle \bar{B} \{ u_\mu, [u^\mu, B] \} \rangle + d_2 \langle \bar{B} [u_\mu, [u^\mu, B]] \rangle + d_3 \langle \bar{B} u_\mu \rangle \langle u^\mu B \rangle + d_4 \langle \bar{B} B \rangle \langle u^\mu u_\mu \rangle .$$

Overall 12 input parameters to be fixed!





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TIM Femtoscopy era in the S=-2 meson-baryon sector

• First combined effort in constraining the input parameters of an effective chiral lagrangian to correlation data

TABLE I. Extracted fit parameters with LECs and subtraction constants of the VBC S = -2 meson-baryon interaction at NLO and normalization constant N_D . The bootstrap method [62–64] was employed to determine the errors of the parameters.

$egin{array}{l} a_{\Xi\pi}\ a_{\Lambdaar{ extsf{K}}}\ a_{\Sigmaar{ extsf{K}}}\ a_{\Xi\eta} \end{array}$	$\begin{array}{c} -2.96 \pm 0.11 \\ -1.87 \pm 0.10 \\ -1.32 \pm 0.02 \\ -2.42 \pm 0.03 \end{array}$
f/f_{π}	1.000 ± 0.001
$ b_0 \ [\text{GeV}^{-1}] \\ b_D \ [\text{GeV}^{-1}] \\ b_F \ [\text{GeV}^{-1}] \\ d_1 \ [\text{GeV}^{-1}] \\ d_2 \ [\text{GeV}^{-1}] \\ d_3 \ [\text{GeV}^{-1}] \\ d_4 \ [\text{GeV}^{-1}] $	$\begin{array}{c} -2.997 \pm 0.002 \\ 1.20 \pm 0.09 \\ -0.30 \pm 0.12 \\ -0.69 \pm 0.18 \\ -0.21 \pm 0.06 \\ 0.08 \pm 0.20 \\ -0.39 \pm 0.05 \end{array}$
N _D	1.0015 ± 0.0004



Work in collaboration with: Dr. A. Feijoo, Dr. I. Vidana, Prof. A. Ramos, Prof. F. Giacosa, Prof. T. Hyodo and Dr. Y. Kamiya



TIM Femtoscopy era in the S=-2 meson-baryon sector





TIT Subtraction constants

• Unitarized scattering amplitude from Chiral Lagrangian (WT+Born+NLO)

$$\begin{split} \overline{V_{ij} = V_{ij}^{WT} + V_{ij}^{D} + V_{ij}^{C} + V_{ij}^{NLO}} &\Longrightarrow T = (1 - VG)^{-1}V \Longrightarrow T_{ij} \\ \text{Only S-wave contribution is taken into account} \\ G_l &= \frac{2M_l}{(4\pi)^2} \left\{ a_l(\mu) + \ln \frac{M_l^2}{\mu^2} + \frac{m_l^2 - M_l^2 + s}{2s} \ln \frac{m_l^2}{M_l^2} + \frac{q_{\text{cm}}}{\sqrt{s}} \ln \left[\frac{(s + 2\sqrt{s}q_{\text{cm}})^2 - (M_l^2 - m_l^2)^2}{(s - 2\sqrt{s}q_{\text{cm}})^2 - (M_l^2 - m_l^2)^2} \right] \right\} \\ a_{\pi^0 \Xi^0} &= a_{\pi^+ \Xi^-} = a_{\pi\Xi} \\ a_{\bar{K}^0 \Lambda} = a_{\bar{K}\Lambda} \\ a_{\bar{K}^0 \Sigma^0} &= a_{K-\Sigma^+} = a_{\bar{K}\Sigma} \\ a_{\eta\Xi^0} &= a_{\eta\Xi} \end{split}$$
 Subtraction constants for the dimensional regularization scale $\mu = 630 \text{MeV}$ in all the "l" channels.



(Thanks to Dr. Feijoo)

Comparison BCN and VBC model





The ΛK^+ correlation in pp collisions

• Correlation below unity at low $k^* \rightarrow \text{Repulsive interaction}$

$$C(k^*) = N_D \cdot C_{model}(k^*) \cdot C_{bckg}(k^*)$$

- Residual background due to initial parton scattering
 - → Typically observed in meson-baryon and baryon-antibaryon correlations^[1,2]
 - \rightarrow Modeled using Monte-carlo simulations $^{[2]}$
- Genuine correlation modeled with the Lednicky-Lyuboshits formula^[2,3]
 → Assuming the scattering amplitude within the effective range expansion





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\square Constraining the scattering parameters of Ξ^-K^+ pairs

- Comparison of data with modeling assuming different values of $(\Re f_0, \Im f_0)$
 - Delivered in terms of number of standard deviations (n σ) in $k^* \in [0,250]$ MeV/c
- Allowed values for f₀ from state-of-the-art chiral calculations at next-to-leading order and phenomenological potentials constrained to available scattering data

Higher precision constraints can be delivered with correlation data





TIM From small to large colliding systems



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A clear signature for bound states



K--p femtoscopy in different colliding systems



TIT Extracted strong weights for $\Sigma\pi$ and \overline{K}^0 n channels

Unique constraint and direct access to $K^-p \leftrightarrow \overline{K}^0 n$ and $K^-p \leftrightarrow \Sigma \pi$ dynamics

- $\Sigma\pi$ consistent with unity
- deviation from unity for $\overline{\mathsf{K}}{}^{0}$ n
 - K⁻p K⁰ n coupling too weak in chiral potentials
 - update the scattering amplitude of KN-πΣ-πΛ system by including correlation measurements to available kaonic hydrogen and scattering data





TIT High-precision data on ΛN - ΣN interaction at LHC





TIM High-precision data on $\Lambda N-\Sigma N$ interaction at LHC

- New scenario arising for ΛN - ΣN interaction
 - NLO19 potentials favoured
 - Sensitivity to residual $p-\Sigma^0$ interaction
 - Crucial input from several measurements: $\rightarrow p\Sigma^{+,-}$ correlations in LHC Run 2/Run 3 $\rightarrow p\Sigma^{+,-}$ scattering data J-PARC E40
- Deviations with correlation data observed

First-ever combined analysis using available pA scattering and correlation data



ALICE Coll. PLB 833 (2022), 137272



$\hfill \Pi$ Quantifying the two-body contribution of U_Λ



D. Mihaylov, J. Haidenbauer and VMS PLB 850 (2024) 138550



\square pA scattering parameters from combined fit

Table 1

Summary table showing the compatibility of different scattering parameters to the femtocsopy data ($n\sigma_{fmt}$), scattering data ($n\sigma_{sct}$) as well as the combined analysis from the present work ($n\sigma_{tot}$). If the combined estimator $n\sigma_{tot}$ is considered, solutions ii, v and vii represent a set of "best" solutions.

Usmani parameterization	f_0 (fm)	<i>f</i> ₁ (fm)	$\mathrm{n}\sigma_{\mathrm{fmt}}$	$n\sigma_{\rm sct}$	$\mathrm{n}\sigma_{\mathrm{tot}}$
NLO13(600)	2.91	1.54	5.2	0.0	4.6
NLO19(600)	2.91	1.41	1.7	0.4	1.1
N ² LO(550)	2.79	1.58	5.4	0.0	4.8
i	2.10	1.44	0.2	2.1	1.0
ii	2.10	1.56	0.0	0.9	0.0
iii	2.10	1.66	1.8	0.2	1.0
iv	2.50	1.32	0.2	2.2	1.1
v	2.50	1.46	0.2	0.8	0.0
vi	2.50	1.55	1.8	0.2	1.0
vii	2.91	1.32	0.1	1.5	0.3
viii	3.34	1.18	1.2	0.9	1.0



Accessing the interaction between light and charm hadrons

ALICE Coll. PRD 106 (2022), 5, 052010



ALI-PUB-502166

Moving towards a charming future

- First measurements of interaction between D(*) mesons and light hadrons
 - Several predictions of exotic states, crucial input for charm nuclei and heavy-flavor observables in heavy-ions

Femtoscopy can be extended to the charm sector

- More results to come with the LHC Run 3 and Run 4 statistics





TIT Measuring the scattering length for $D\pi$ and $D^*\pi$ systems

- Extracted scattering lengths compatible with zero
 - \rightarrow No influence of the hadronic phase on heavy-flavour observables in heavy-ions
- Tension with available theoretical models
 - \rightarrow Novel possibility to constrain effective QCD models in the charm sector!



First experimental constraints available for D^(*) - light mesons dynamics

TIM Accessing the strong interaction with charm hadrons

- First measurement of the genuine correlation between protons and D⁻ mesons
 - \rightarrow Important input in studies and searches for charm nuclear states^{[1]}
- Comparison with available models
 - \rightarrow Indication of an **attractive interaction**
 - \rightarrow Compatible also with the formation of bound state

TABLE I. Scattering parameters of the different theoretical models for the ND interaction [22–25] and degree of consistency with the experimental data computed in the range $k^* < 200 \text{ MeV}/c$.

Model	$f_0(I = 0)$	$f_0(I = 1)$	n_{σ}
Coulomb			(1.1–1.5)
Haidenbauer <i>et al.</i> [22] $(g_{\sigma}^2/4\pi = 2.25)$	0.67	0.04	(0.8 - 1.3)
Hofmann and Lutz [23]	-0.16	-0.26	(1.3–1.6)
Yamaguchi et al. [25]	-4.38	-0.07	(0.6-1.1)
Fontoura et al. [24]	0.16	-0.25	(1.1–1.5)



ALI-PUB-502166

[1] A. Hosaka et al. Prog. Part. Nucl. Phys. 96 (2017), 6, 062C01