

Current Status of Astronomical Observations of Neutron Stars (especially magnetars!)

Teruaki Enoto (Kyoto University / RIKEN)

General overview of astronomical observations



 [@teru_enoto](https://twitter.com/@teru_enoto)

Compact Stars in the QCD Phase Diagram (CSQCD2024),
Kyoto University, 2024 October 7, 9:00-9:50 (40+10)
<https://indico.yukawa.kyoto-u.ac.jp/event/30/>

Neutron stars (NSs) are ideal laboratory of physics

- Neutron stars (NSs) are compact objects with 1.4 Solar mass and ~ 10 km radius \rightarrow Extreme physics
 - High density exceeding the atomic nucleus density
 - Strong gravitational field that bends light and causes spectral redshift
 - Strong photon field ranging from radio waves to gamma rays
 - Strong magnetic field close to the QED critical field



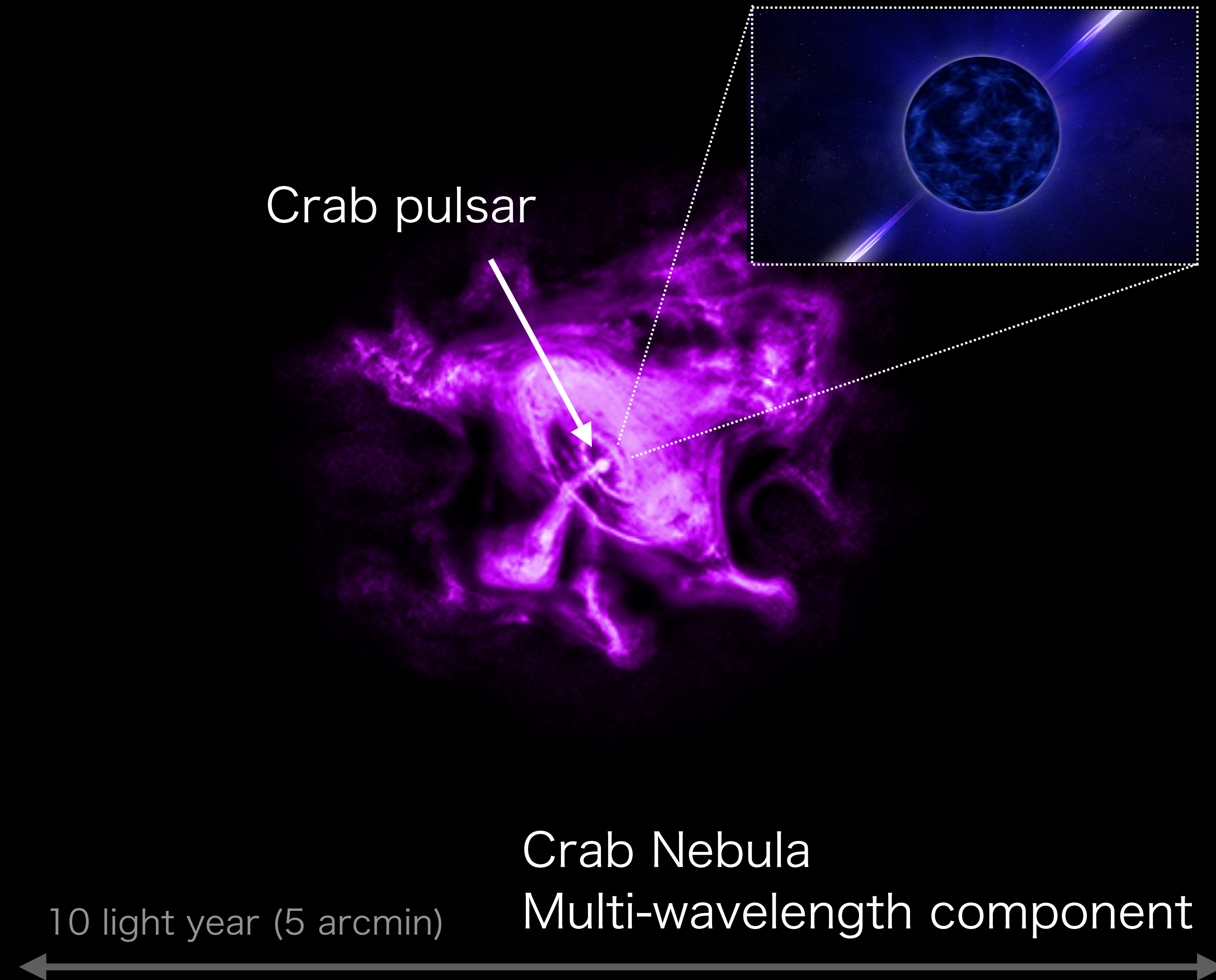
Crab Nebula
Multi-wavelength component

10 light year (5 arcmin)

Credit: NASA/CXC/SAO/STScI

Neutron stars (NSs) are ideal laboratory of physics

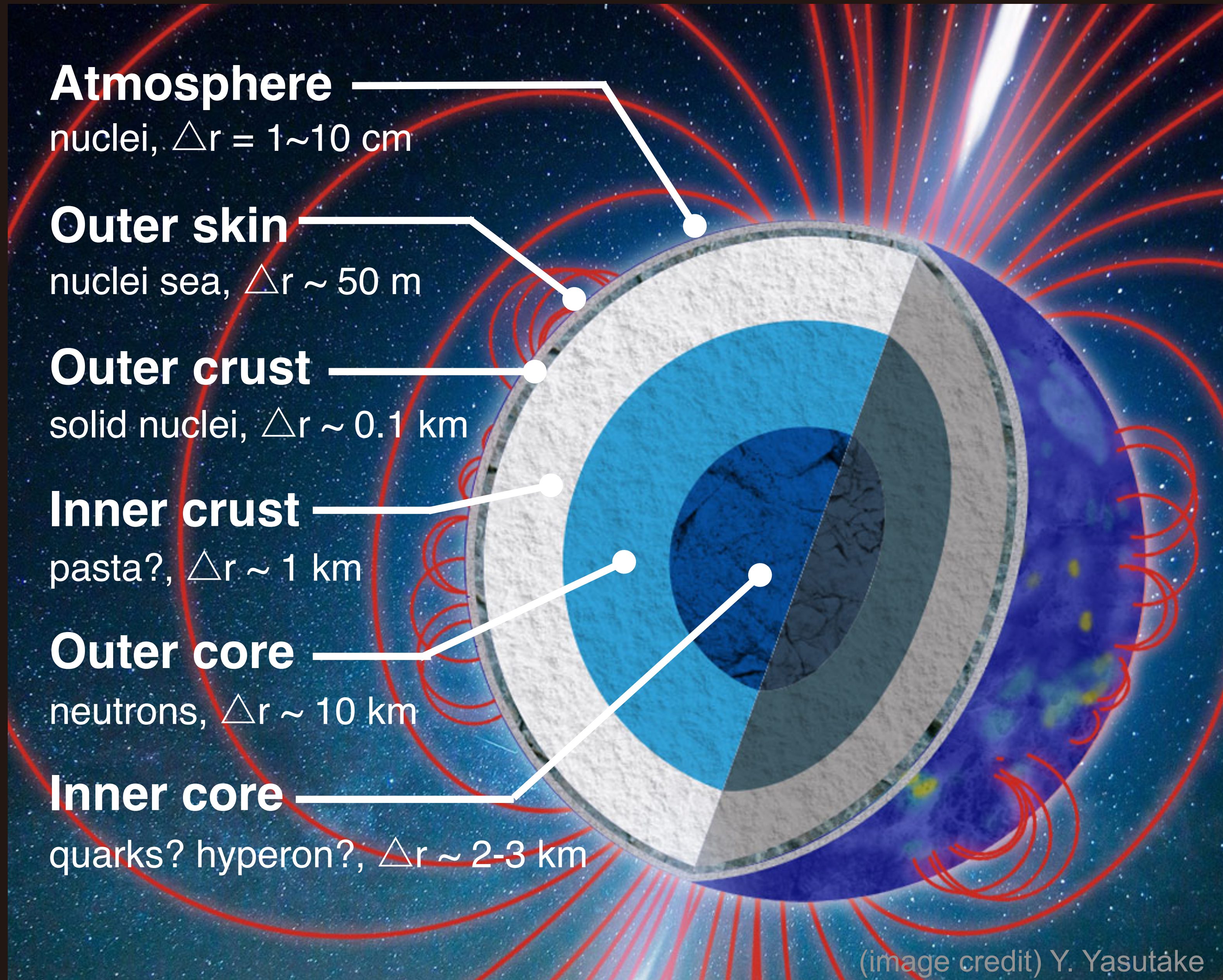
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Credit: NASA/CXC/SAO/STScI

Neutron stars (NSs) are ideal laboratory of physics

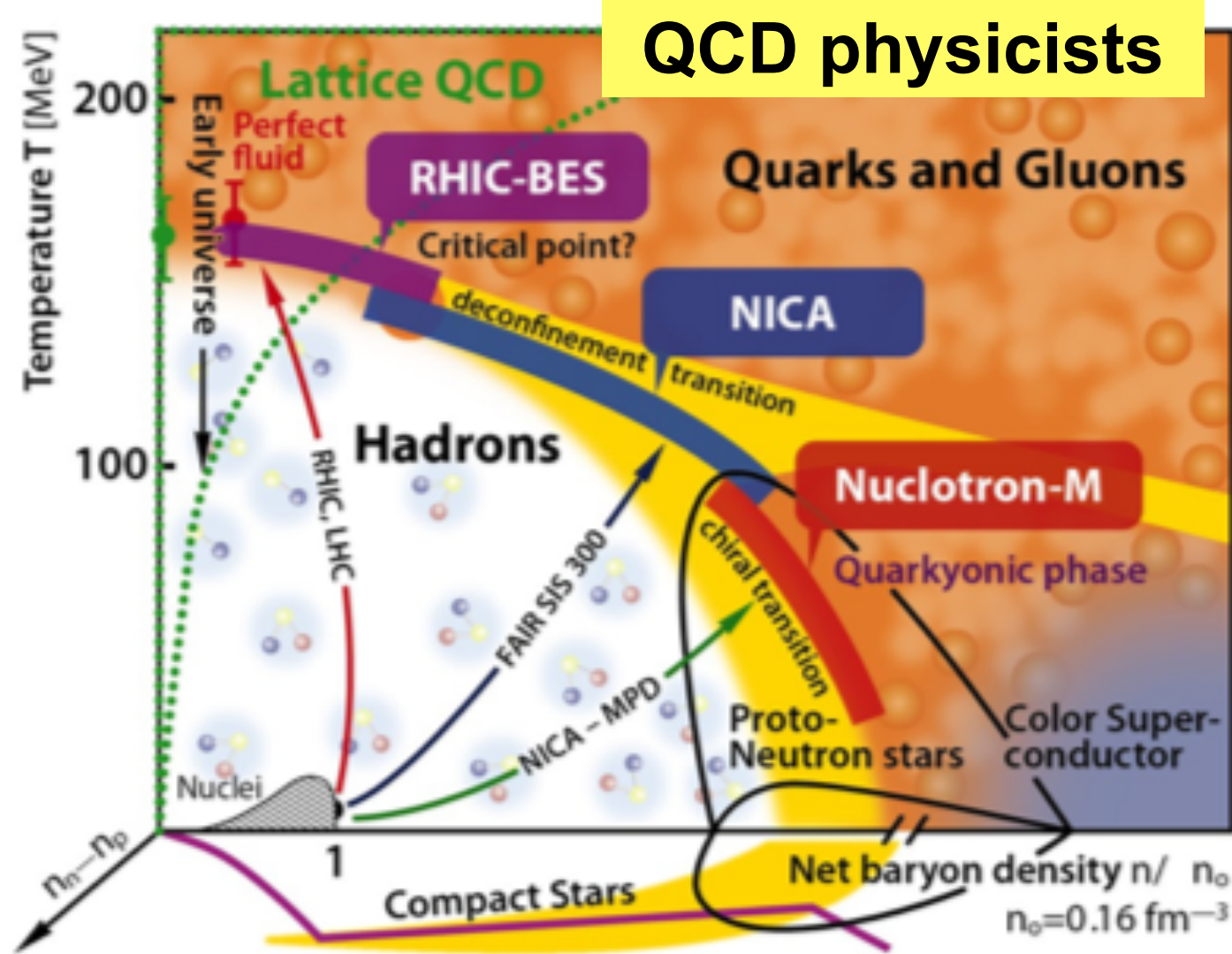
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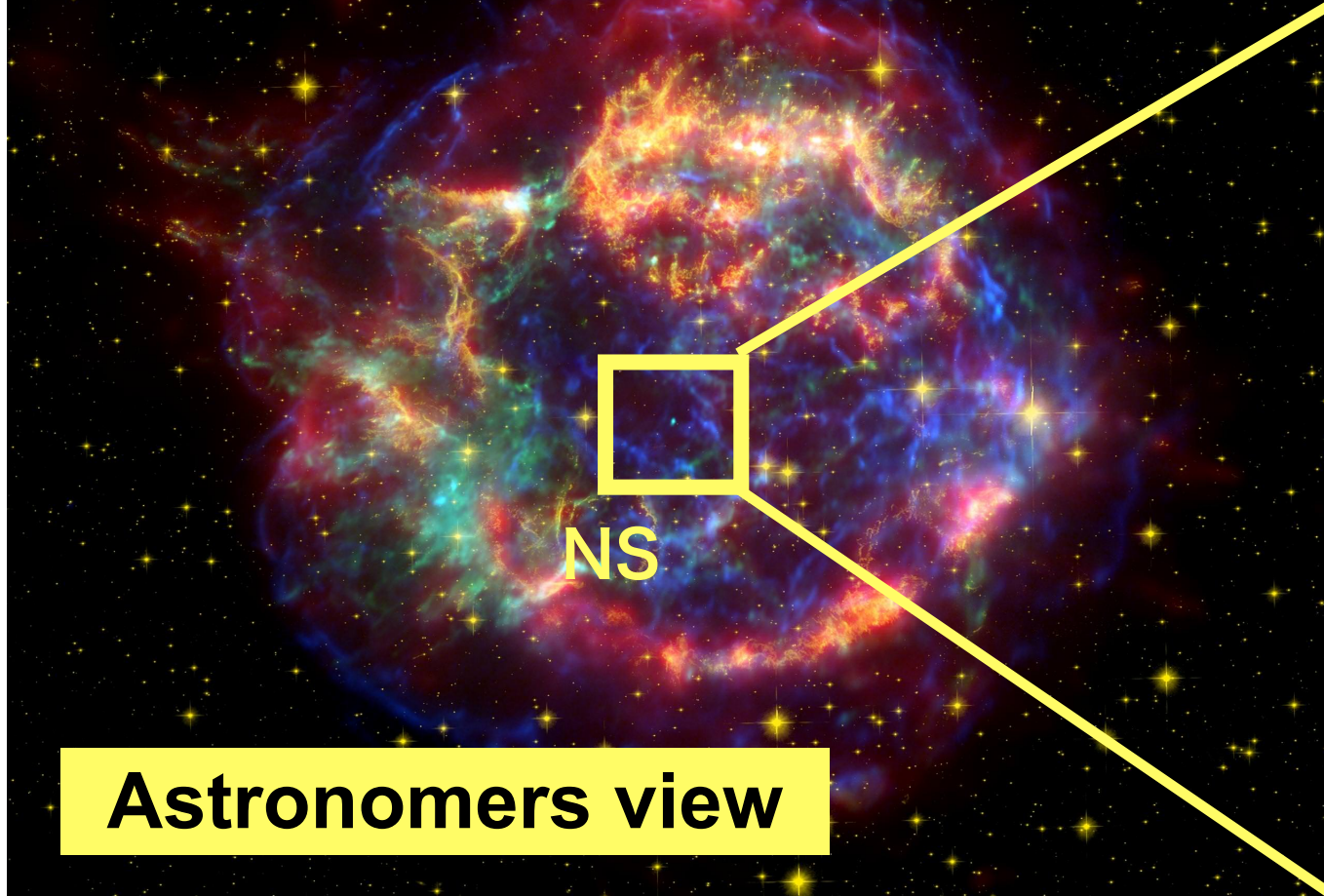
Observational quantities of neutron stars

- QCD physicists might want to know the mass, radius and interior of NSs...but

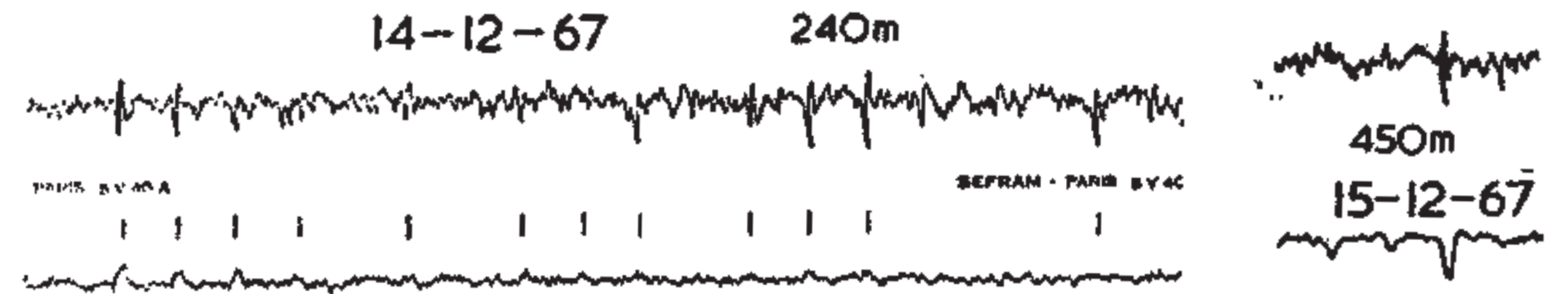
<https://www.interactions.org/blog/our-experiment>



NS in supernova remnant Cas A



Discovery of neutron stars in 1967 (57 years ago)



CP1919 (PSR J1921+2153) P=1.33 s

Hewish, Bell, et al., Nature (1968)



Radio observatory for this discovery

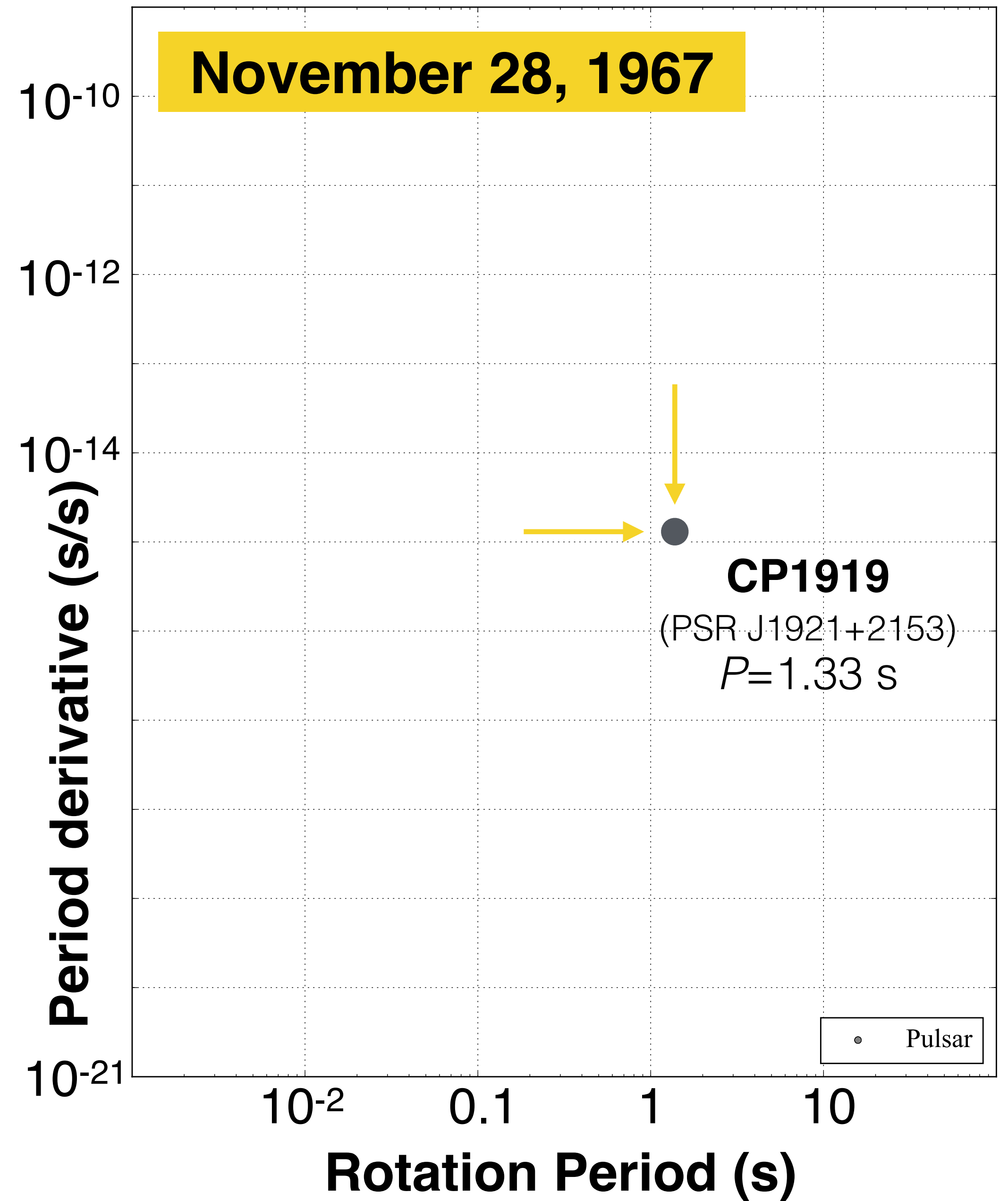
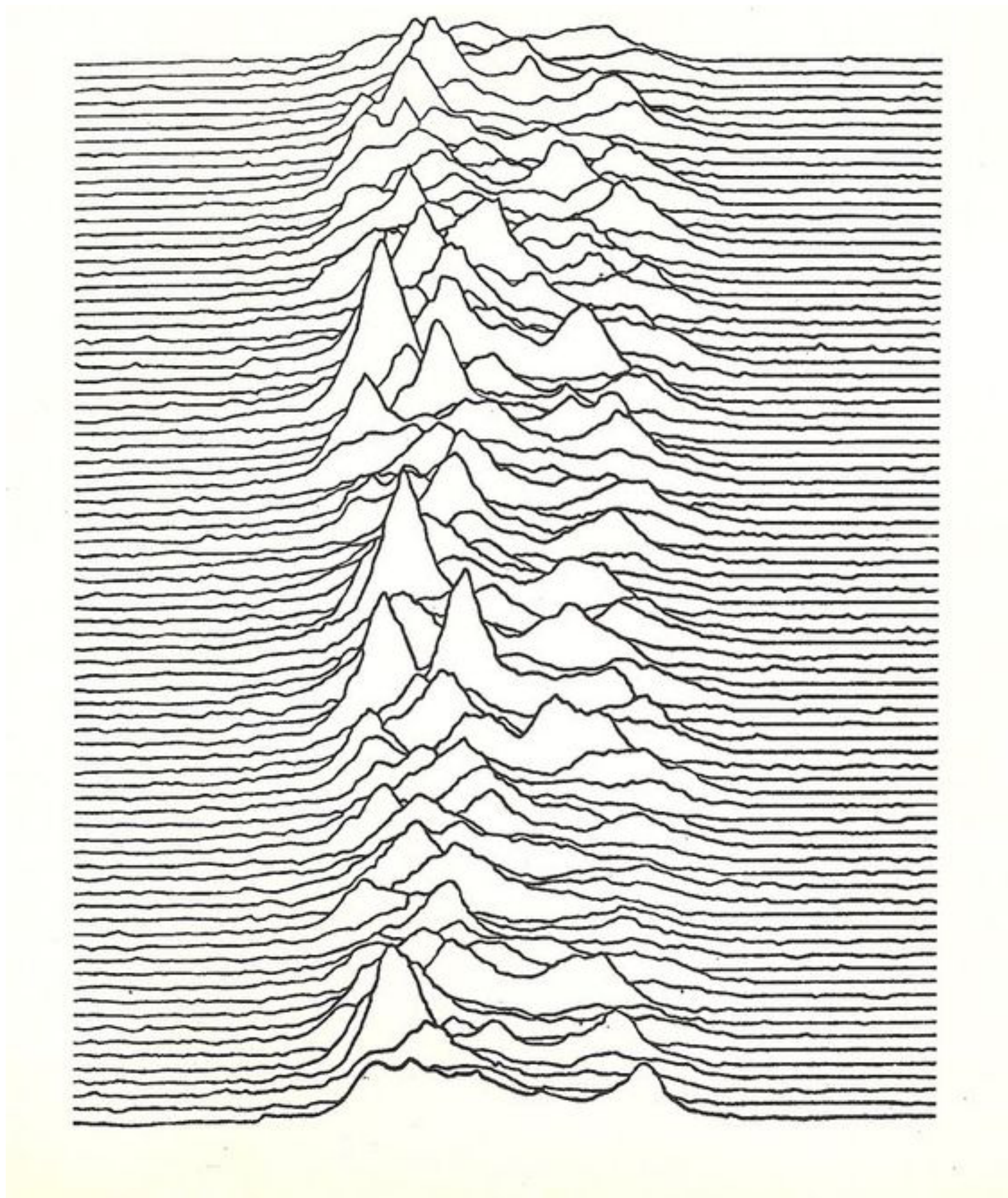
Four-acre array at the Mullard Radio Astronomy Observatory, Cambridge, UK, Credit: Graham Woan (J. B. Burnell, 2017, Nature astronomy)



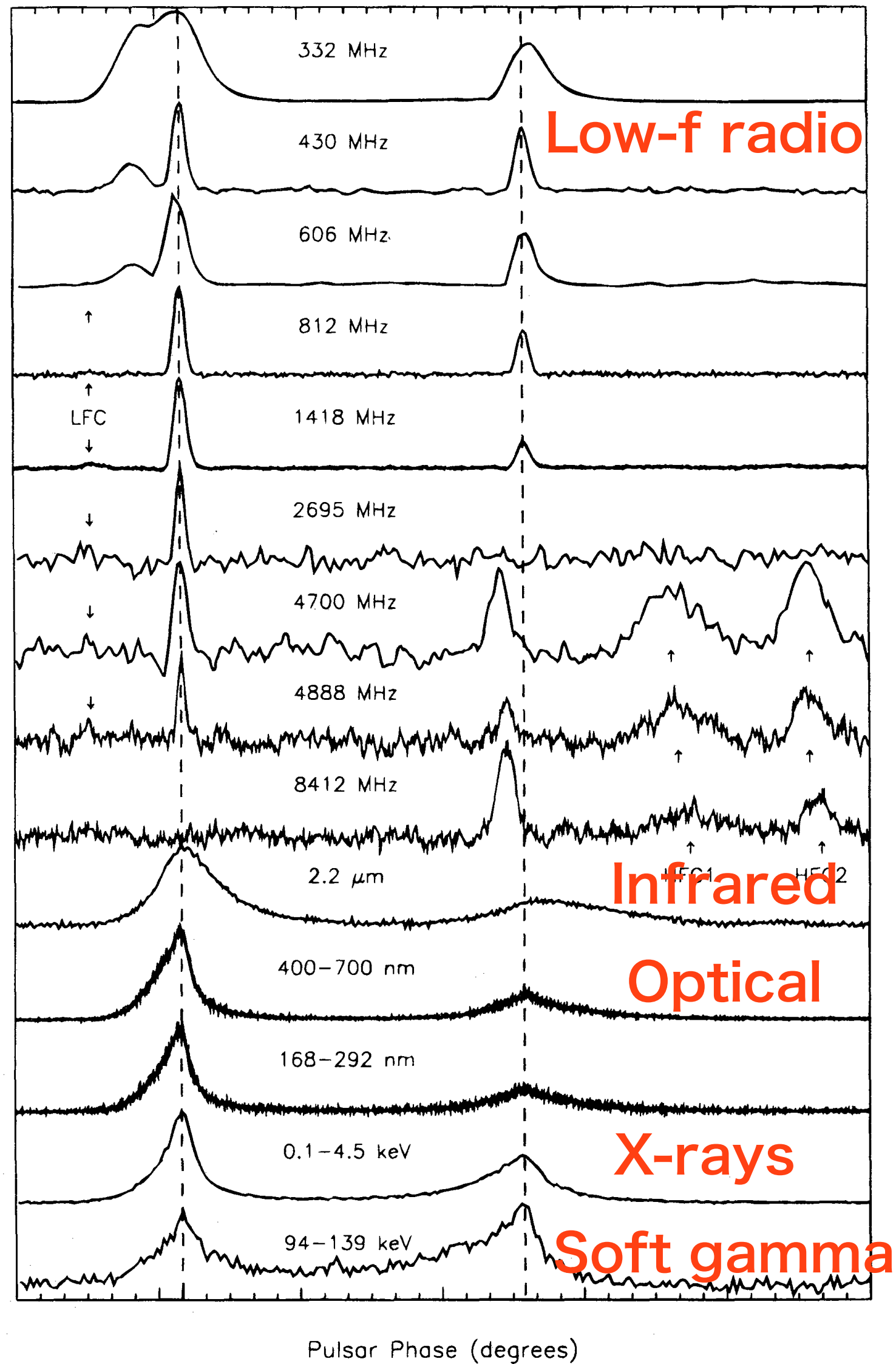
Enoto

J. B. Burnell

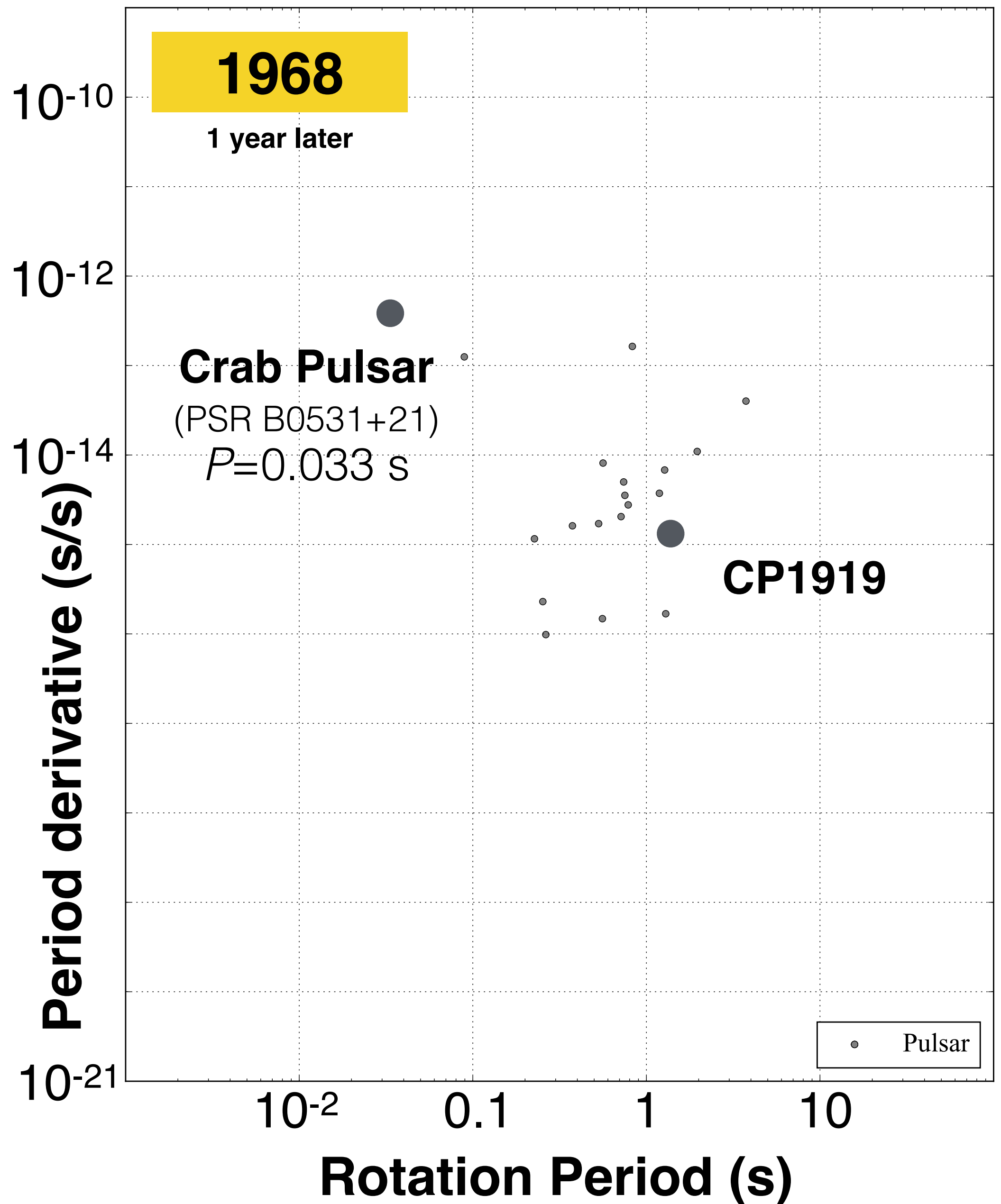
Diversity of Neutron Stars



Diversity of Neutron Stars

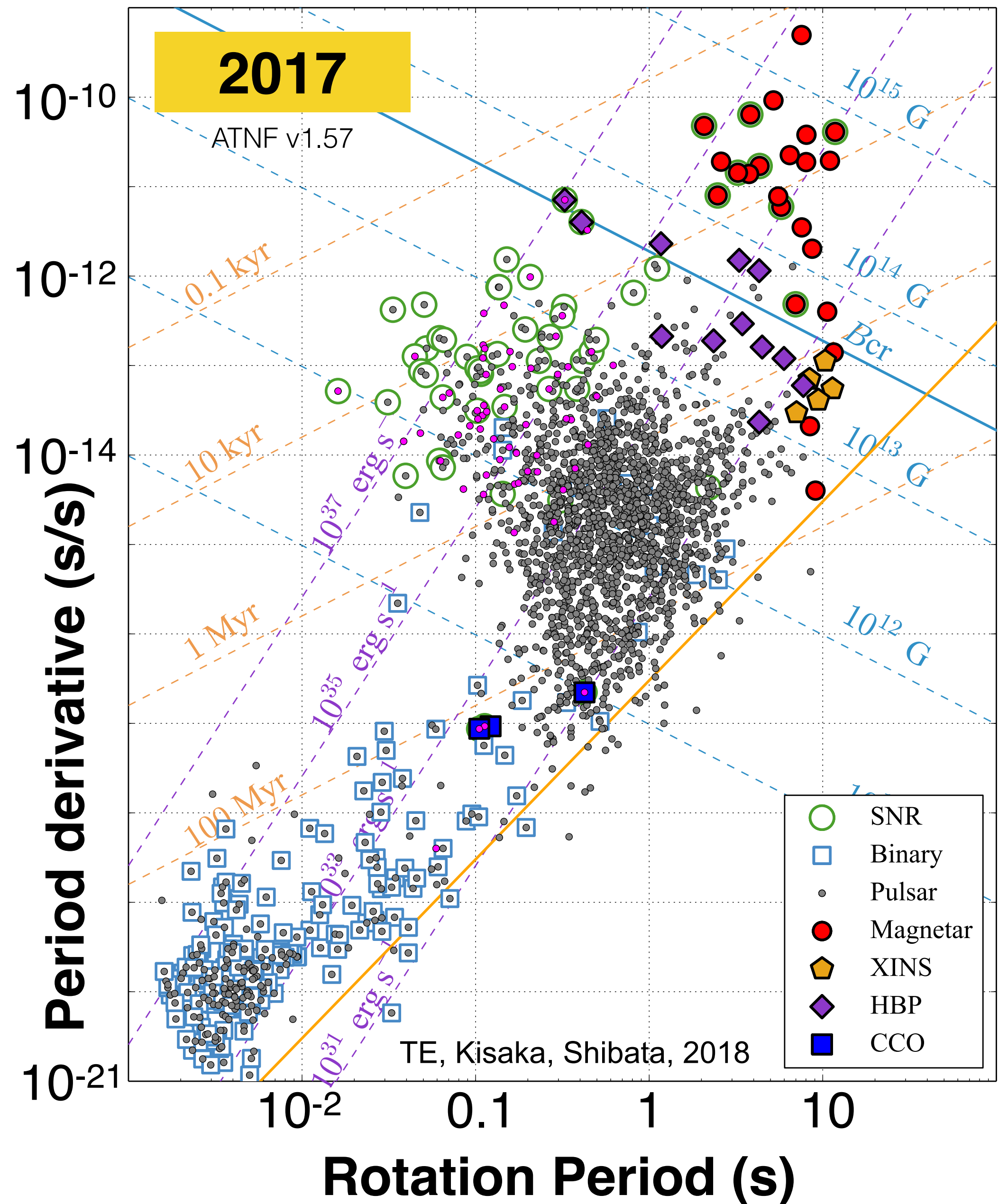


$P = 33 \text{ ms}$
 $\dot{P} = 4.2 \times 10^{-13} \text{ s/s}$



Diversity of Neutron Stars

- >3,000 known pulsars (10^5 in our Galaxy?)
- Multi-wavelength observations from radio, optical, X-rays, and gamma rays.

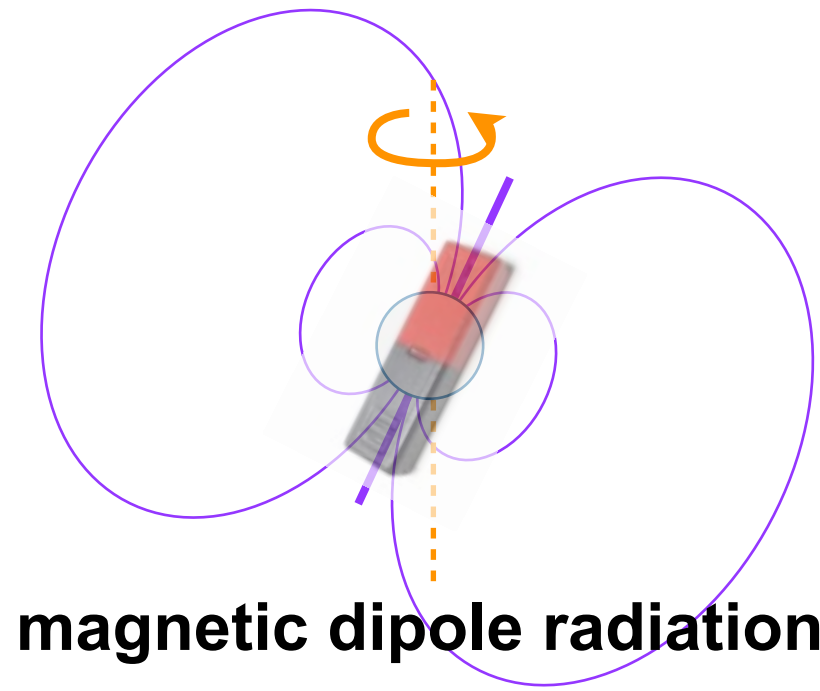


Diversity of Neutron Stars

- >3,000 known pulsars (10^5 in our Galaxy?)
- Multi-wavelength observations from radio, optical, X-rays, and gamma rays.
- Magnetic field strength

$$L_{\text{rot}} = \frac{dE_{\text{rot}}}{dt} = -\frac{d}{dt} \left(\frac{1}{2} I \Omega^2 \right)$$

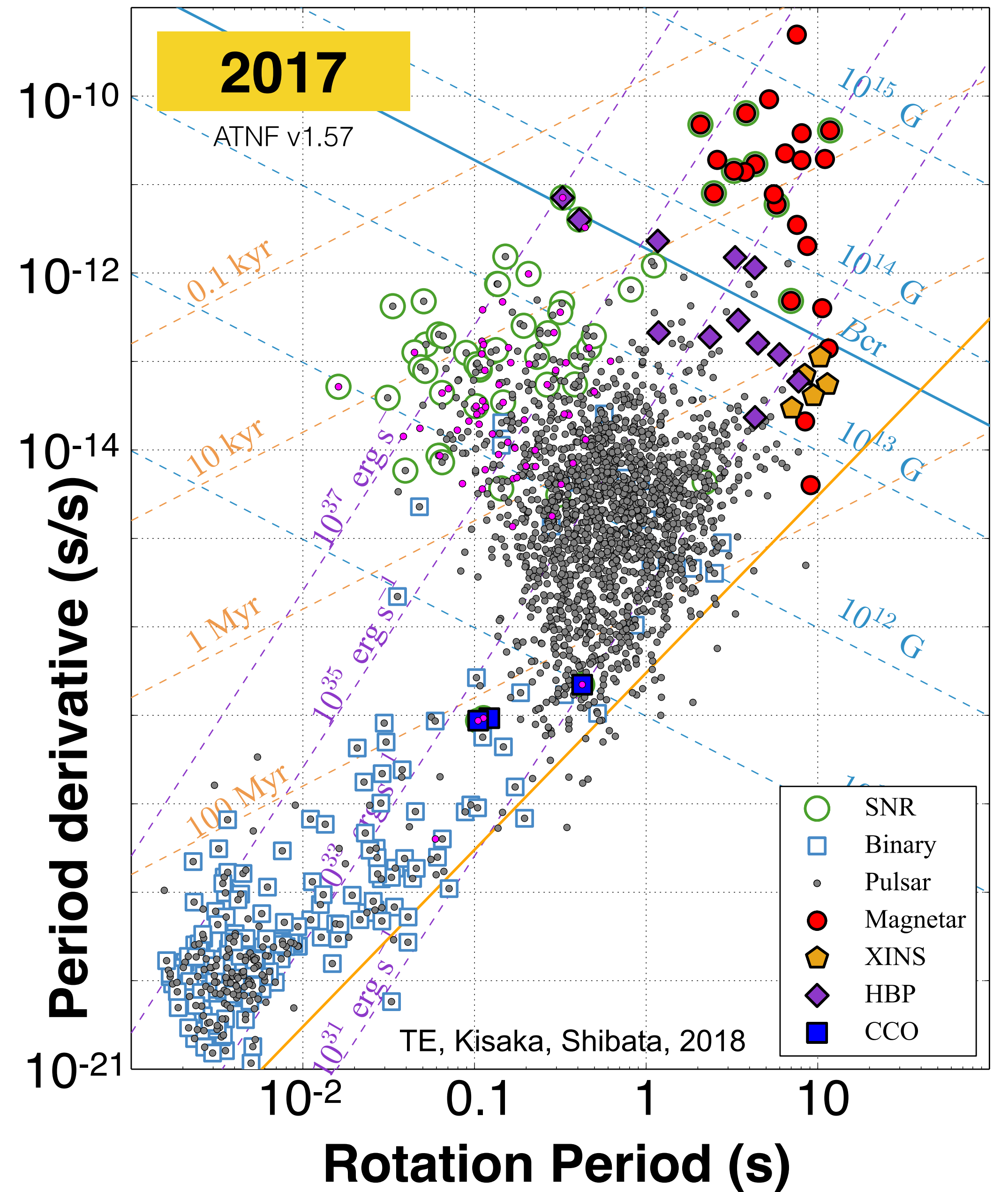
$$= 3.9 \times 10^{46} \frac{\dot{P}}{P^3} \text{ erg/s}$$



$$L_{\text{mag}} = \frac{2}{3c^3} |\ddot{\mu}|^2 = \frac{2}{3c^3} |\mu|^2 \Omega^4 \sin^2 \theta \propto \frac{B^2}{P^4}$$

$$L_{\text{rot}} \sim L_{\text{mag}} \longrightarrow B = 1.0 \times 10^{12} \sqrt{\left(\frac{P}{1 \text{ s}} \right) \left(\frac{\dot{P}}{10^{-15} \text{ s/s}} \right)} \text{ G}$$

- Characteristic age $\tau_c = \frac{P}{2\dot{P}}$

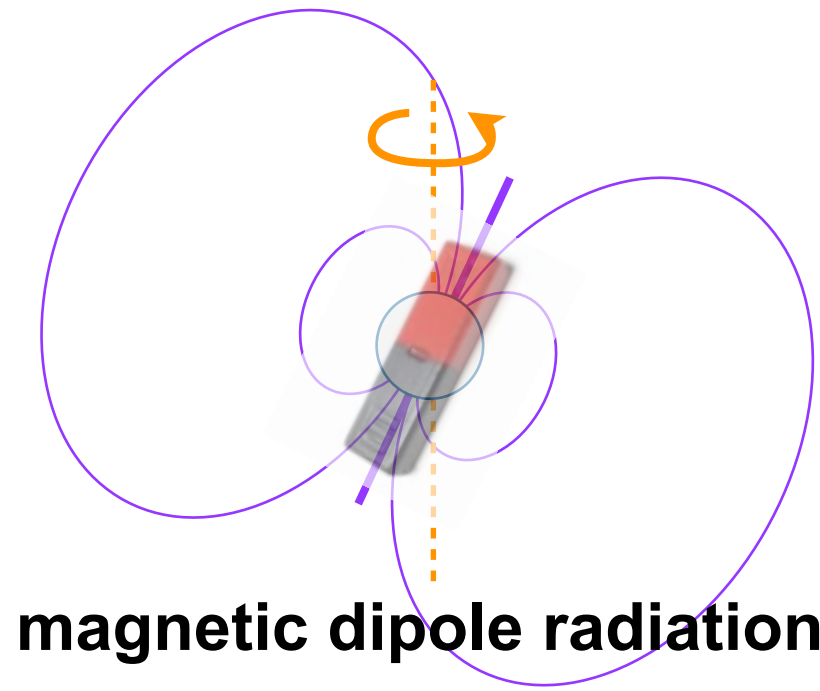


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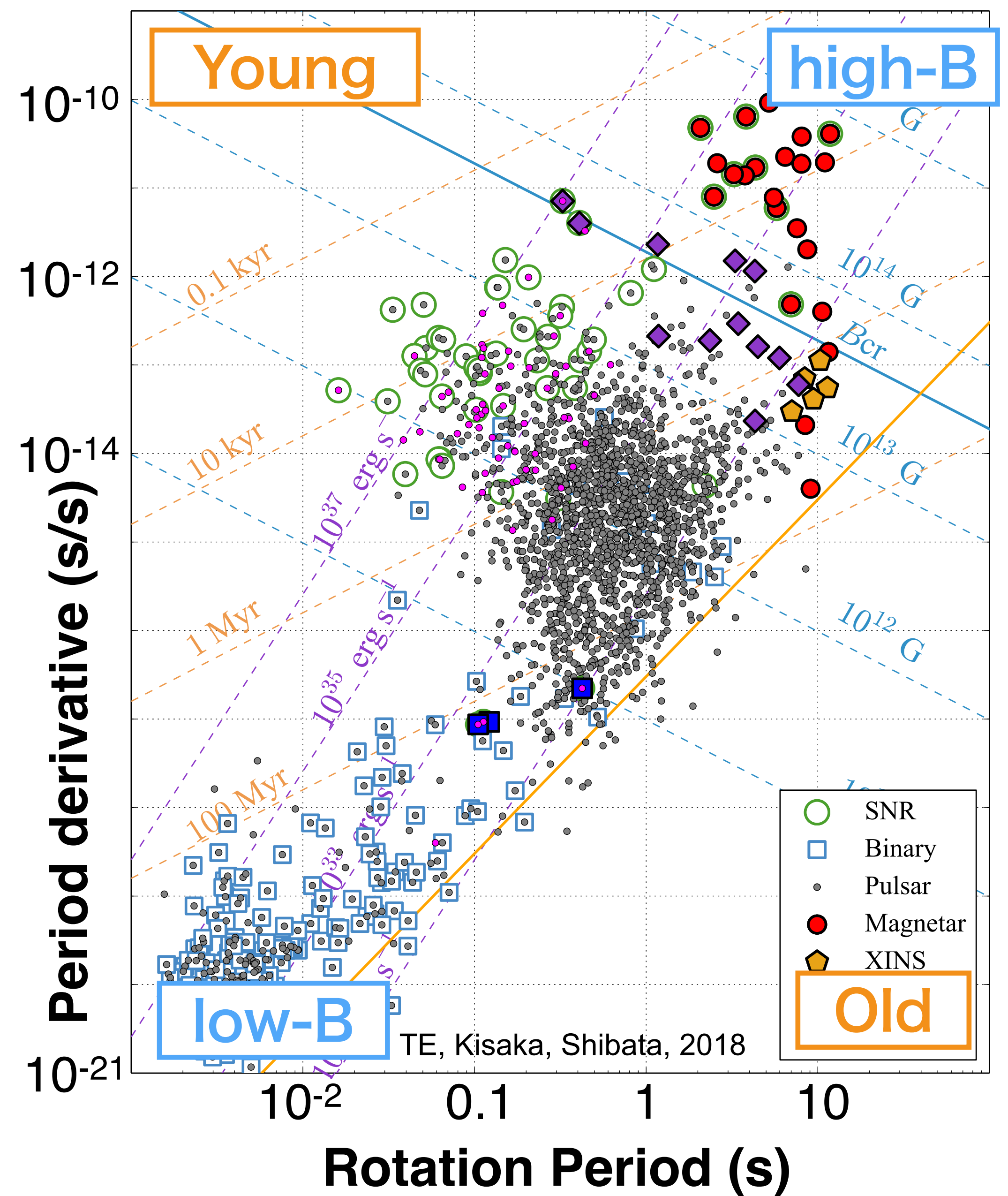
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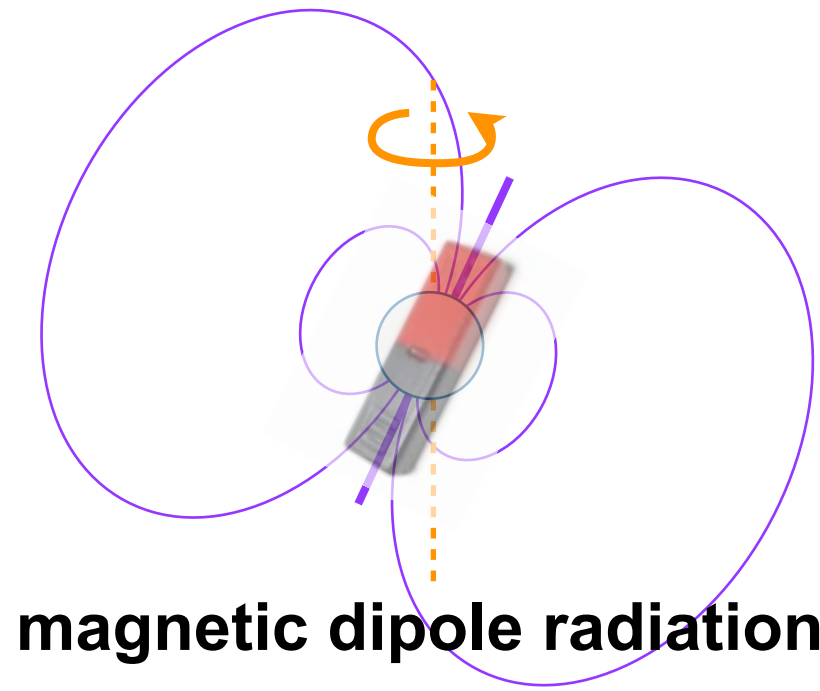


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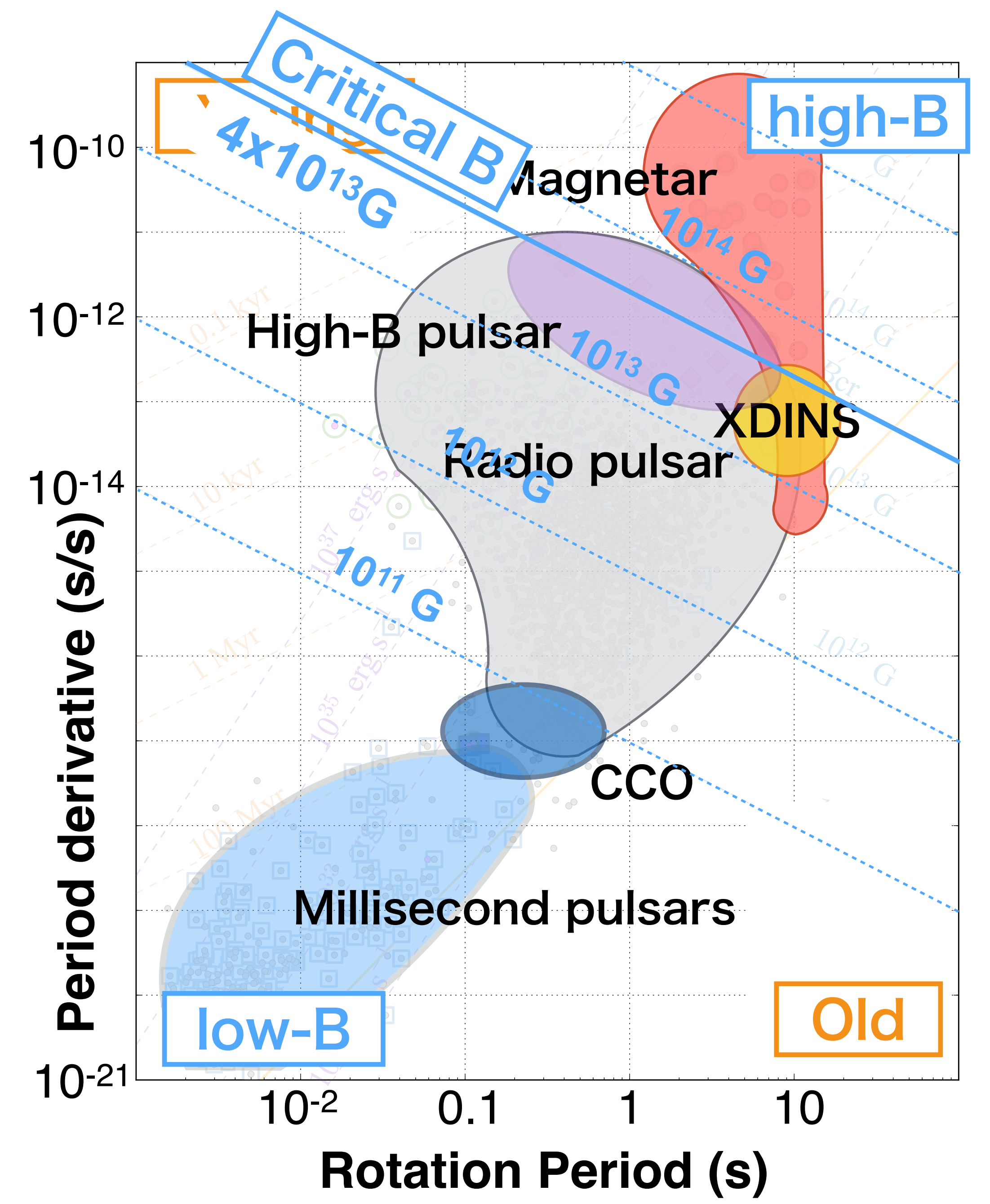
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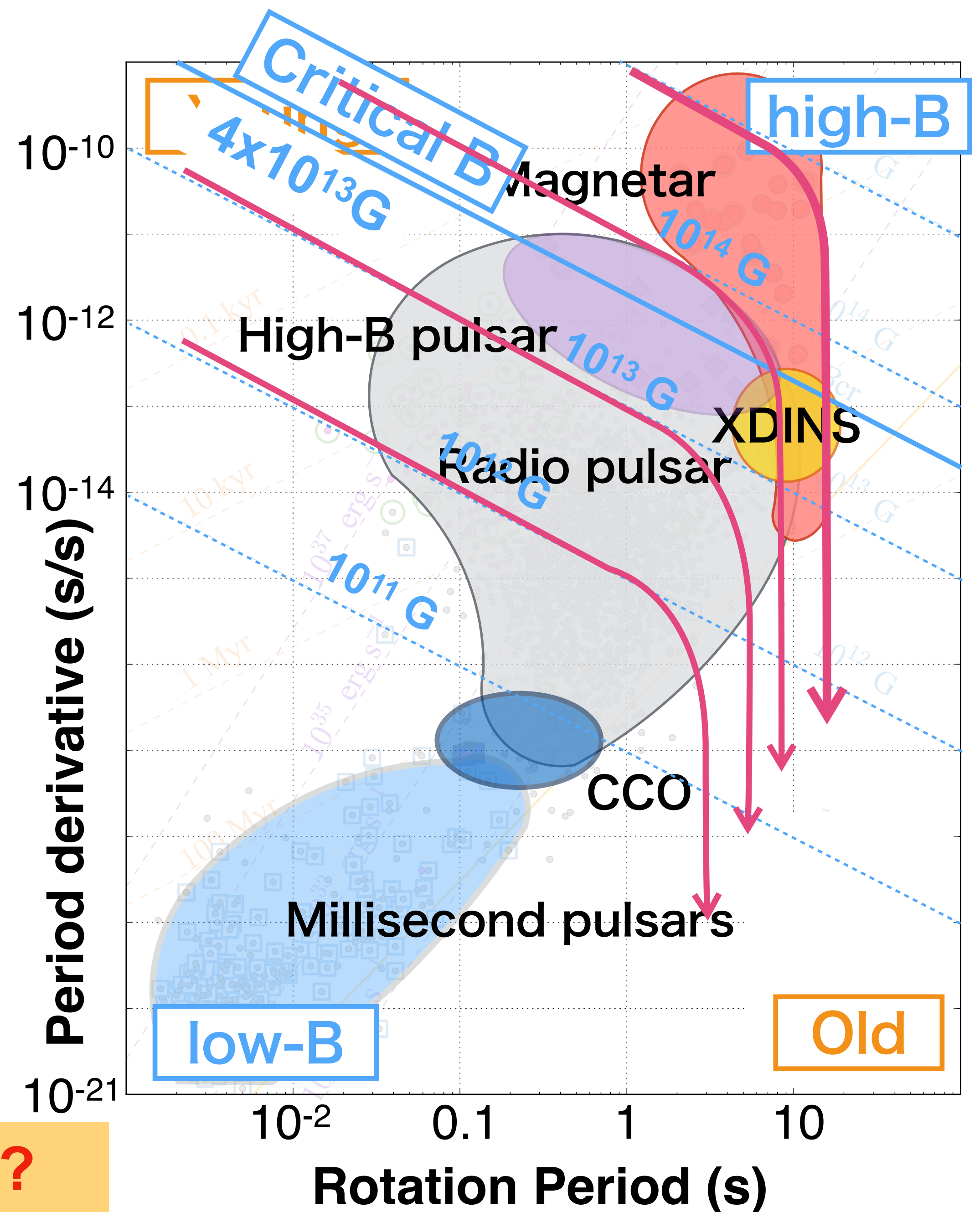
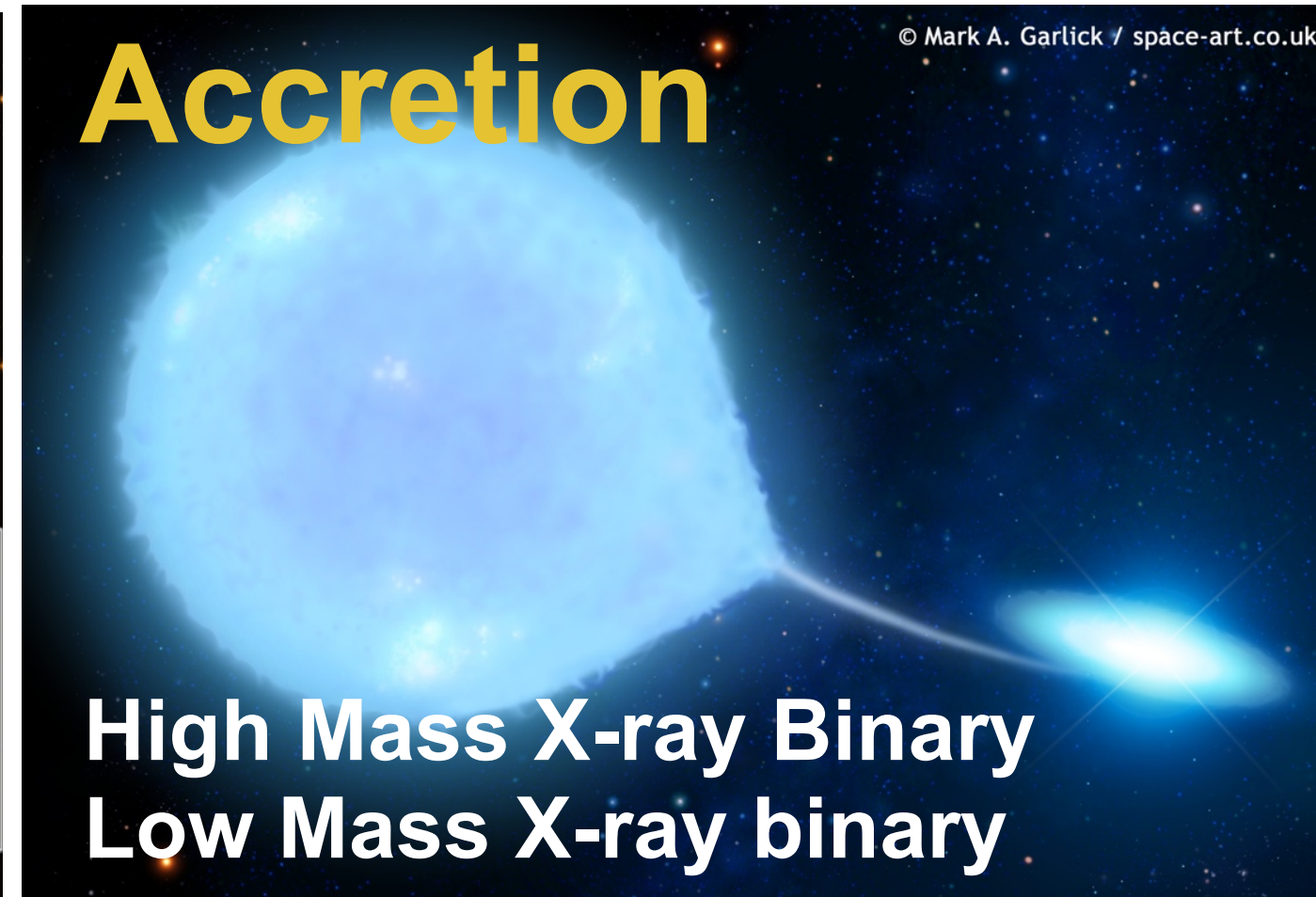
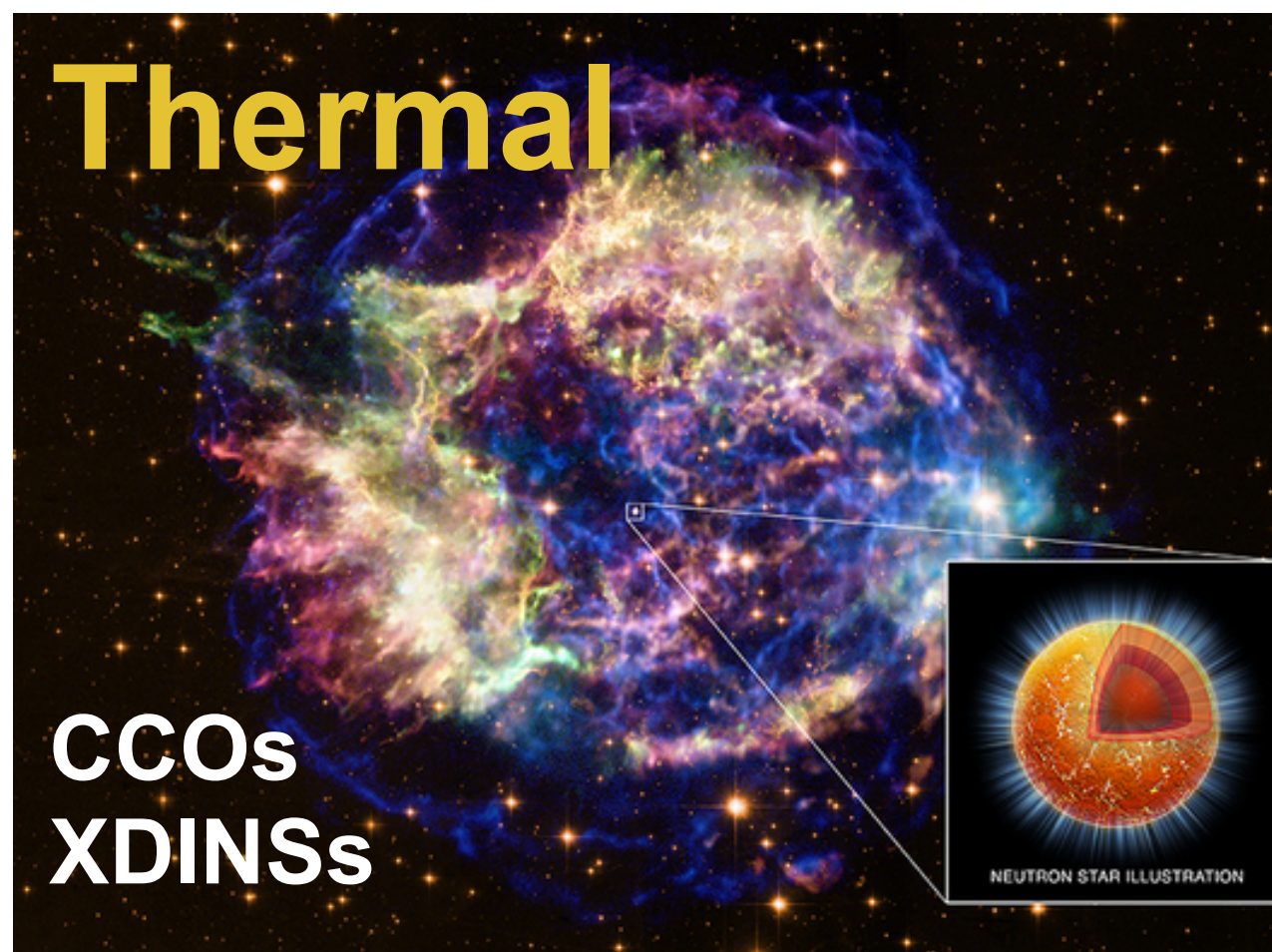
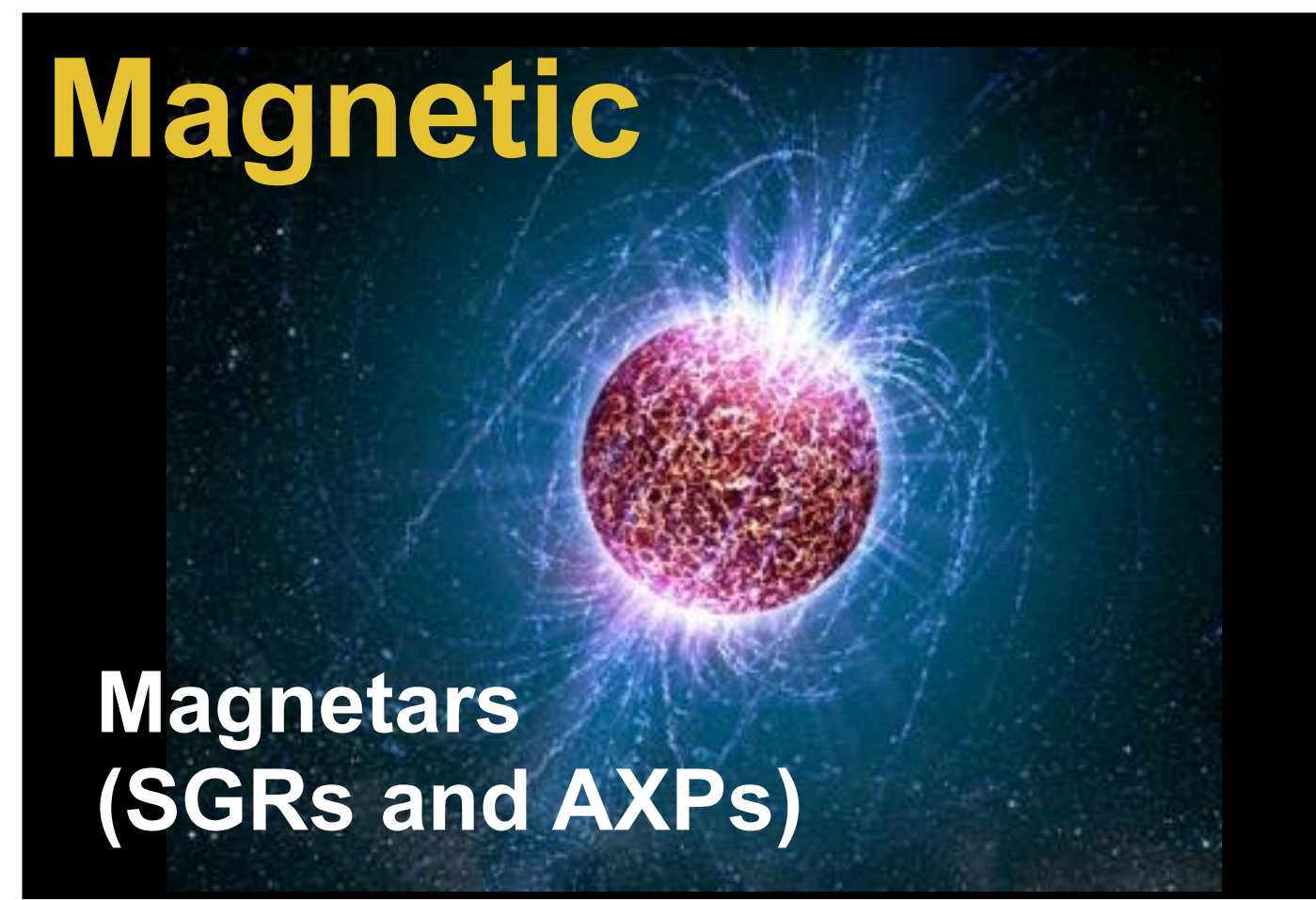
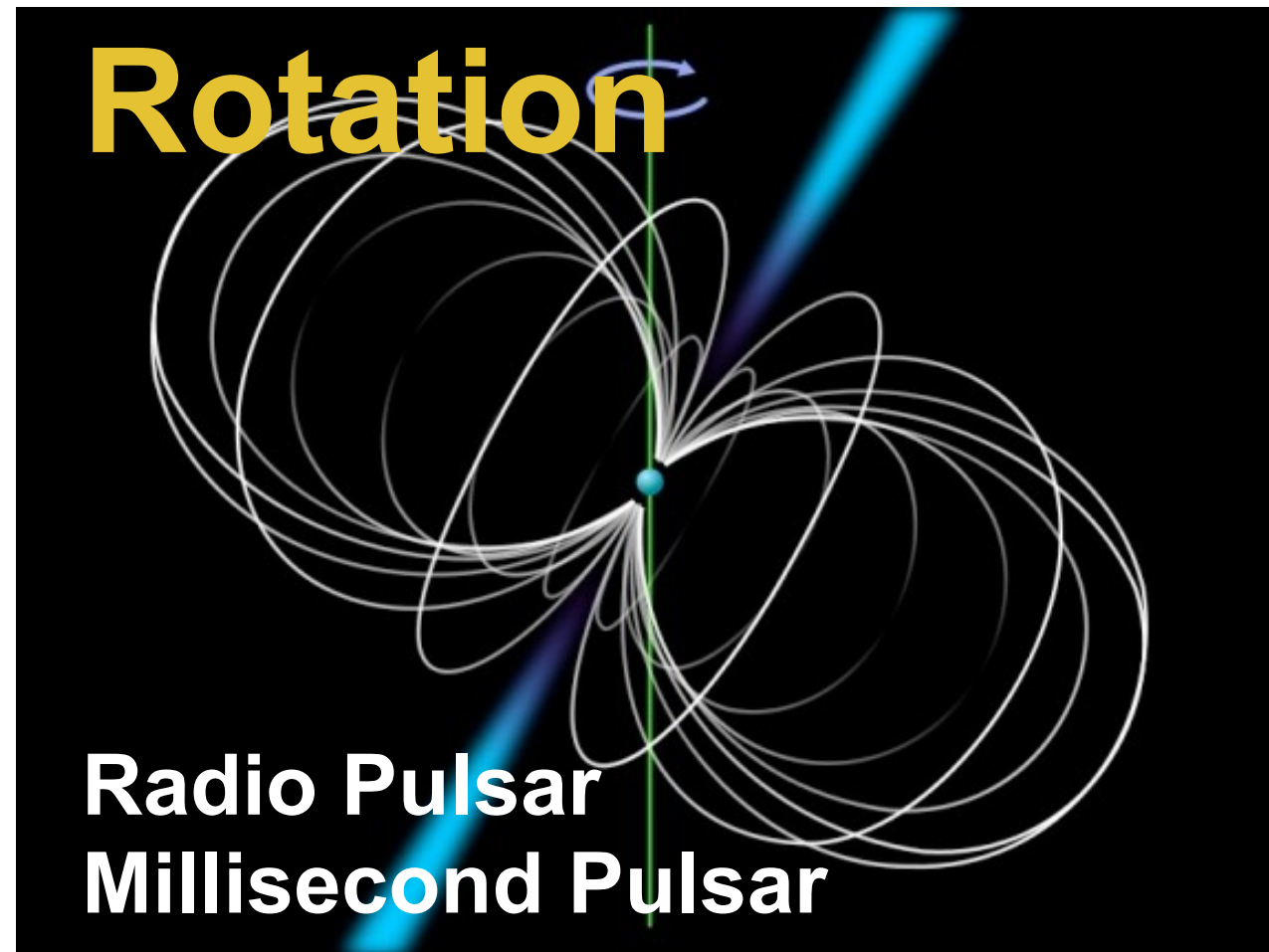
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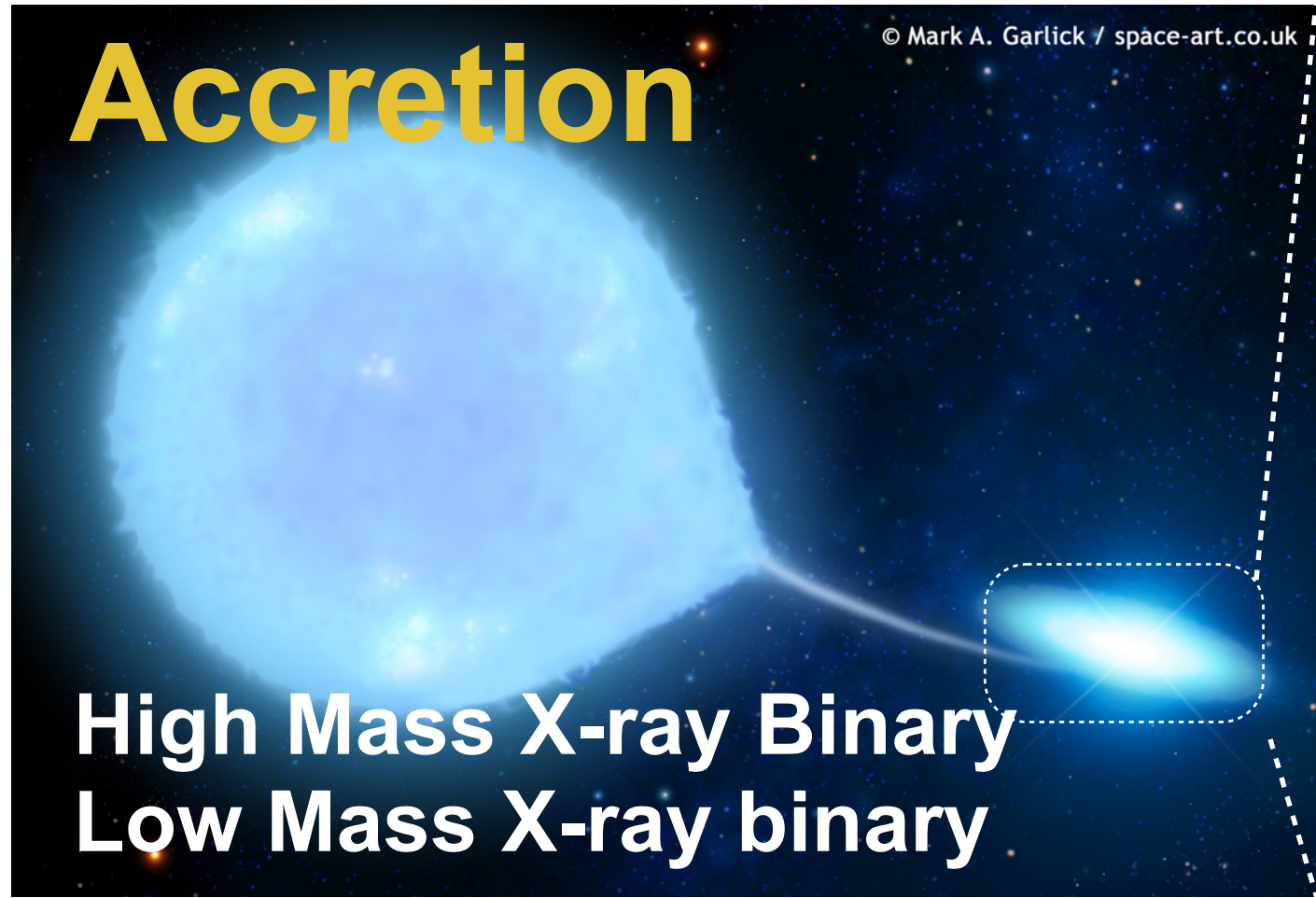
Diversity of Neutron Stars

Energy source of radiation & outflows

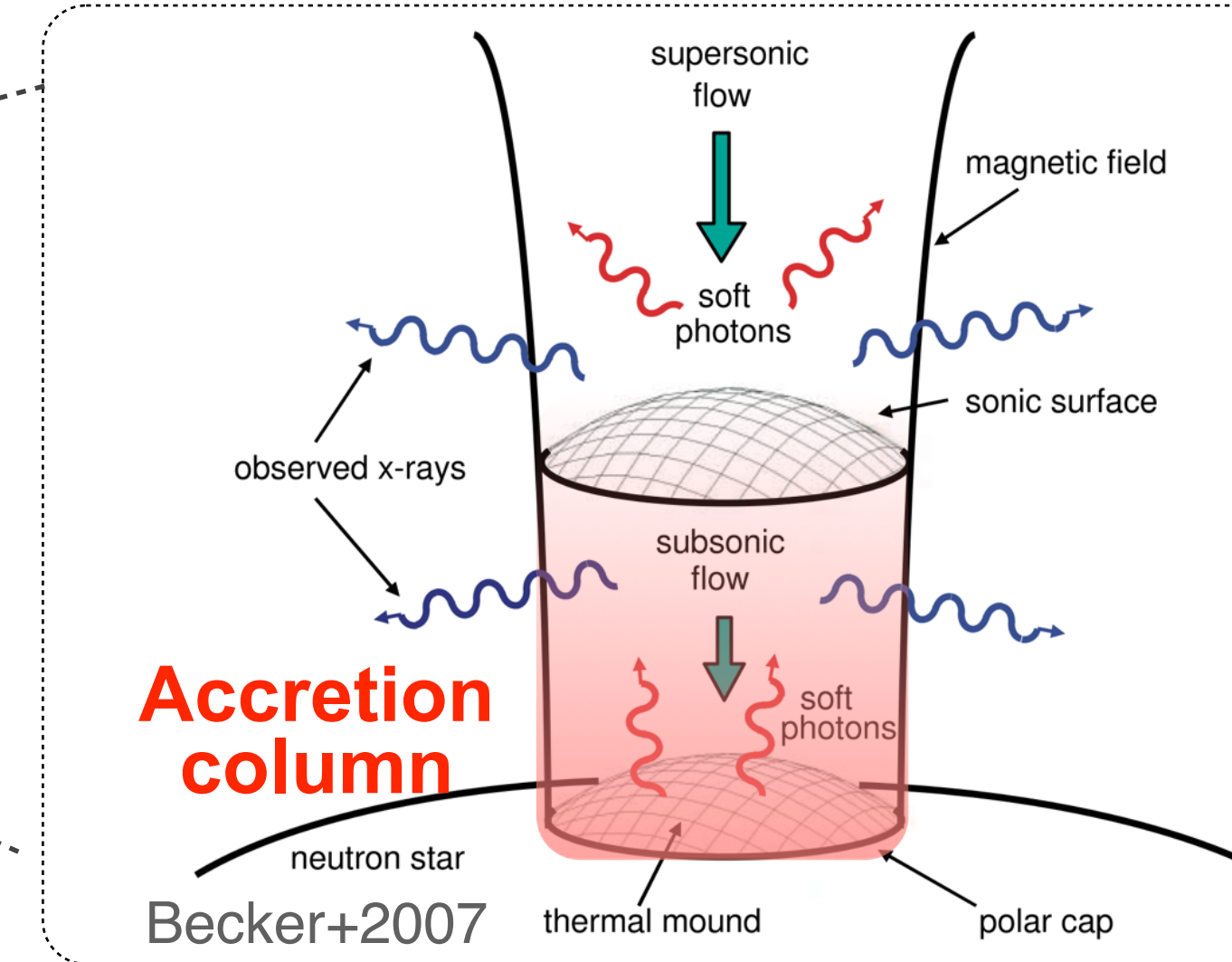
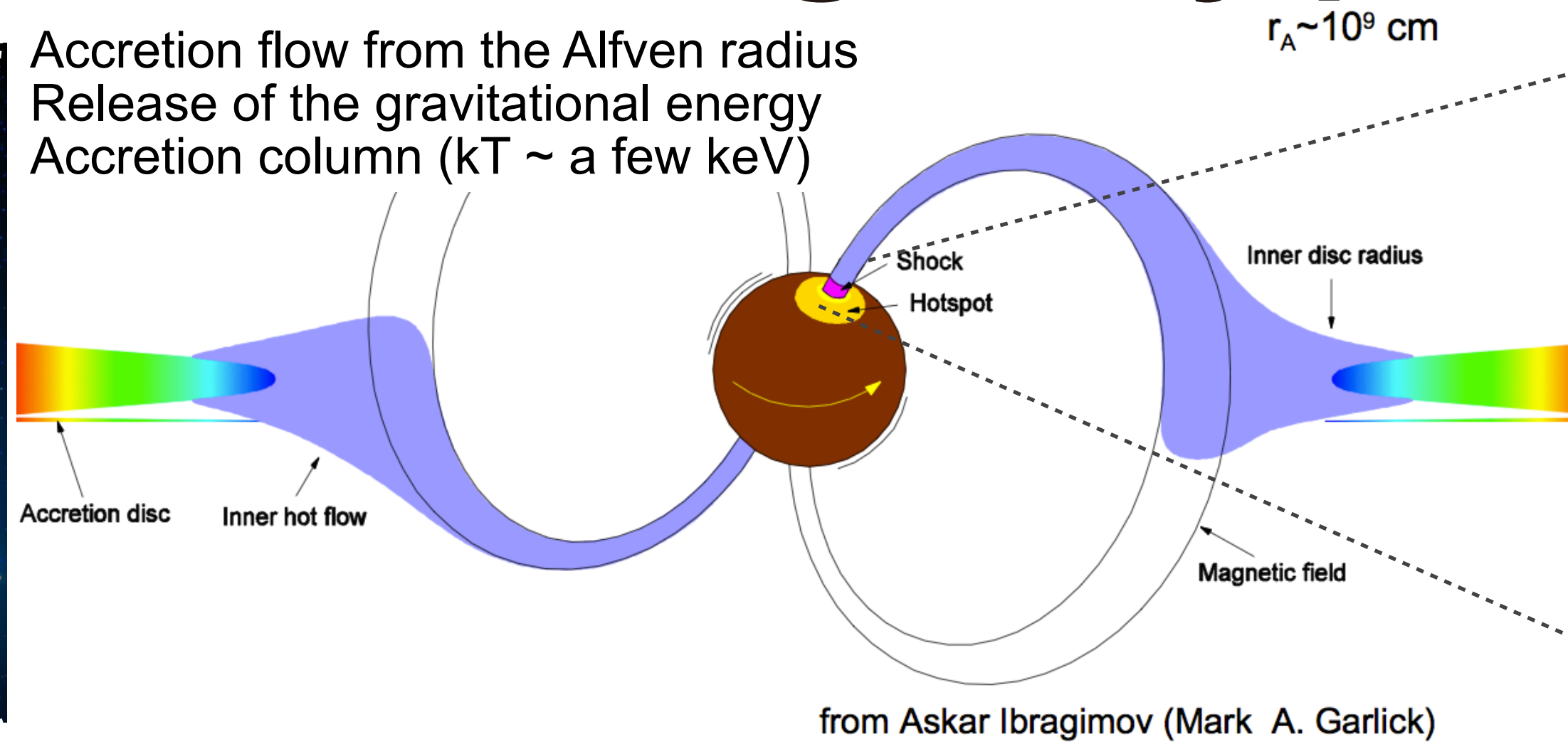


What is the unified evolution theory of NSs?

Magnetic field of accreting X-ray pulsars



Accretion flow from the Alfvén radius
Release of the gravitational energy
Accretion column (kT ~ a few keV)



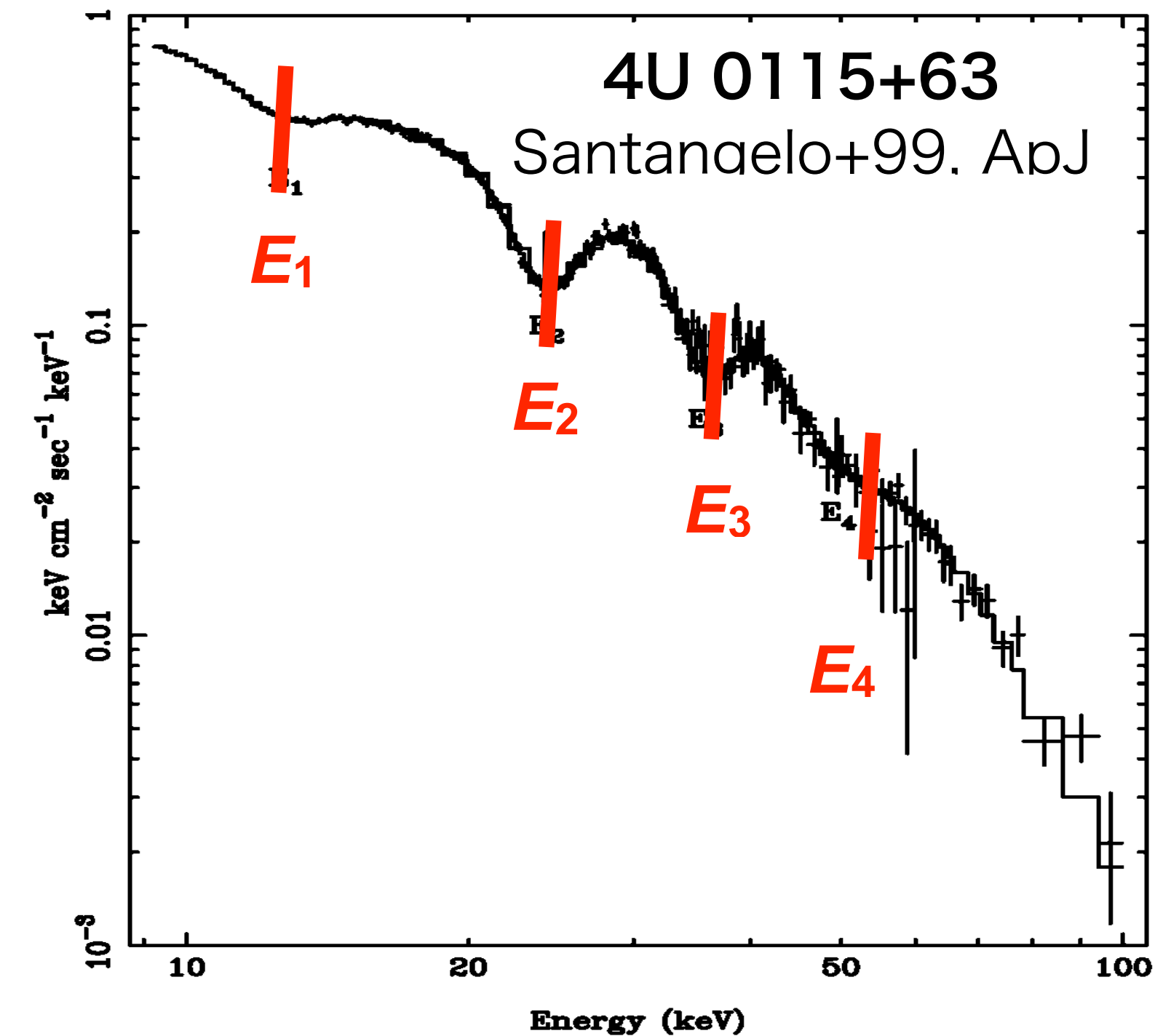
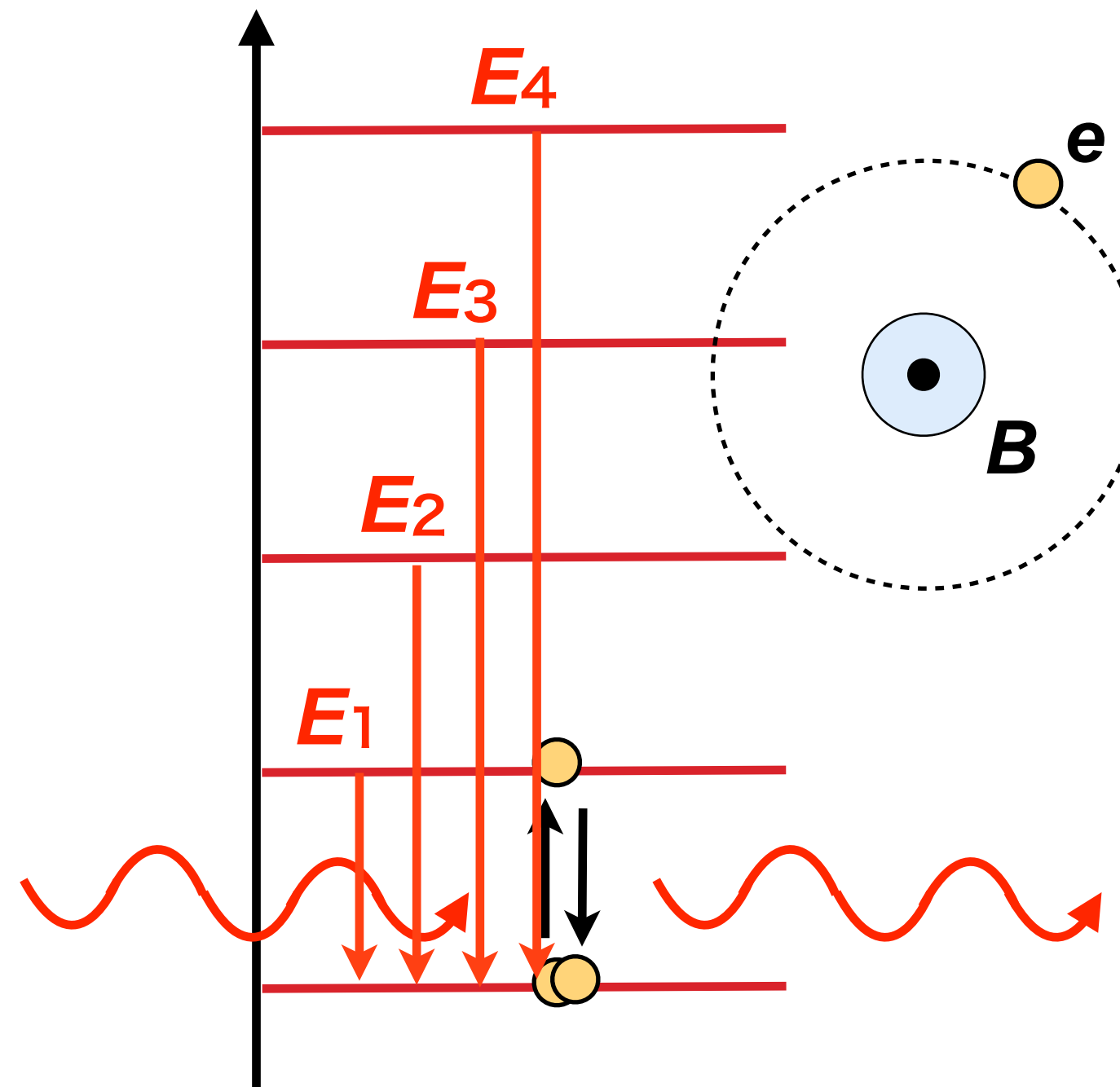
Cyclotron Resonance Scattering Feature (CRSF)

$$E_n = n\hbar\omega_c = m_e c^2 \frac{B}{B_c} \cdot n$$

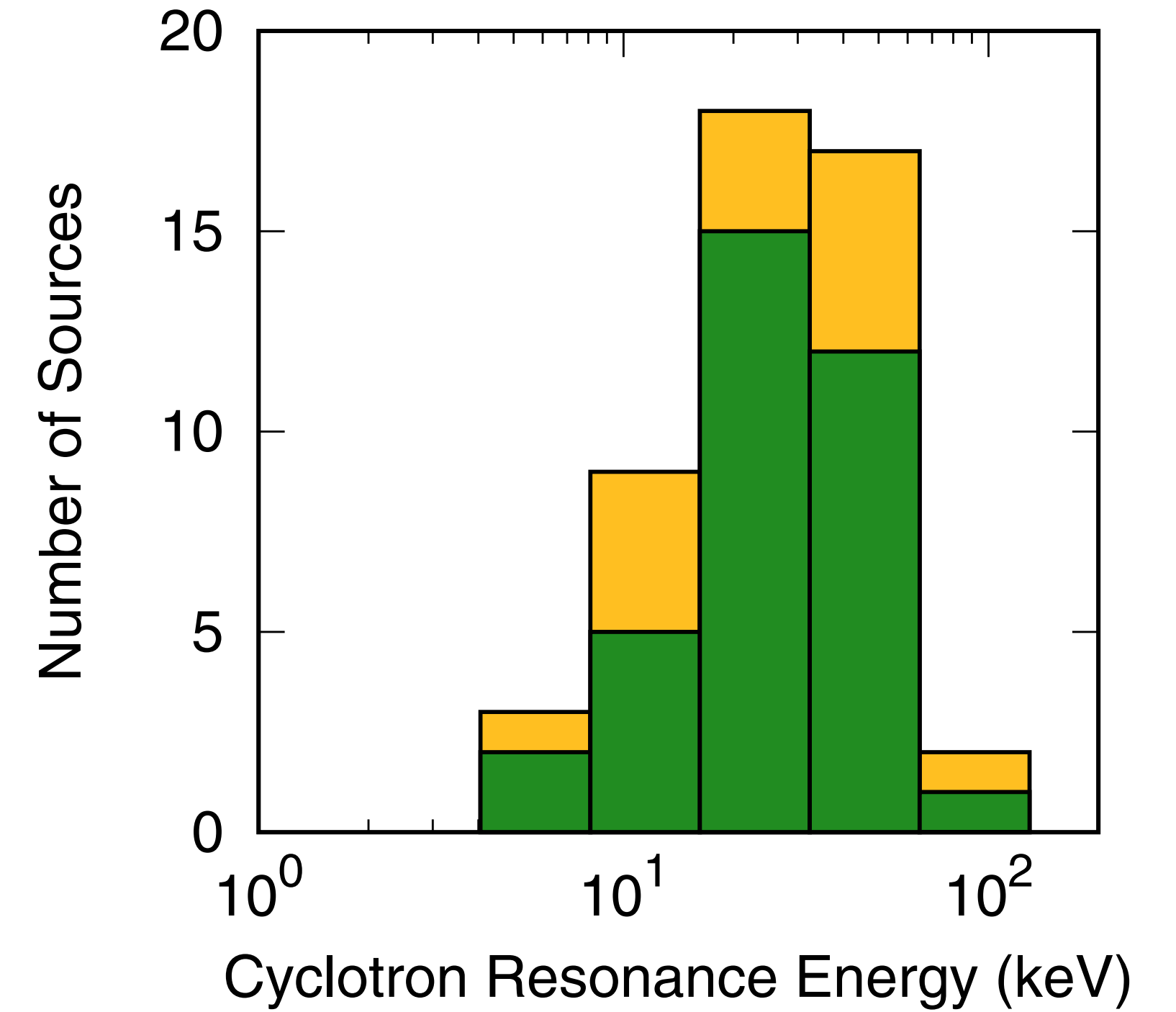
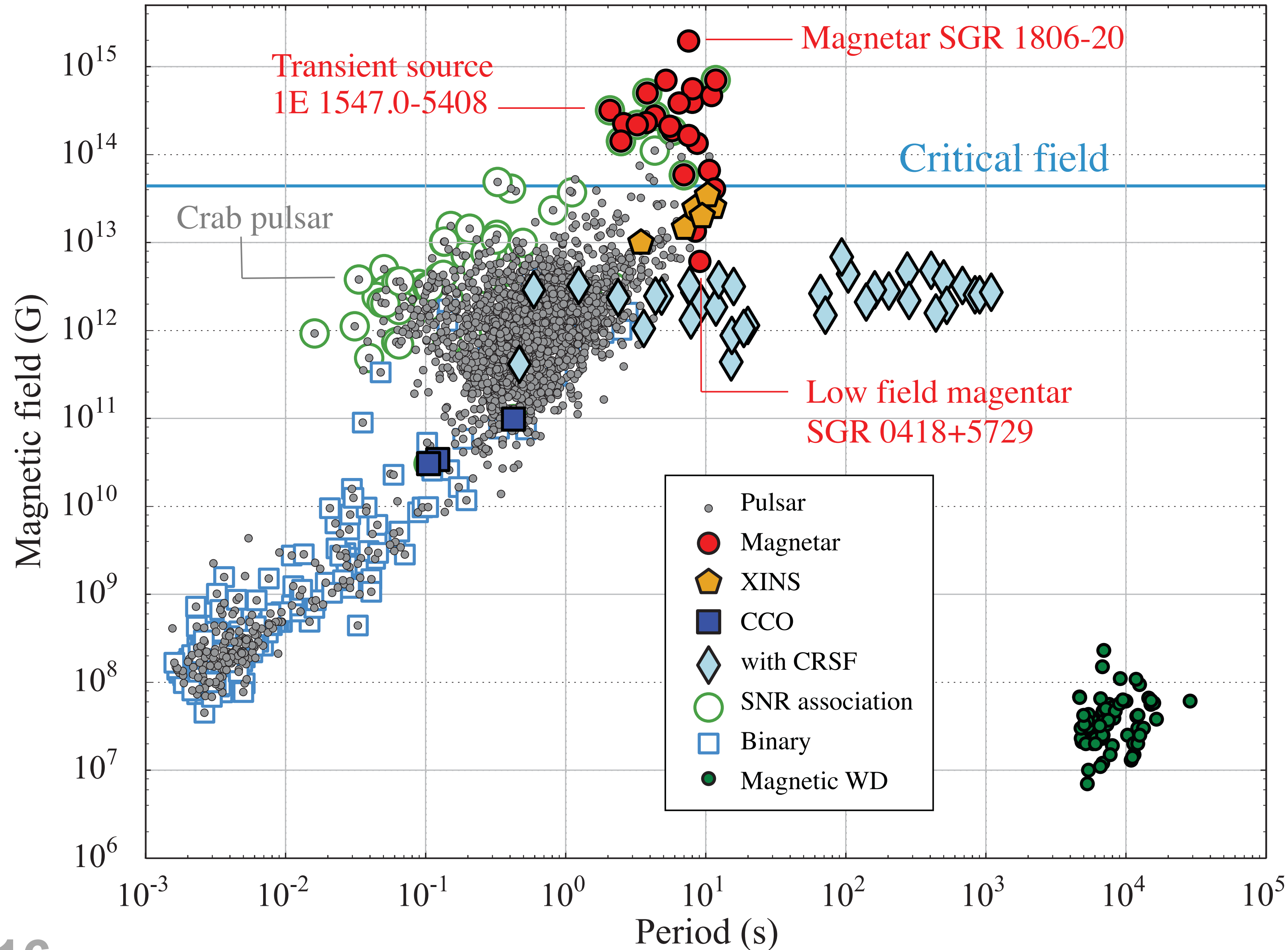
$$B_{cr} = \frac{m_e^2 c^3}{\hbar e} = 4.4 \times 10^9 \text{ T}$$

$$E_n \sim 11 \text{ keV for } B=10^8 \text{ T}$$

cf. atom $E_n = -\frac{\alpha^2}{2} m_e c^2 \cdot \frac{Z^2}{n^2}$



NS rotation period vs. magnetic field strength



- Canonical neutron stars:
 $B \sim 10^{12}$ G ($=10^8$ T)
- Magnetars $B \sim 10^{14-15}$ G
- millisecond pulsars
 $B \sim 10^8-10^9$ G

Review

Observational diversity of magnetized neutron stars

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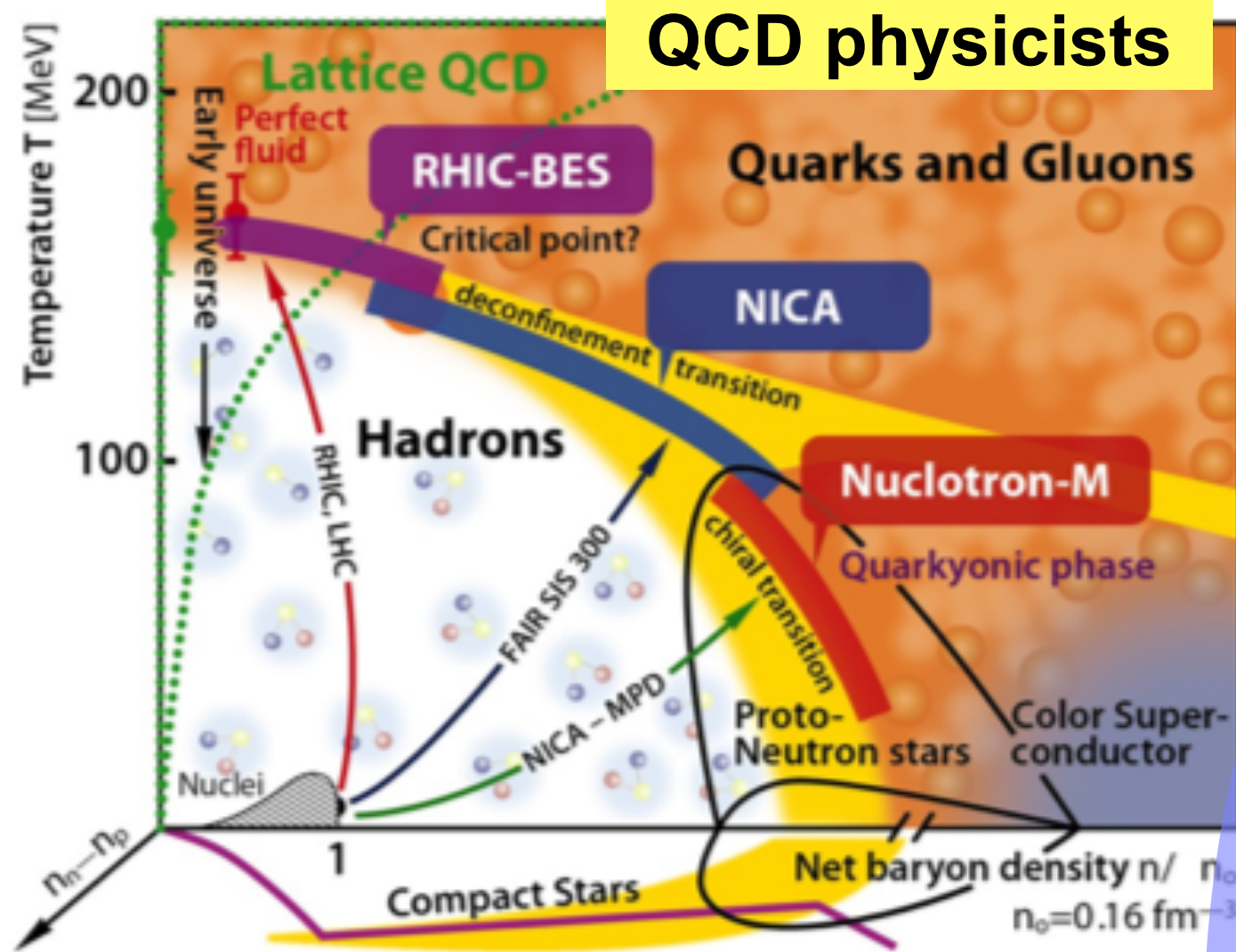


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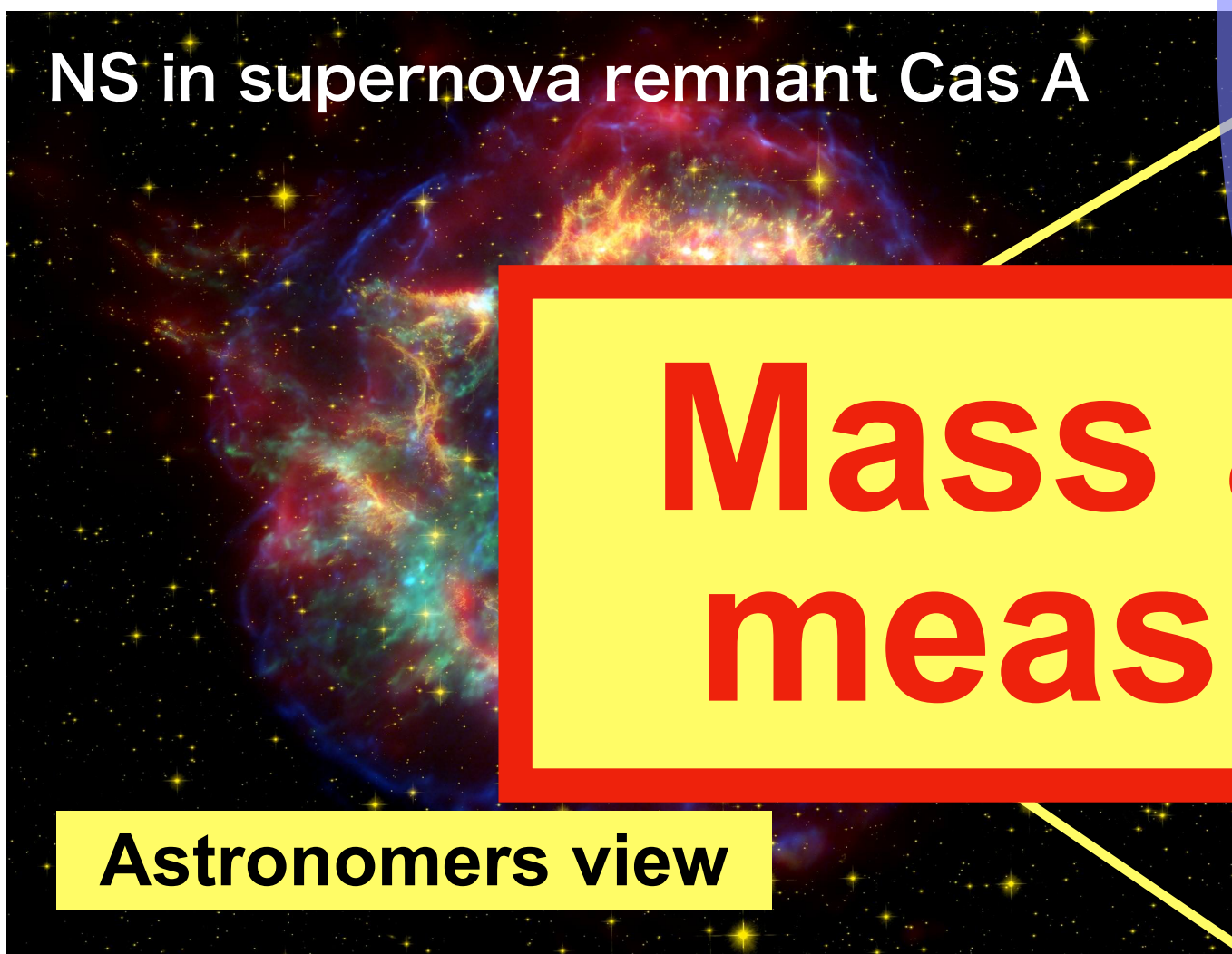
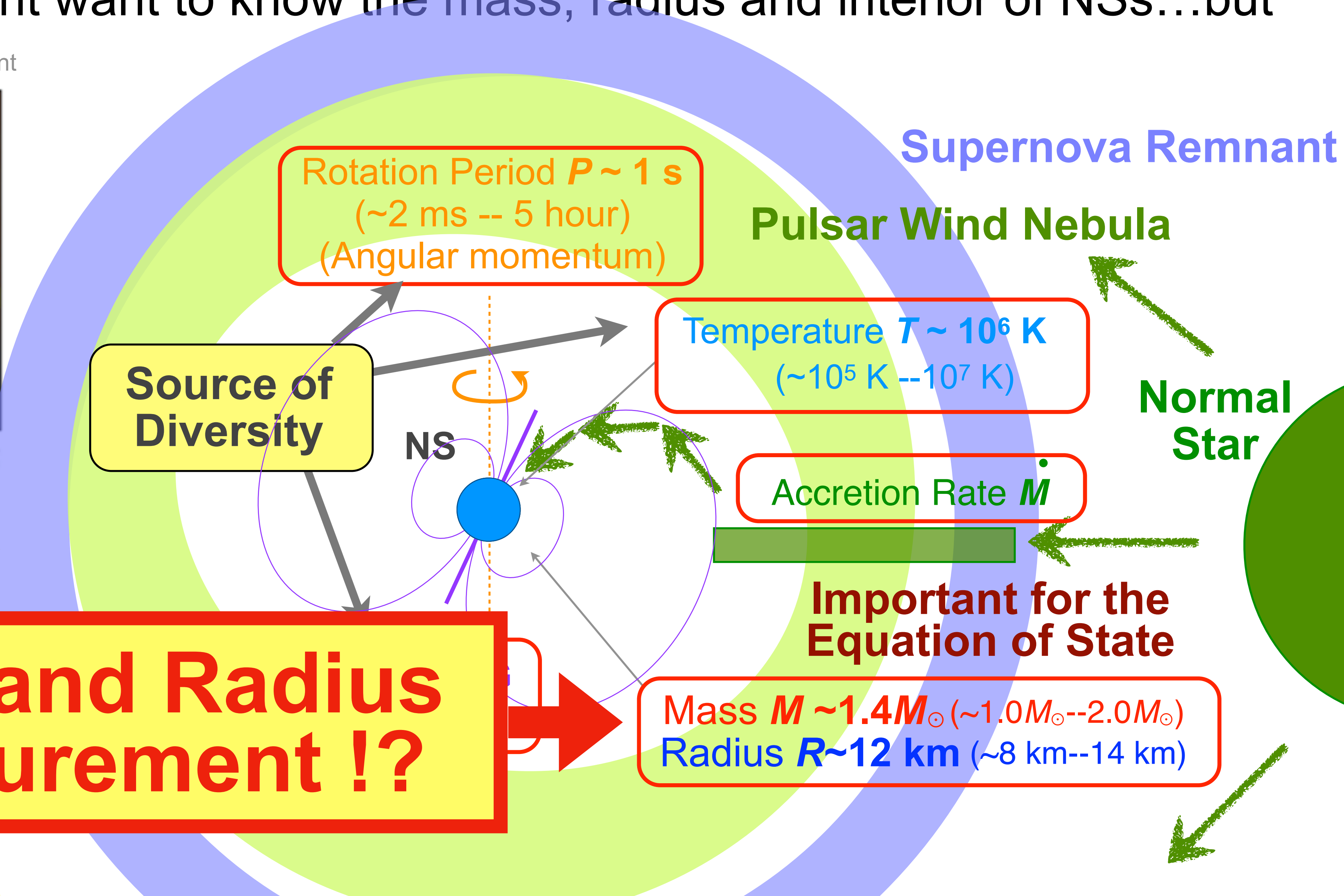
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QCD physicists

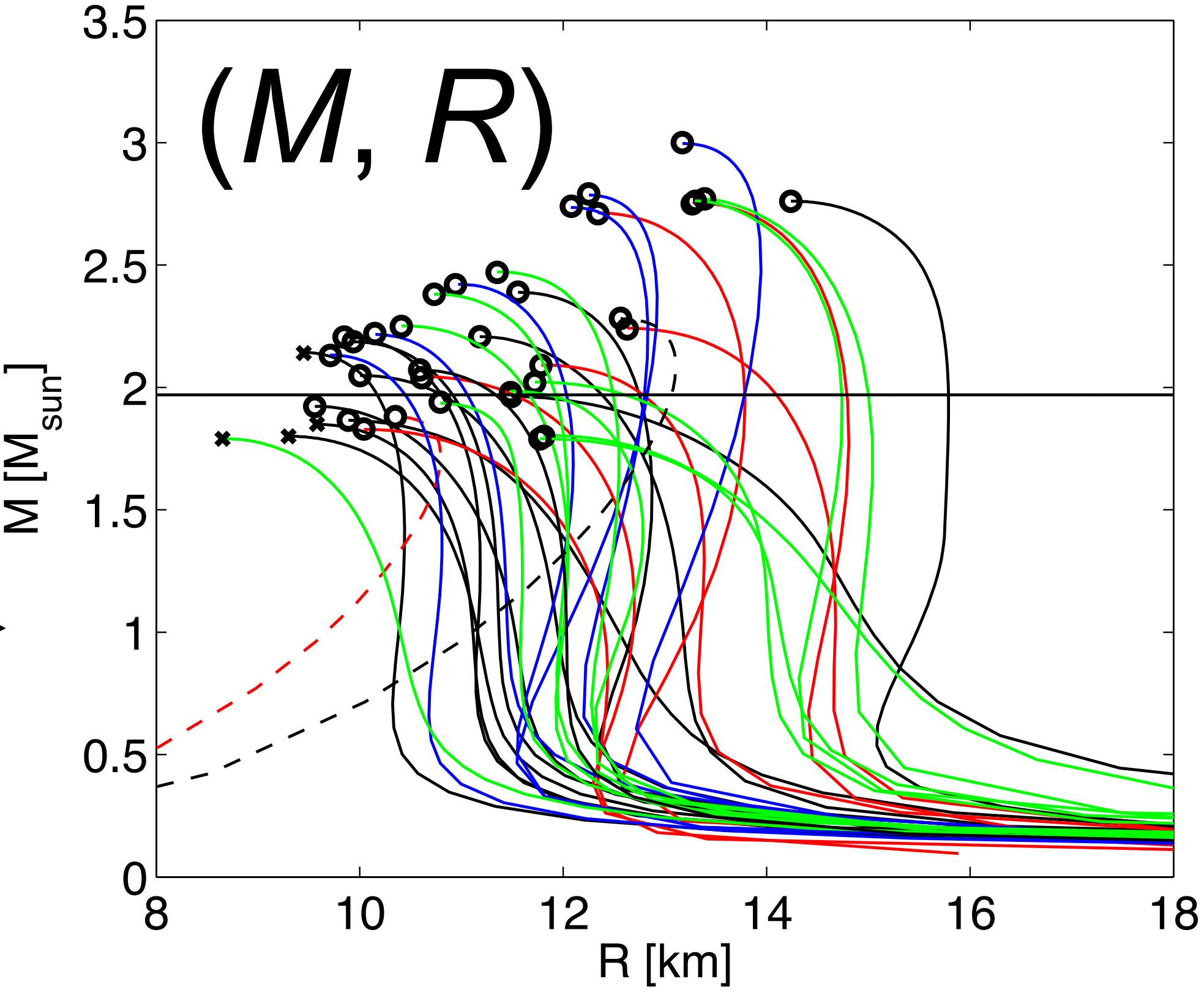
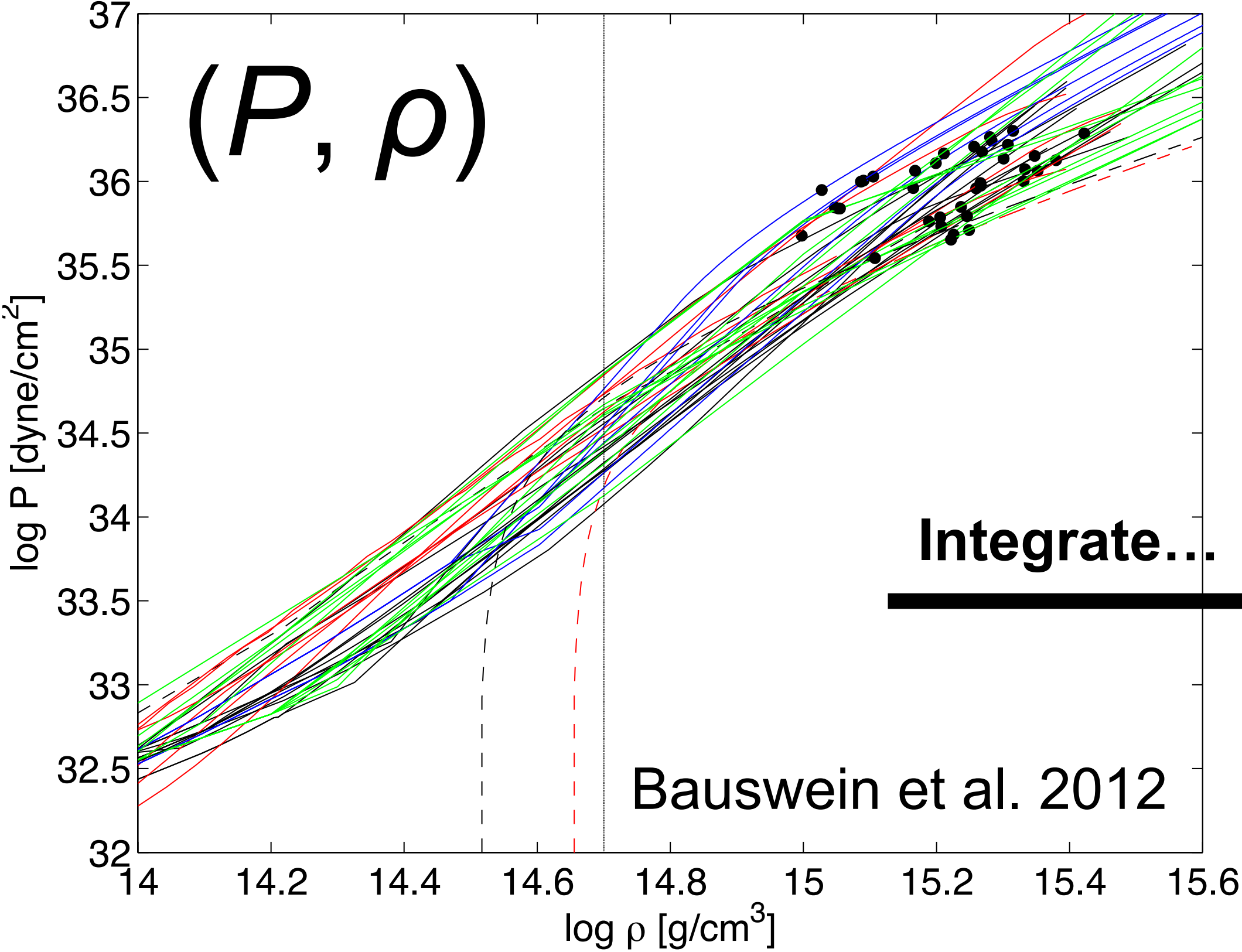


NS in supernova remnant Cas A

Mass and Radius measurement !?

Astronomers view

Equation of state of neutron star nuclear matter



$$\frac{dP}{dr} = -\rho \frac{GM(r)}{r^2}$$

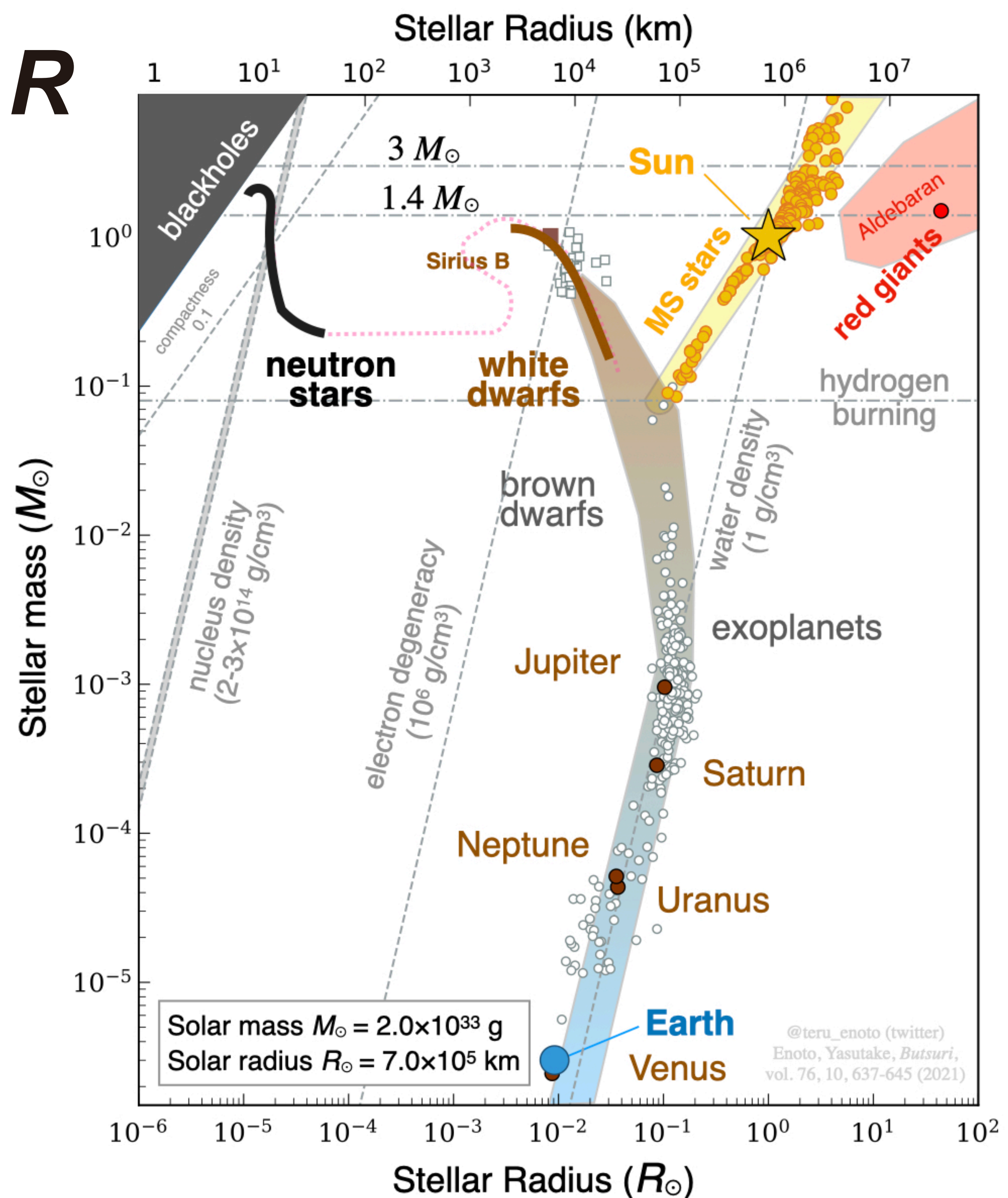
Outward Gravity

Pressure valance
(Non relativistic case,
Relativistic case is
the TOV equation)

- The state equation (P, ρ) corresponds to the curve of macroscopic mass and radius (M, R)
- and can be expected to be measured in astronomical observation.

Stellar mass M and radius R

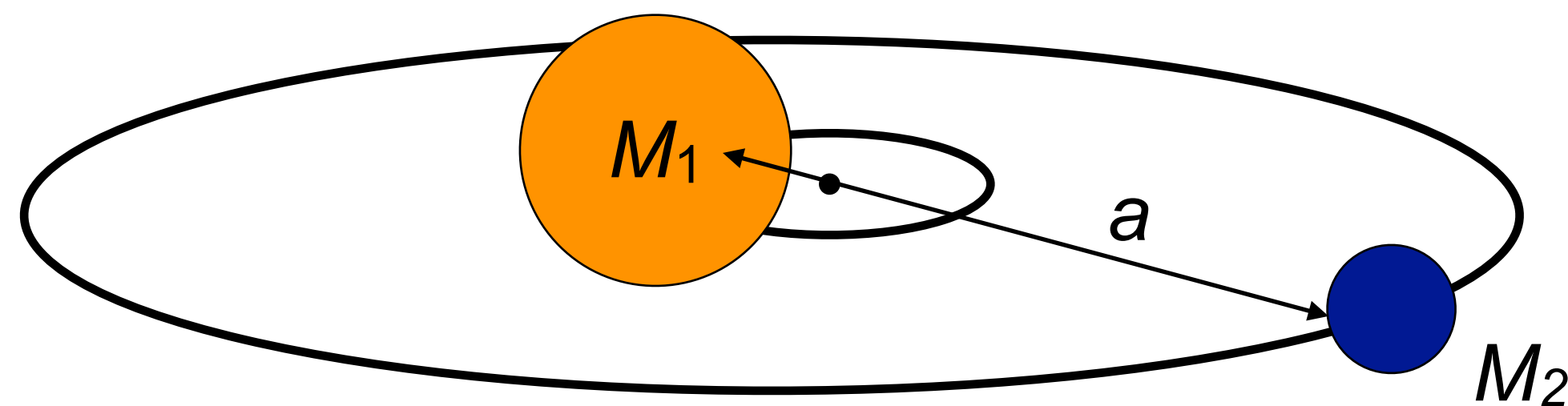
- M and R of various celestial bodies (self-gravitational systems) are determined by the equation of state (including internal structure, composition, pressure...)
- Planet: electrical repulsion $M \sim R^3$
- Star: gas & radiation pressure $M \sim R$
- White dwarf: e-degenerate pressure $M \sim R^{-1/3}$
- Neutron stars: n-degenerate pressure $M \sim R^0$
- Observational data is scattered around the M-R relation with large uncertainties.
- Equation of state of neutron stars (and thus the M-R relation) requires precise astronomical observations in the upper left region.



Astronomical measurements of mass and radius

Mass

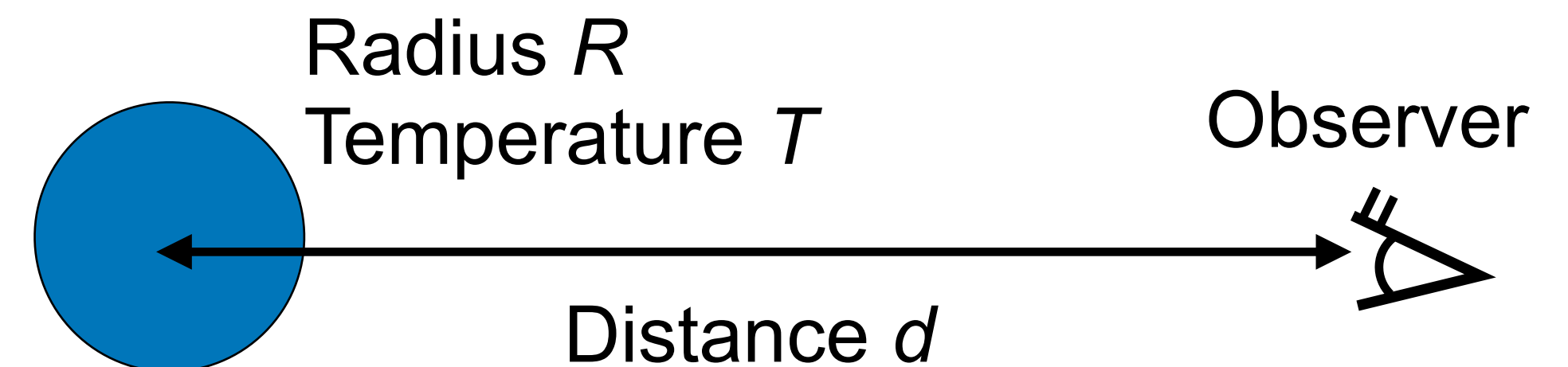
- Measurement using pulsation in radio, X-rays, gamma rays to measure the binary orbital motion
- Precise



$$G(M_1 + M_2) = a^3 \left(\frac{2\pi}{P} \right)^2$$

Radius

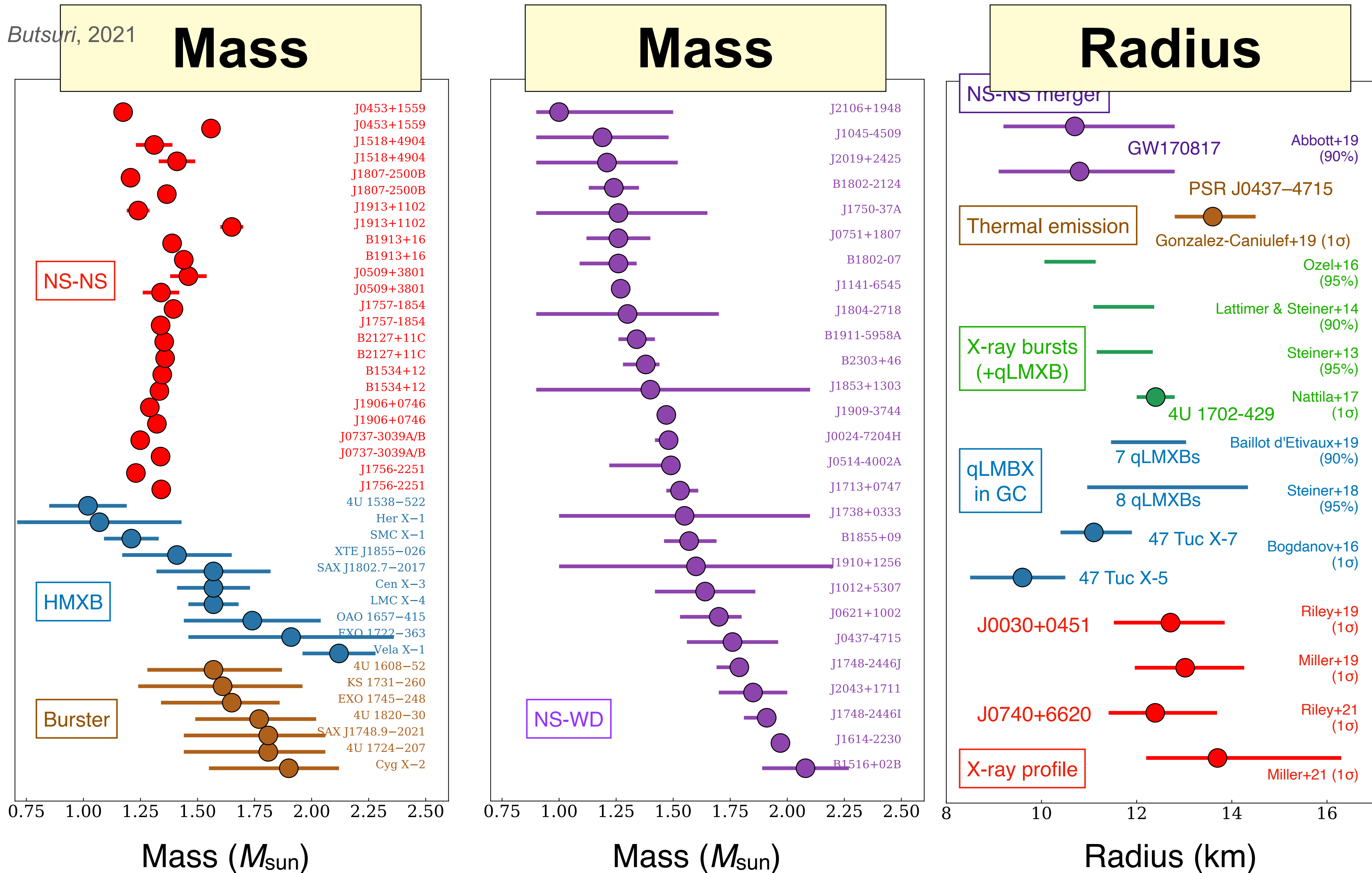
- Necessary to estimate the radius from the surface radiation in X-rays
- Large uncertainties, e.g., distance and atmospheric composition.



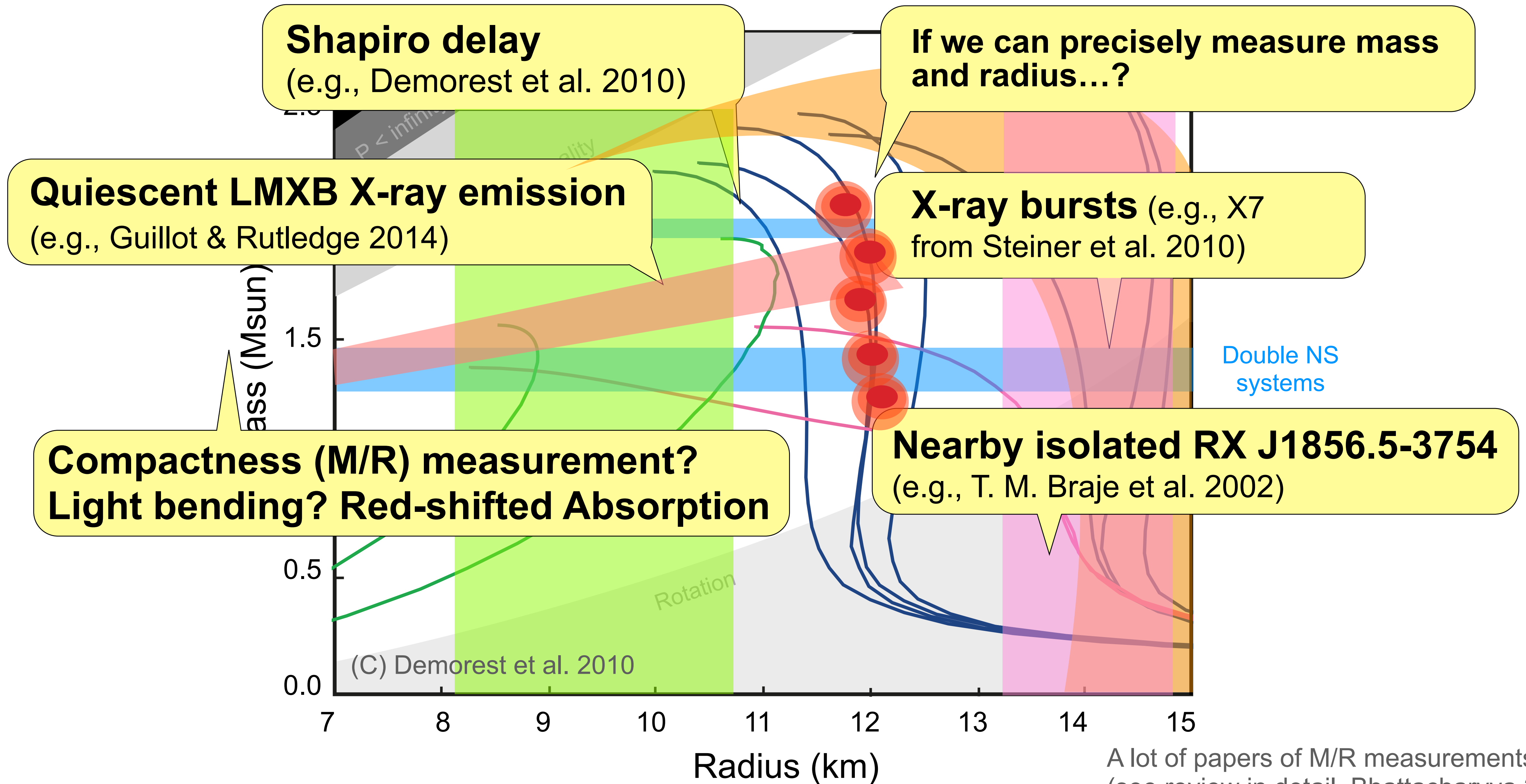
$$f = \frac{L}{4\pi d^2} = \frac{4\pi R^2 \sigma T^4}{4\pi d^2}$$

Astronomical measurements of mass and radius

Enoto, Yasutake, *Butsuri*, 2021

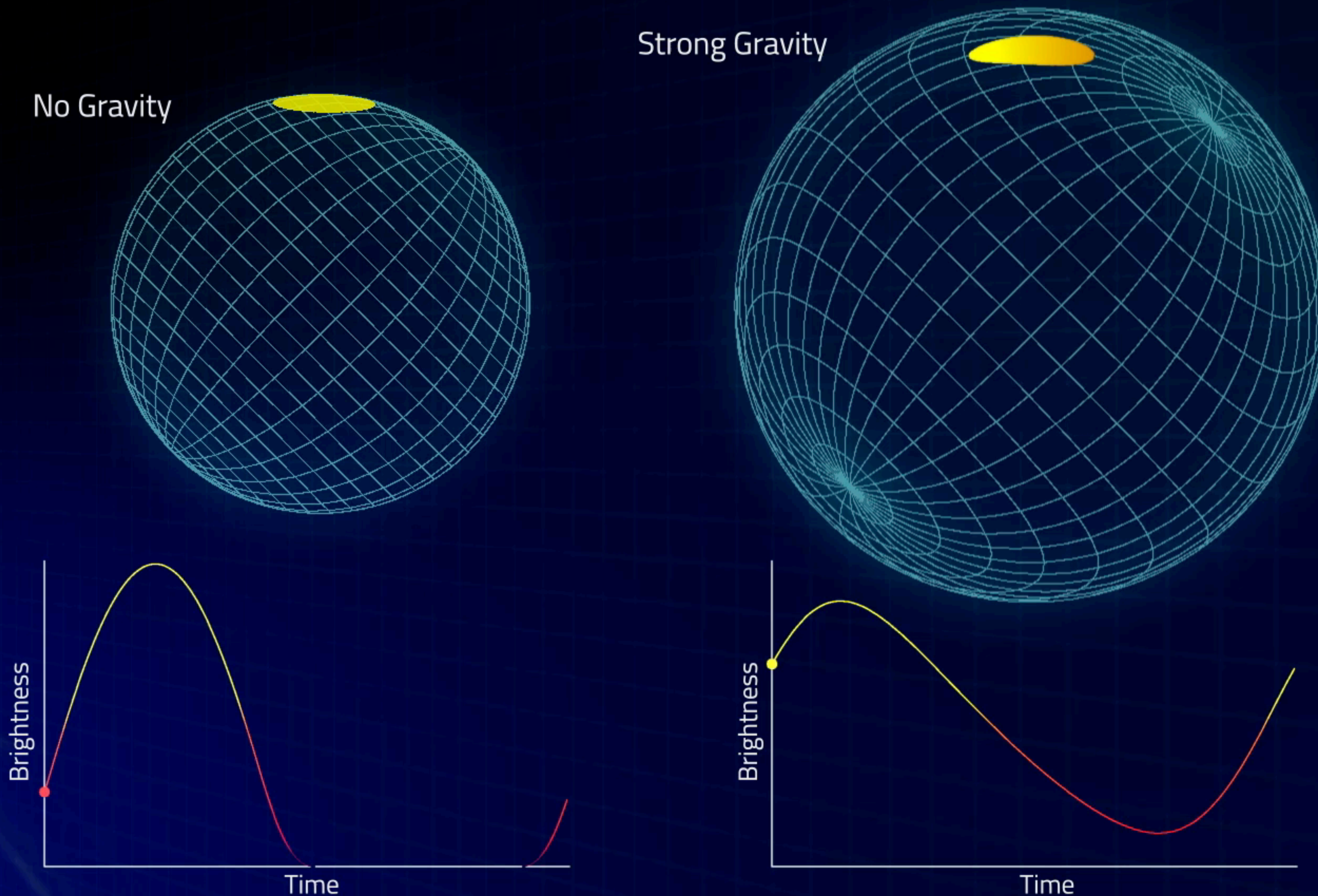


Astronomical measurements of mass and radius



A lot of papers of M/R measurements
(see review in detail, Bhattacharyya 2010)

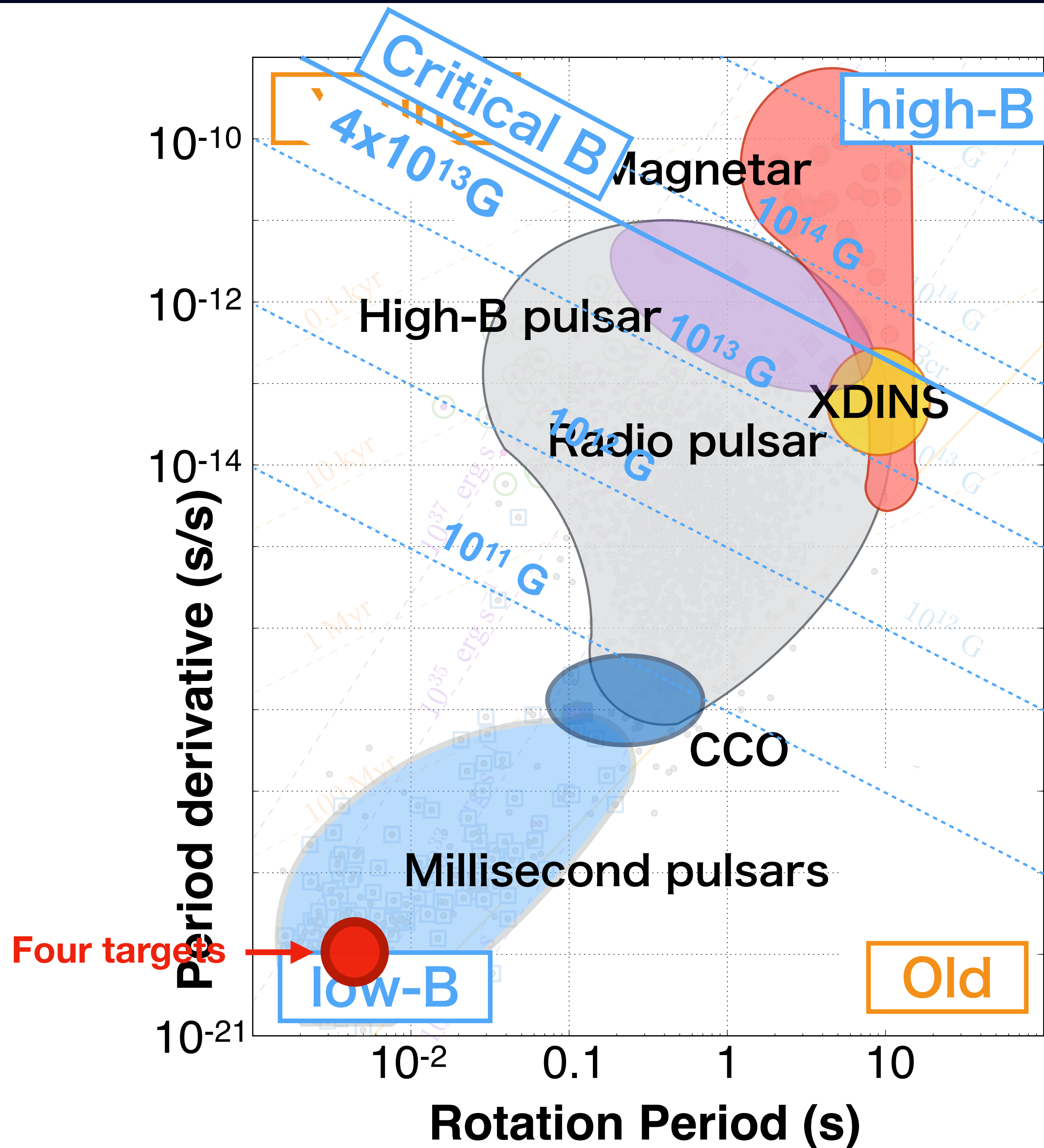
Light-bending for compactness measurements



- X-ray pulse profile from a surface hot spot is affected by the gravitational light bending. Comparison between the observation and precise modeling gives the compactness (M/R)
- Target: Non-accretion stable millisecond pulsars with a high rotation speed and low magnetic field.

Light

measurements



- X-ray pulse profile from a surface hot spot is affected by the gravitational light bending. Comparison between the observation and precise modeling gives the compactness (M/R)
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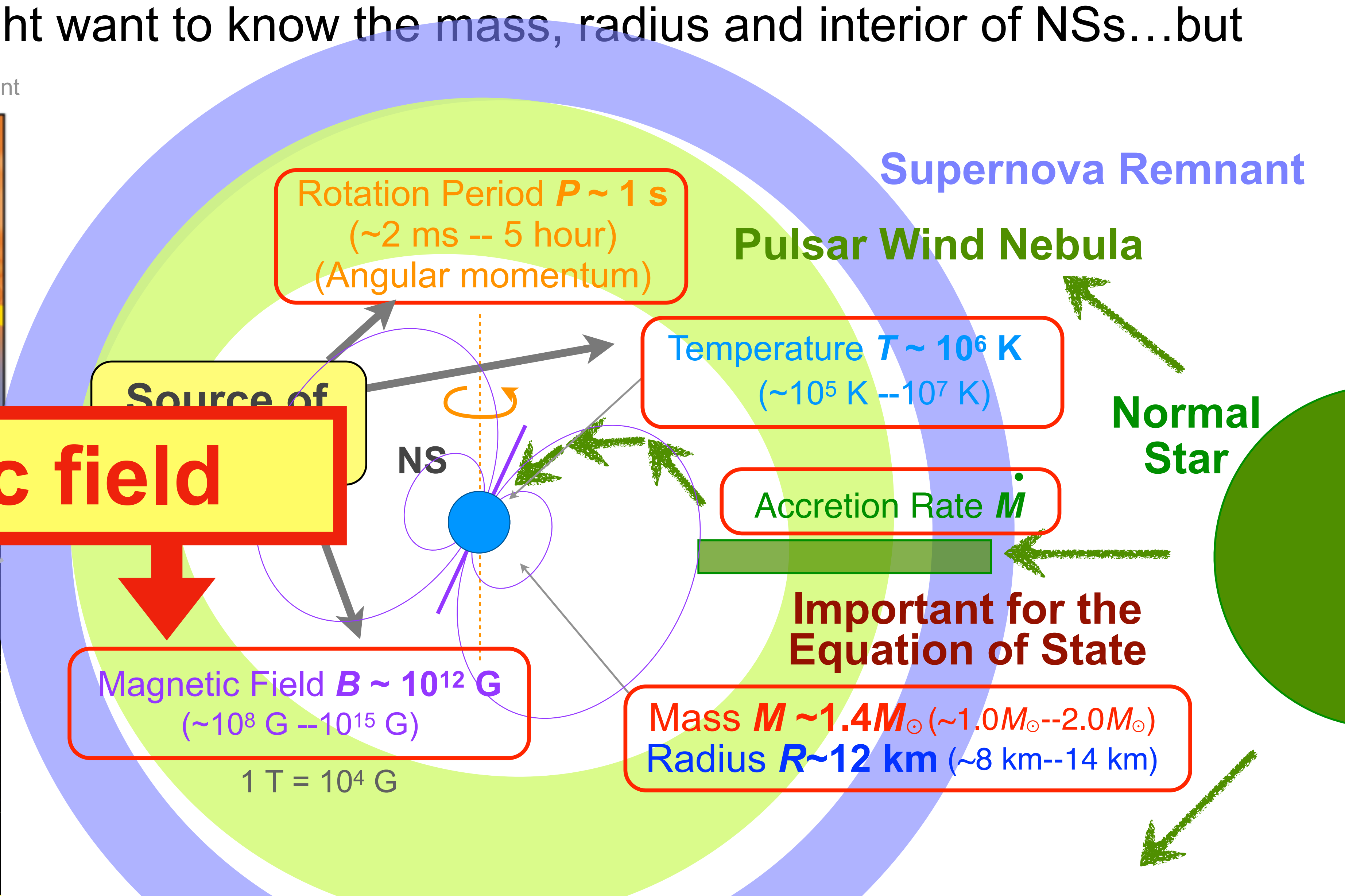
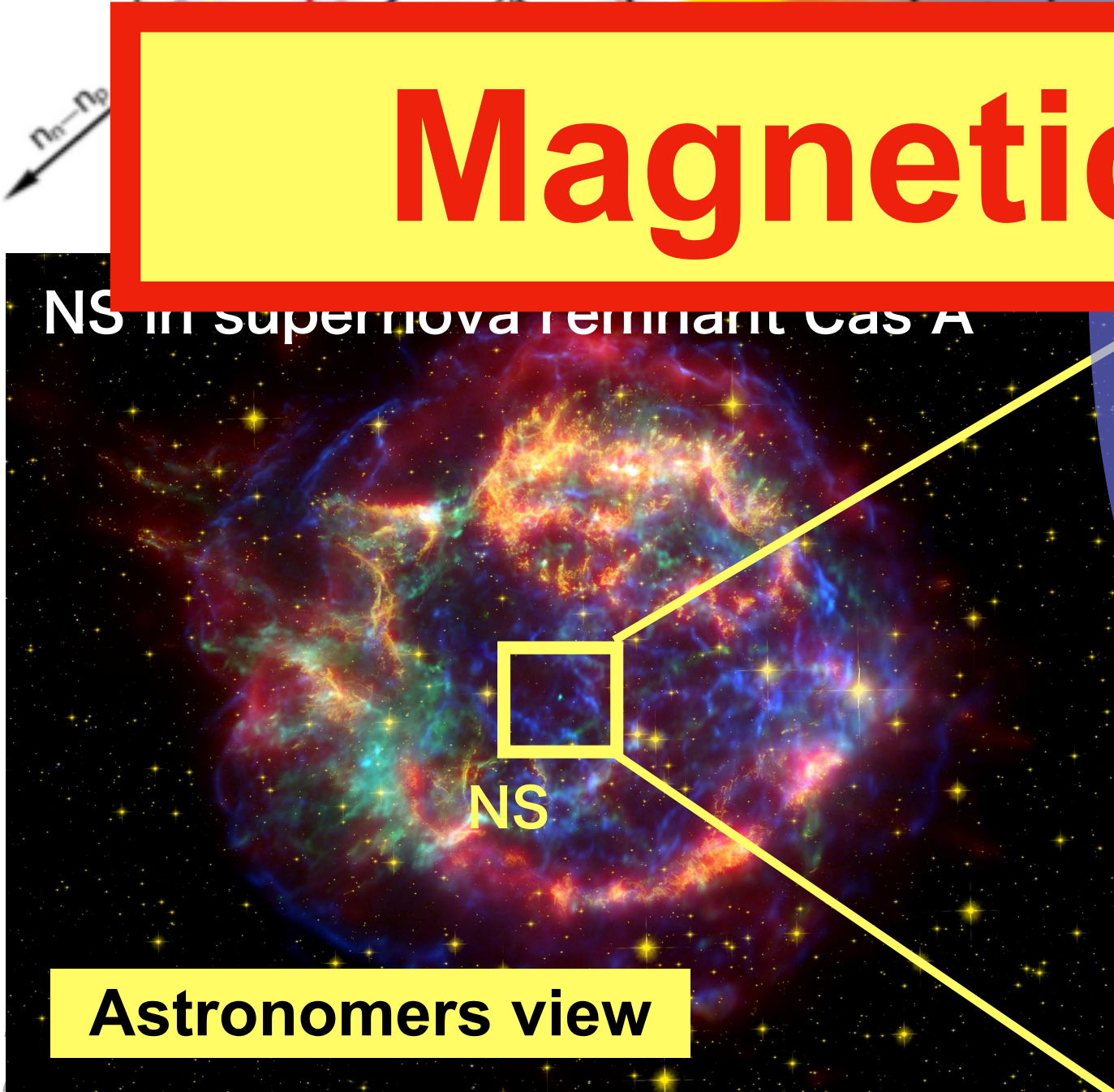
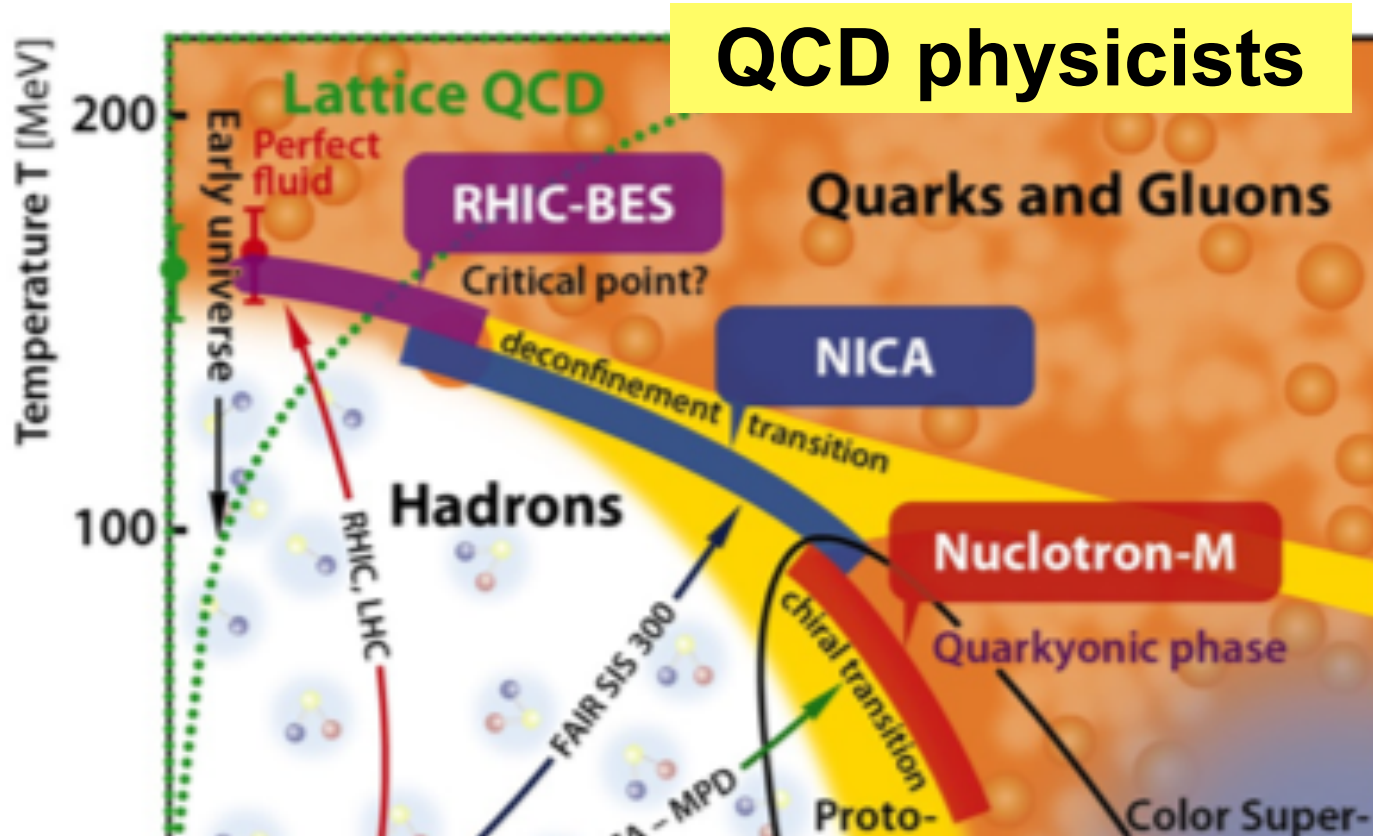
No Gravity

Brightness

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<https://www.interactions.org/blog/our-experiment>

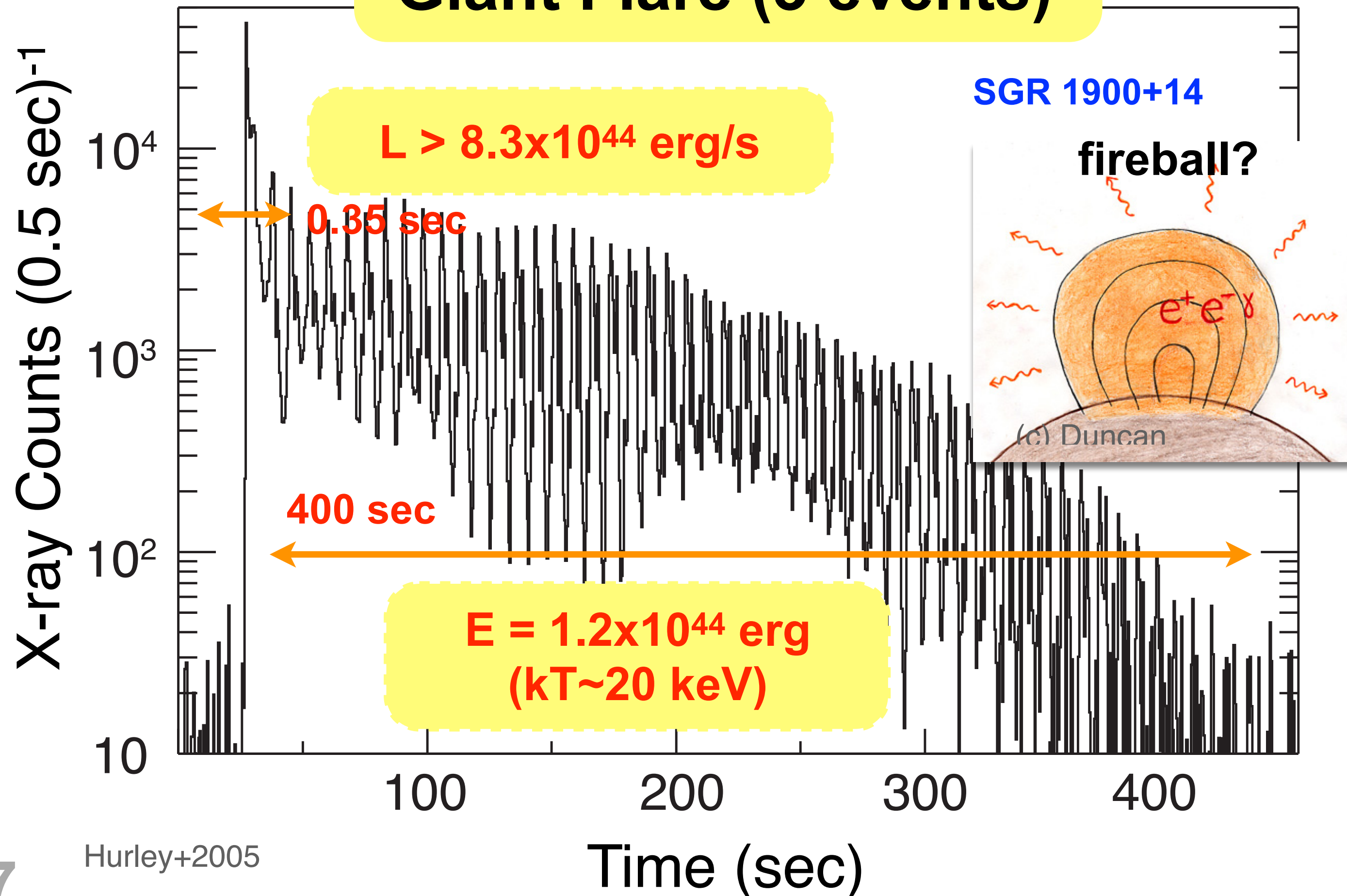


Magnetar: Soft Gamma Repeater (SGR)

Discovered by “Giant Flares” or recurrent burst activities. ~ 5 SGRs

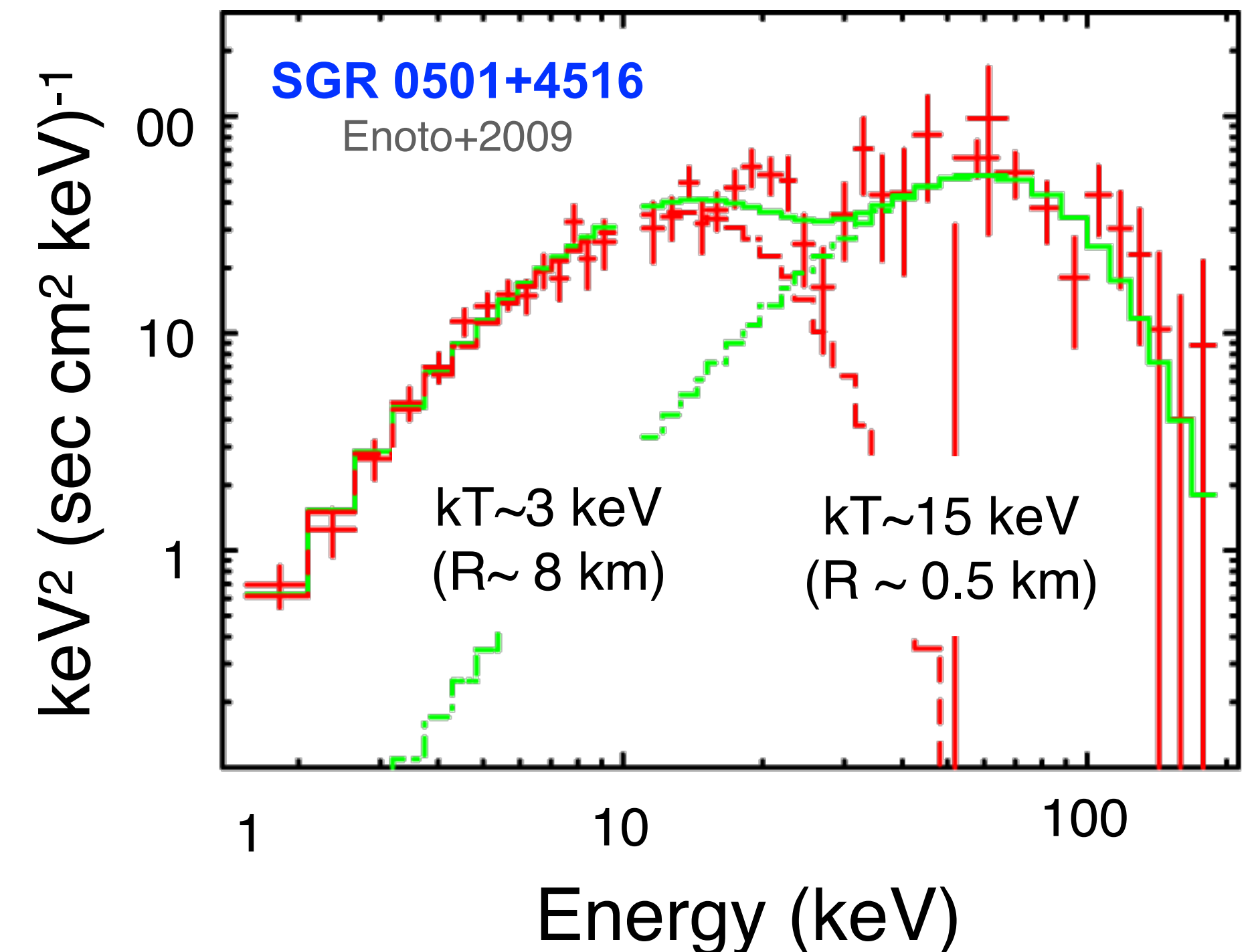
- Exceeding the Eddington Luminosity ($\sim 10^{38}$ erg/s) by ~6 orders of magnitudes
- $B > 10^{14}$ G is required to confine a few dozen keV plasma for ~400 sec

Giant Flare (3 events)



Short Bursts

a few hundred millisecond empirically two Blackbody



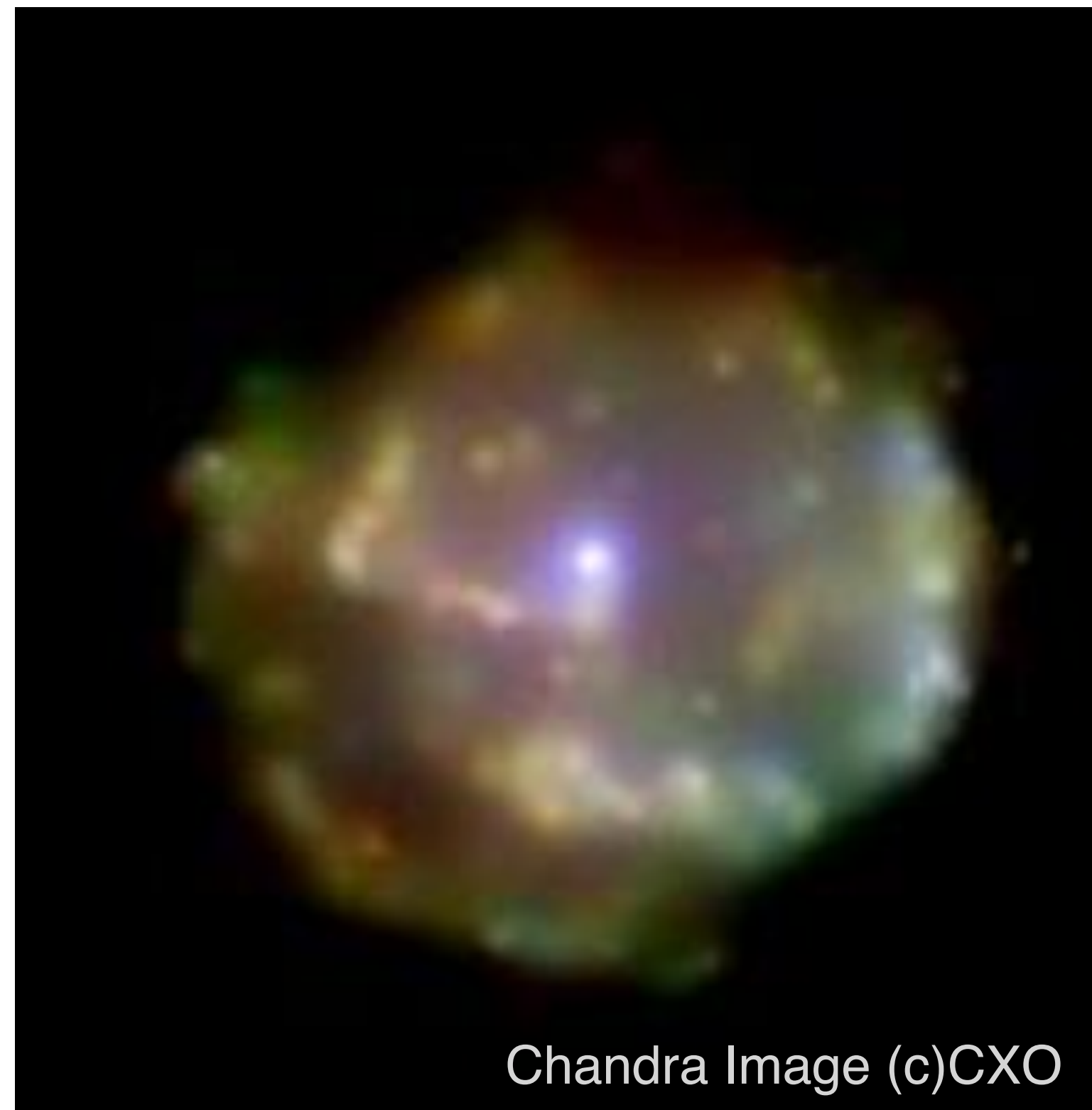
Magnetar: Anomalous X-ray Pulsar (AXP)

Discovered as pulsed bright persistent X-ray sources. ~15 AXPs

- Exceeding the spin-down luminosity by ~2 orders of magnitudes ($L_x \gg L_{sd}$)

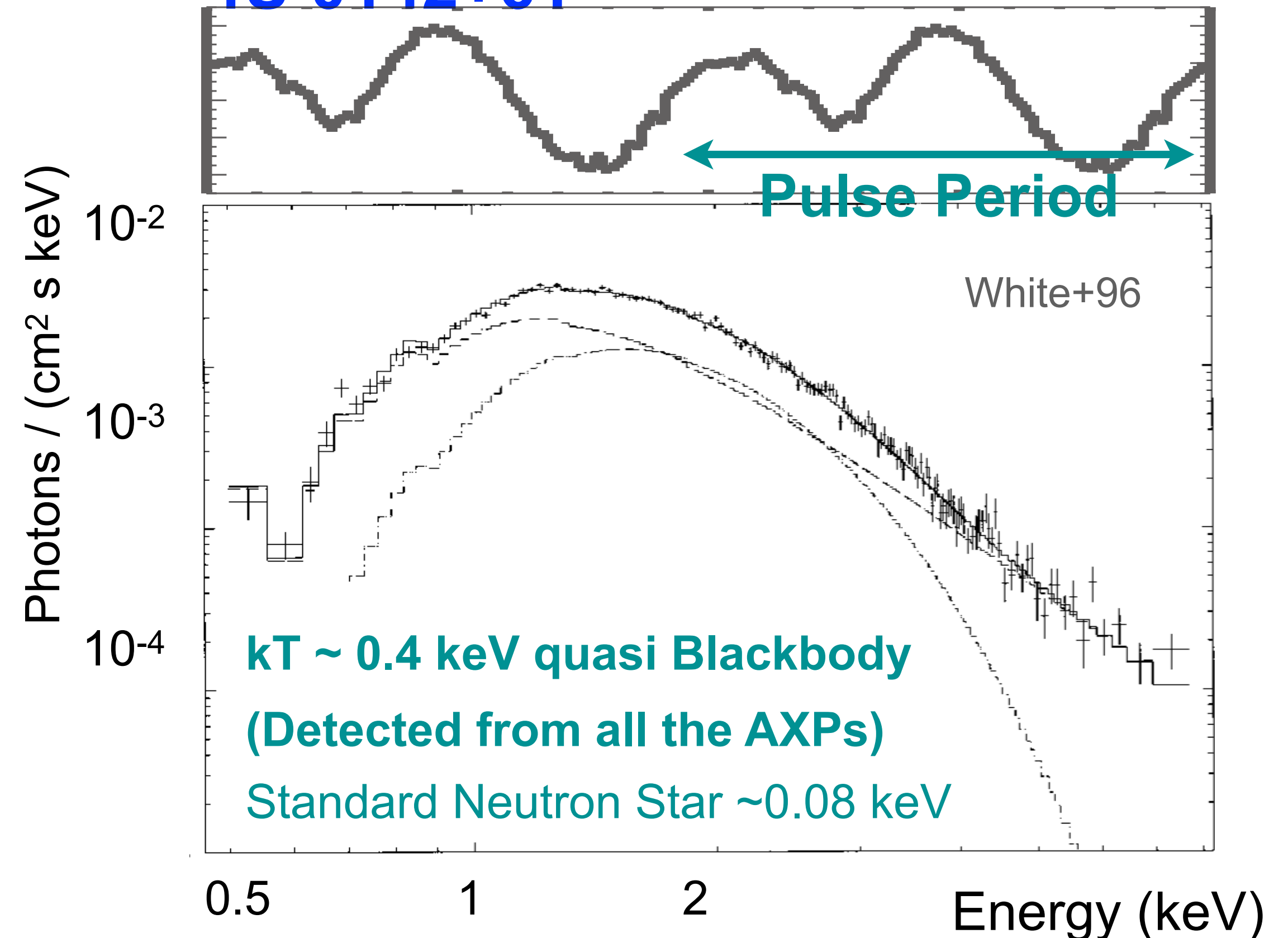
Associated with SNR

1E 1841-045 (SNR Kes73)



Persistent X-ray Emission

4U 0142+61



Magnetar hypothesis to the establishing model

“SGRs and AXP are ultra-strongly magnetized NSs with $B \sim 10^{14-15}$ G powered by their stored magnetic energy in the stellar interior.” Thompson & Duncan+95, 96

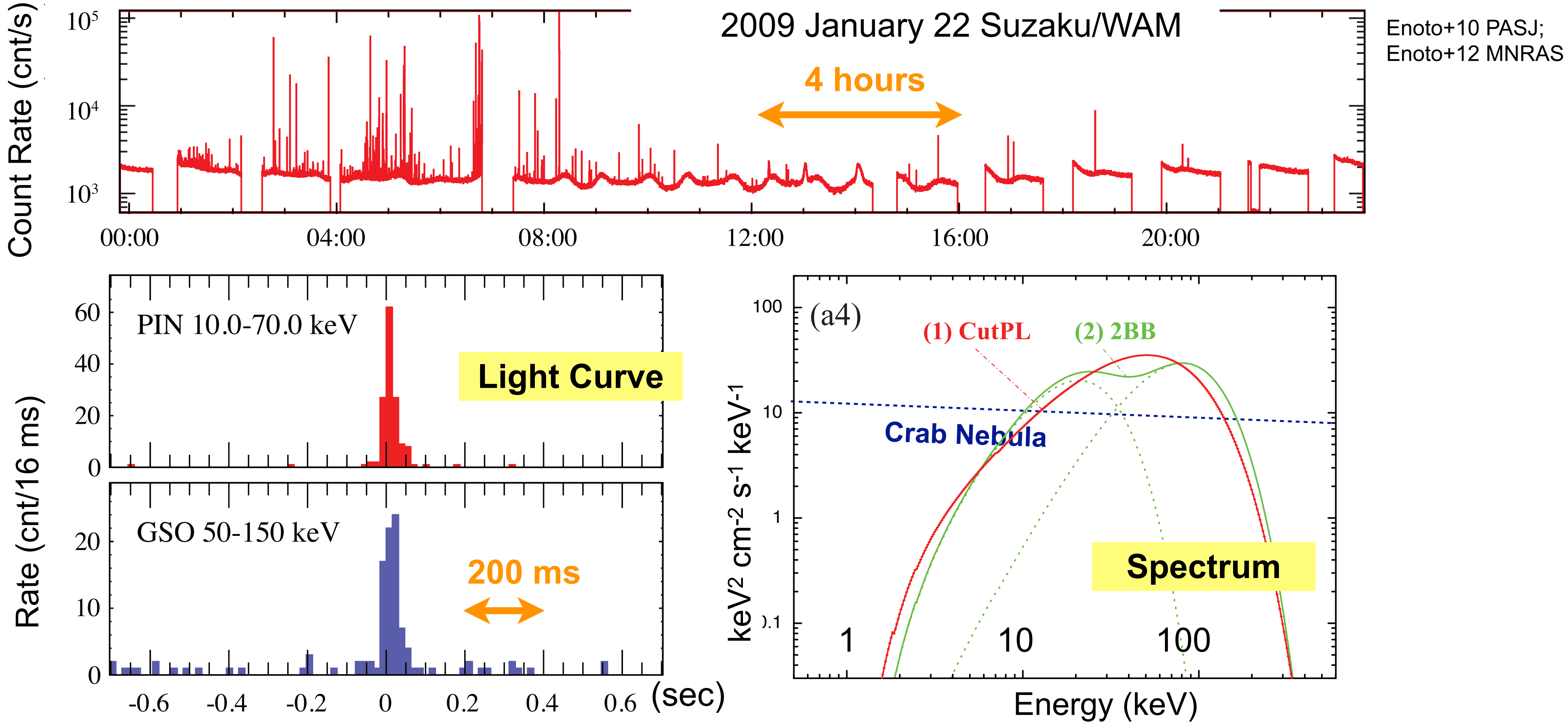
1. SNR association, slow P and large \dot{P} \Rightarrow Young ($\tau < 100$ kyr) & $B \sim 10^{14-15}$ G
2. $L_x \gg L_{sd}$ by 2-3 orders of mag. \Rightarrow Not rotation-powered pulsars
3. No evidence of binary system \Rightarrow Not accretion-powered pulsars
4. Marginal “proton” cyclotron resonance \Rightarrow Suggests $B > 10^{14}$ G
5. Peculiar burst activities \Rightarrow Magnetic dissipation (e.g., reconnections)??
6. Super-Eddington giant flares $\Rightarrow B > 10^{14}$ G & suppression of σ

QED Critical Field $\hbar \frac{eB}{m_e c} = m_e c^2 \Rightarrow B_{\text{QED}} = 4.4 \times 10^{13}$ G

Suppression of σ **Distortion of atom** **Photon Splitting** **Birefringence**

Magnetar outburst (example 1E 1547.0-5408)

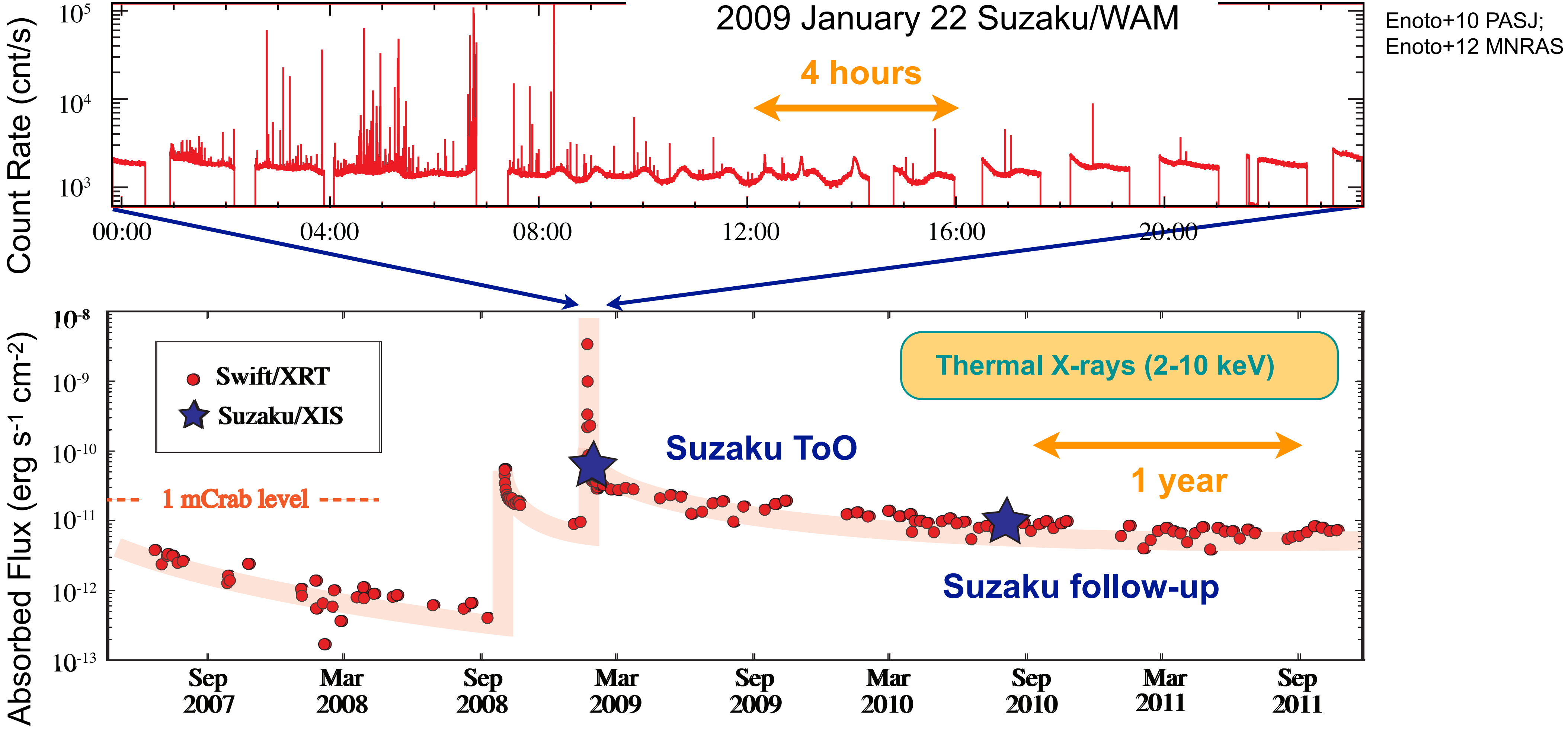
Known as a fast rotation faint AXP (P~2 sec)



Feature 1: Recurrent Bright “Short Burst”
 Duration ~100-500 ms, (Empirically) Two blackbody spectrum (kT ~ 4, 11 keV)

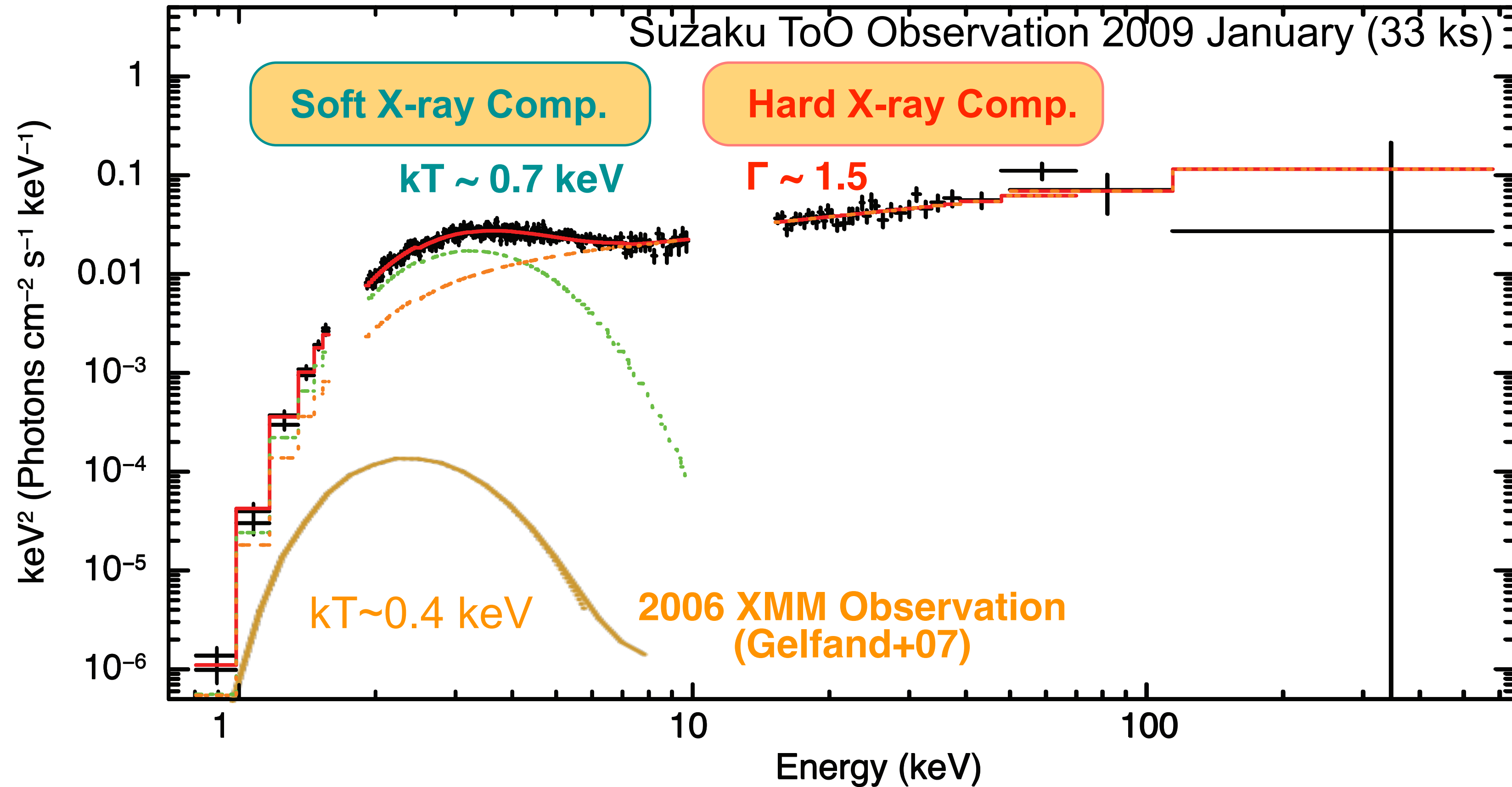
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Known as a fast rotation faint AXP ($P \sim 2$ sec)



Feature2: Persistent X-ray becomes brighter by 2-3 orders of magnitude. ("Outburst")

Magnetar outburst (example 1E 1547.0-5408)



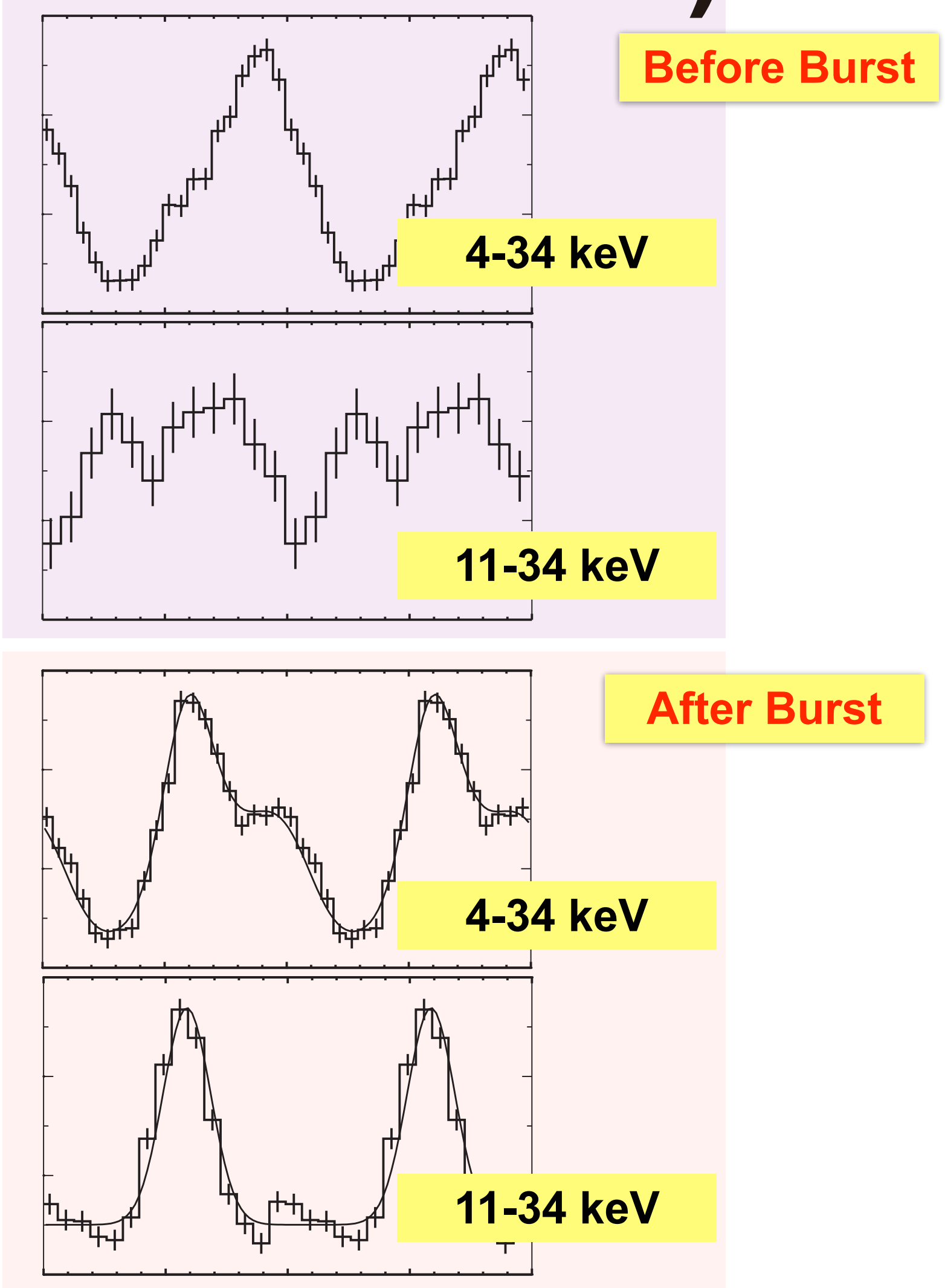
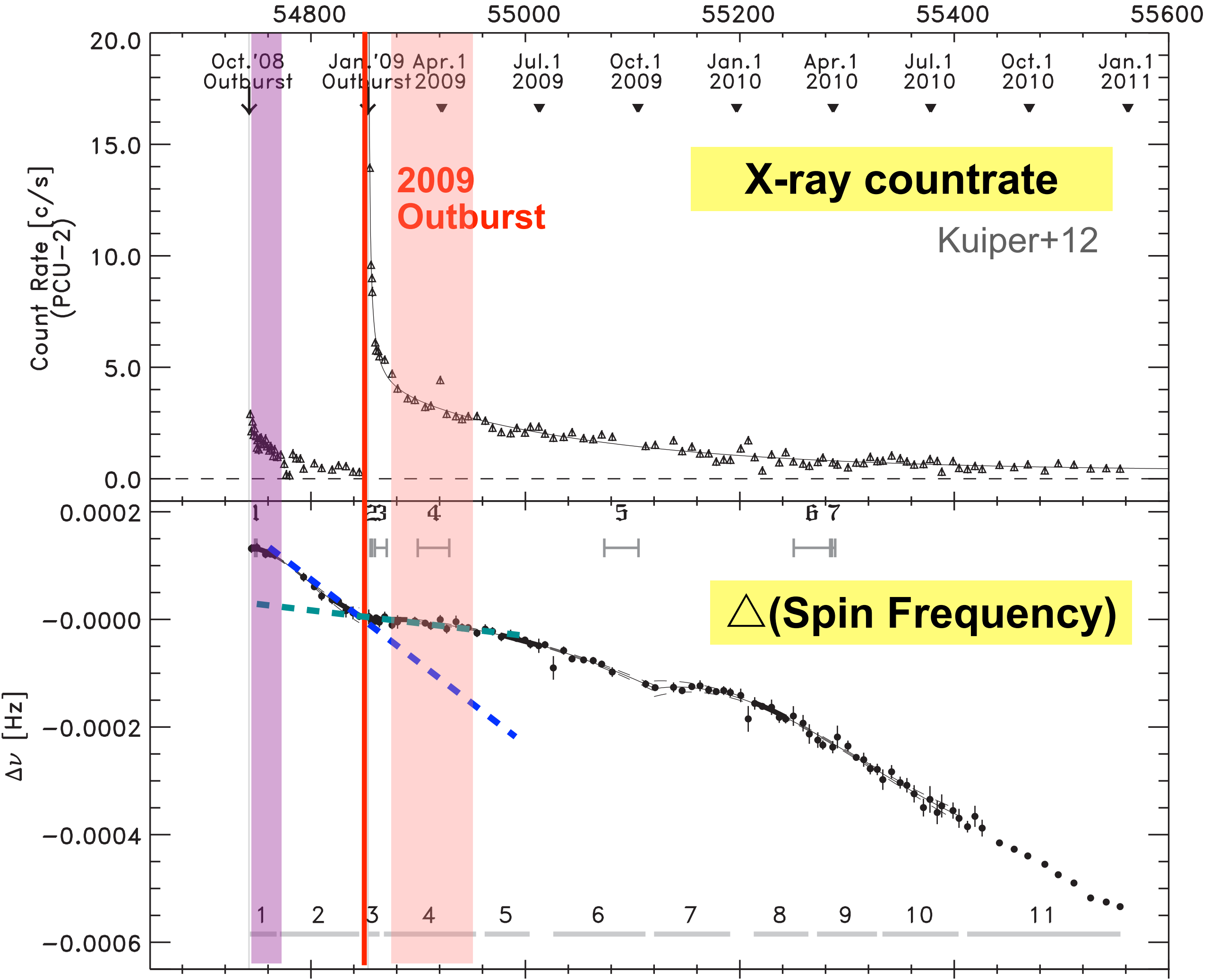
Enoto+10 PASJ;
Enoto+12 MNRAS

New hard X-ray components have been discovered from persistently bright famous magnetars (Kuiper et al., 2006) and some transients (Enoto et al., 2010).

Feature3: Two spectral components: distinctive soft and hard X-rays

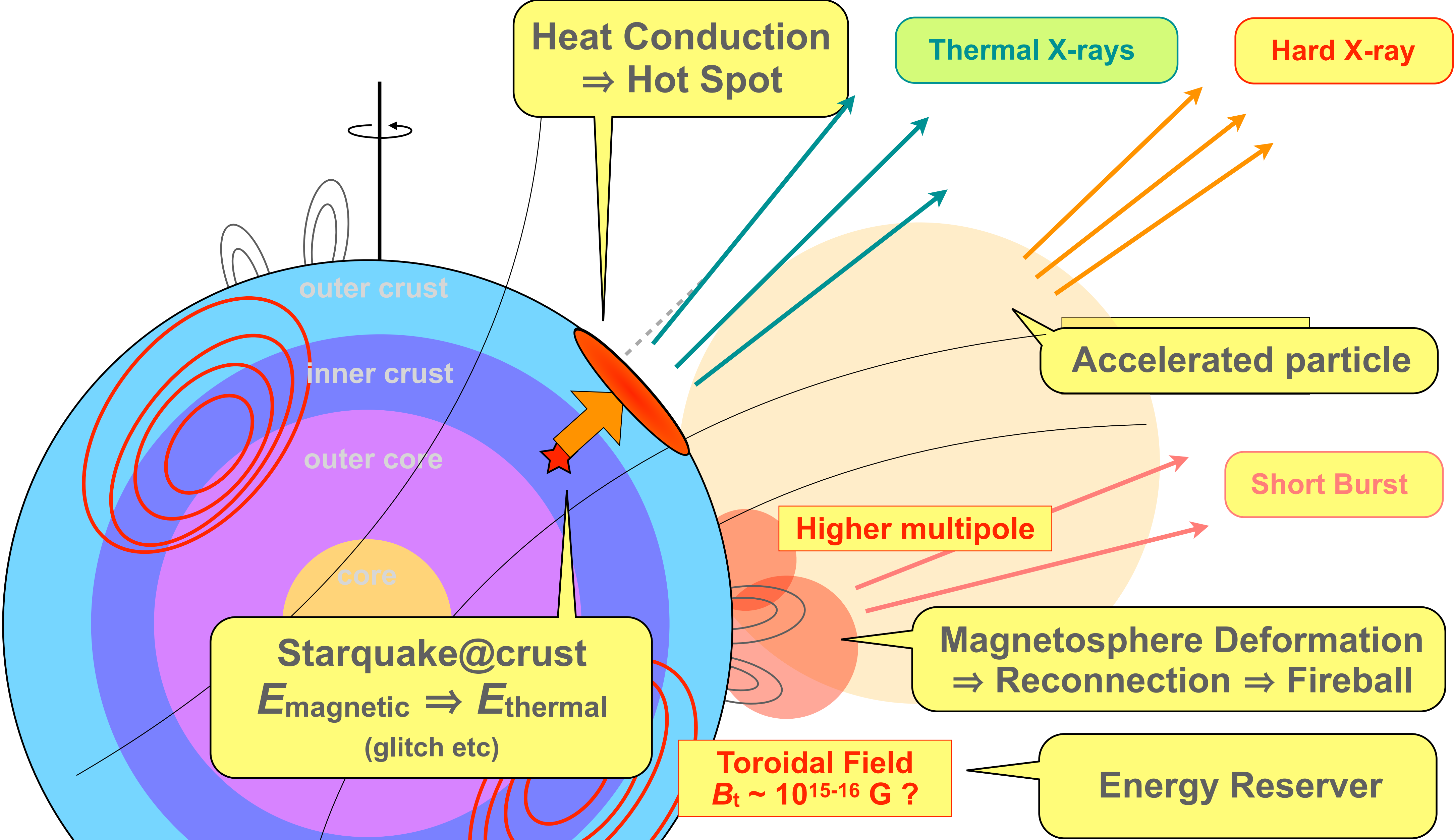
Both becomes brighter during the outburst

Magnetar outburst (example 1E 1547.0-5408)

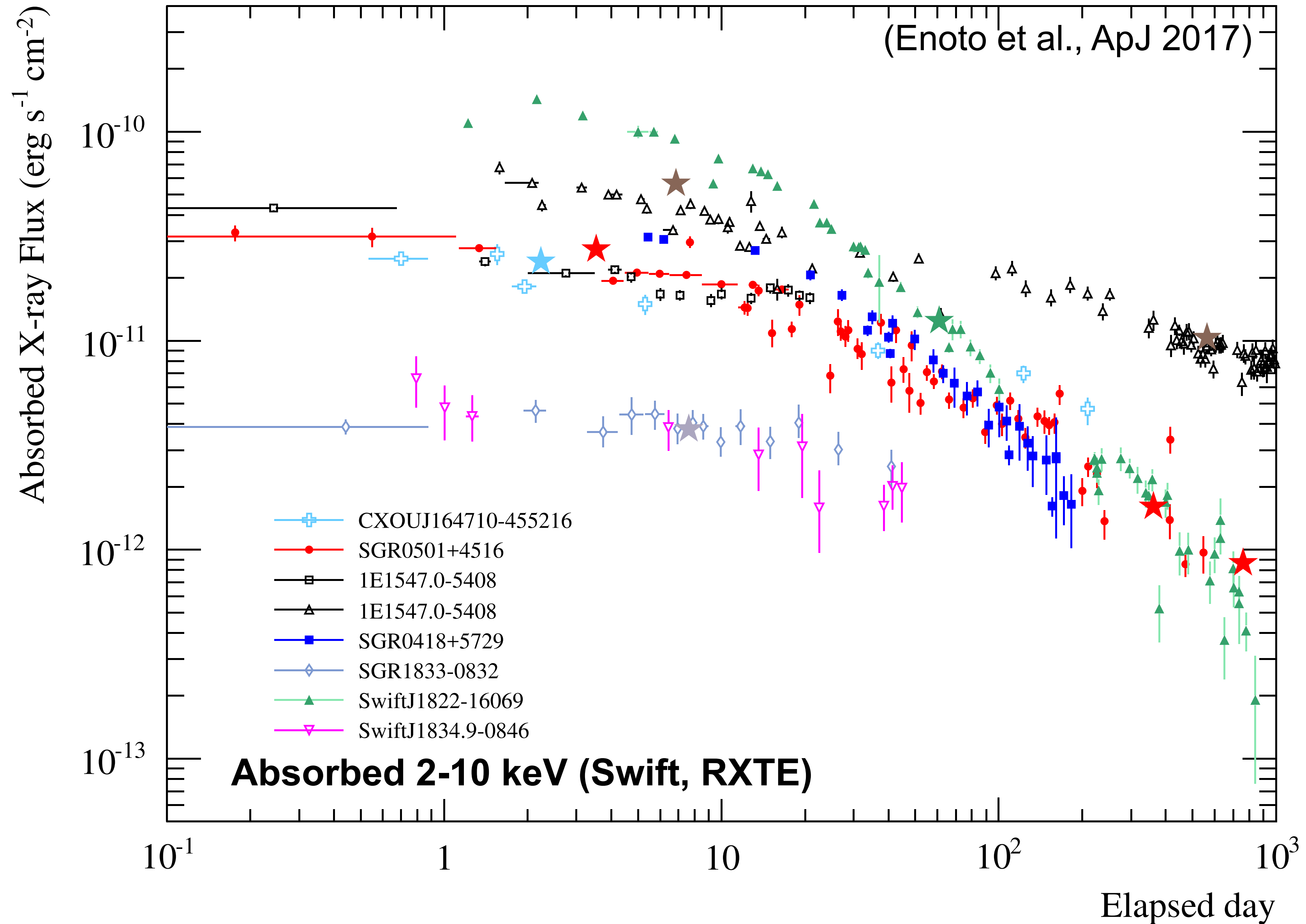


A frequency derivative jump at the outburst ($\Delta\dot{\nu}/\nu = -0.69 \pm 0.07$)
 Pulse profile change around the onset of the burst \Rightarrow Hot spot?

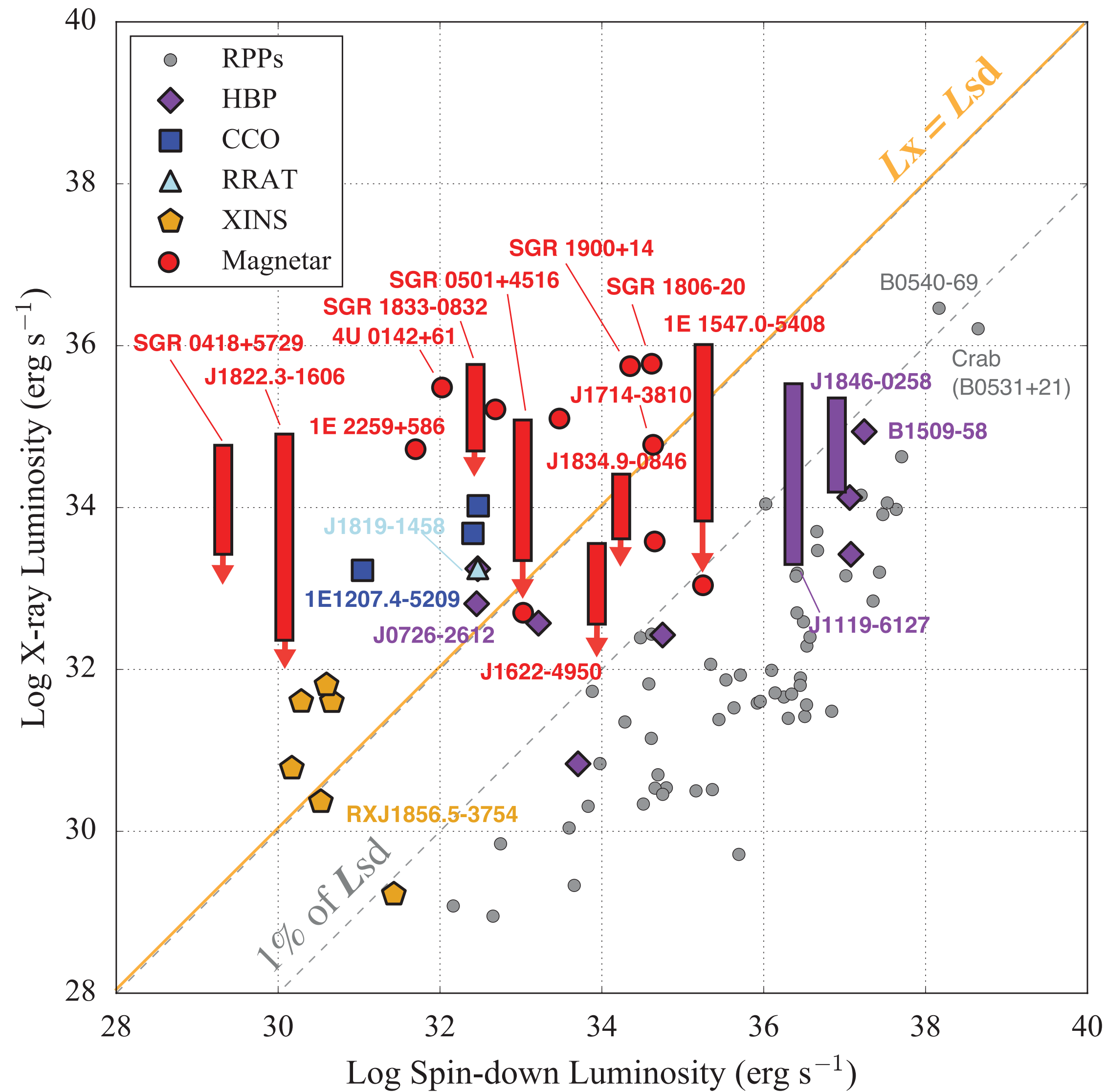
Magnetar energy release and emission



X-ray flux decay of outbursts of transient magnetars



Spin-down luminosity L_{sd} vs. X-ray luminosity L_x



- Spin-down luminosity

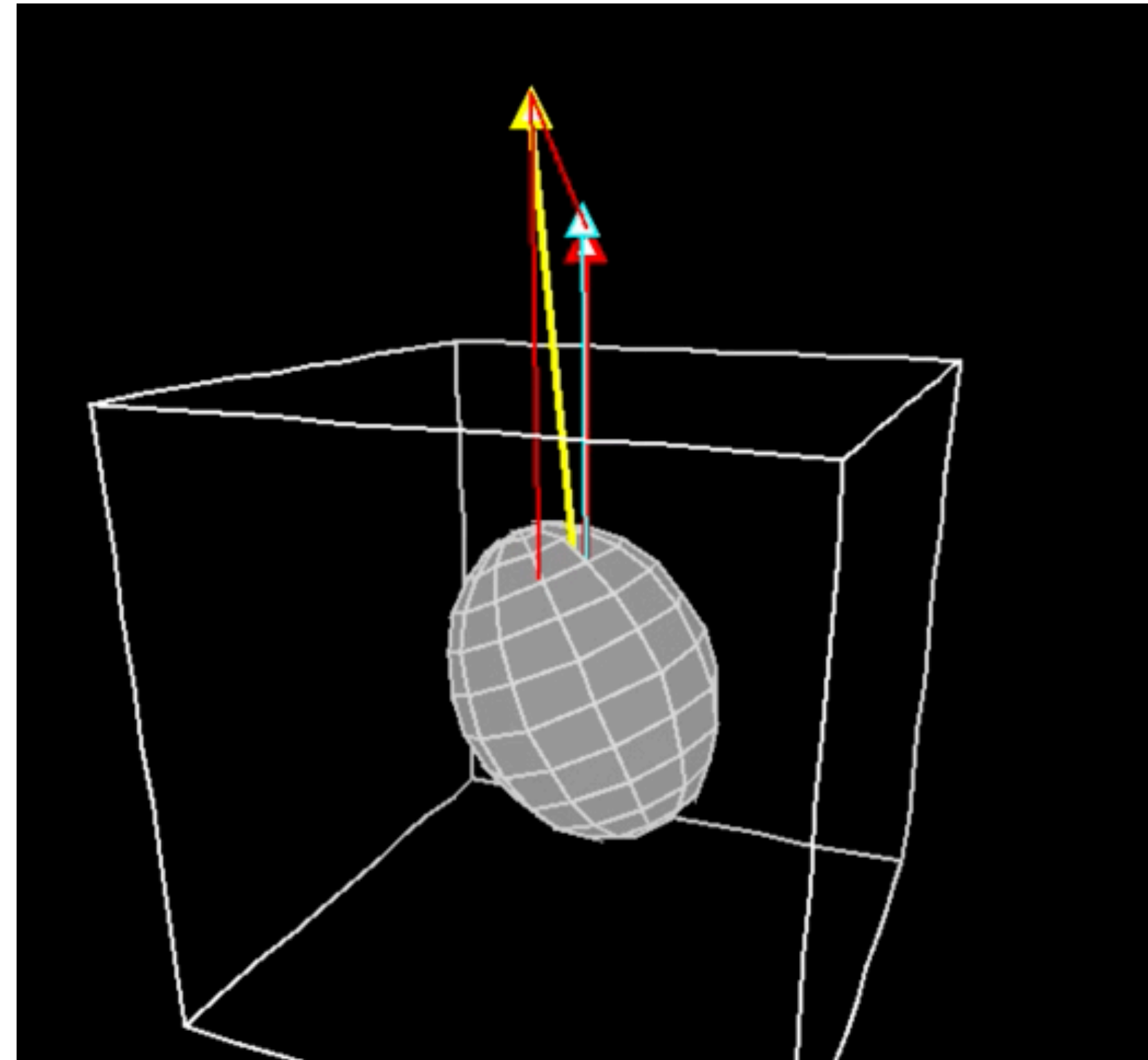
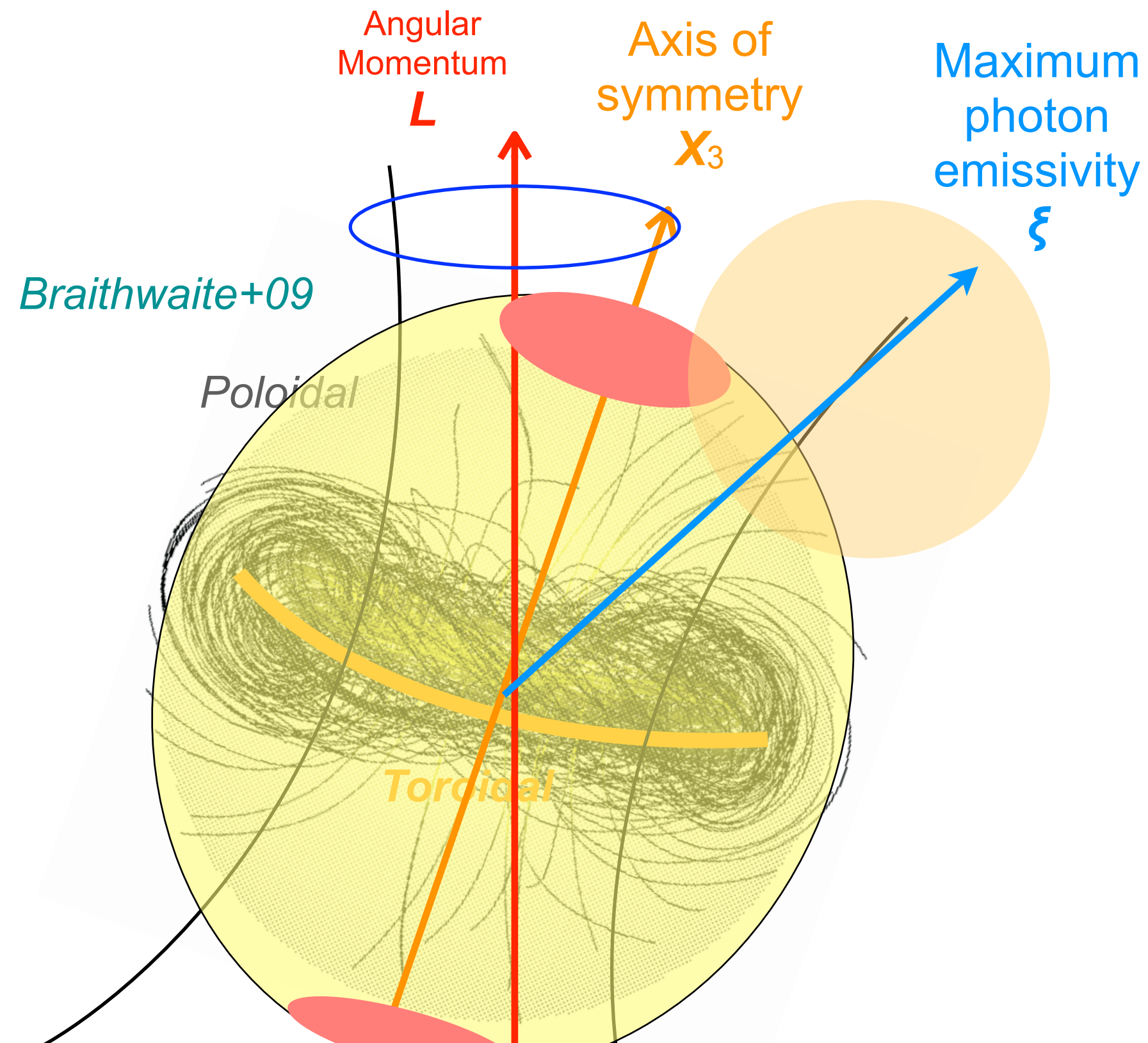
$$L_{sd} \propto \dot{P}/P^3$$

- Rotation powered pulsars: $L_x < L_{sd}$
 - c.f., Eddington luminosity $\sim 10^{38}$ erg/s
- Persistent magnetars: $L_x > \sim L_{sd}$
- Transient magnetars: $L_x \rightarrow < L_{sd}$
- Possibility that many neutron stars can exhibit magnetar-like outbursts?

Toroidal magnetic field induced NS precession?

Huge energy reserver is needed inside the magnetars

⇒ **Strong toroidal Field inside NSs?** (can not be measured by $P\text{-}P_{\text{dot}}$)



Toroidal B-field ⇒ Prolate shape

$$\epsilon = \frac{\Delta I}{I} \sim 10^{-4} \left(\frac{B_t}{10^{16} \text{ G}} \right)^2$$

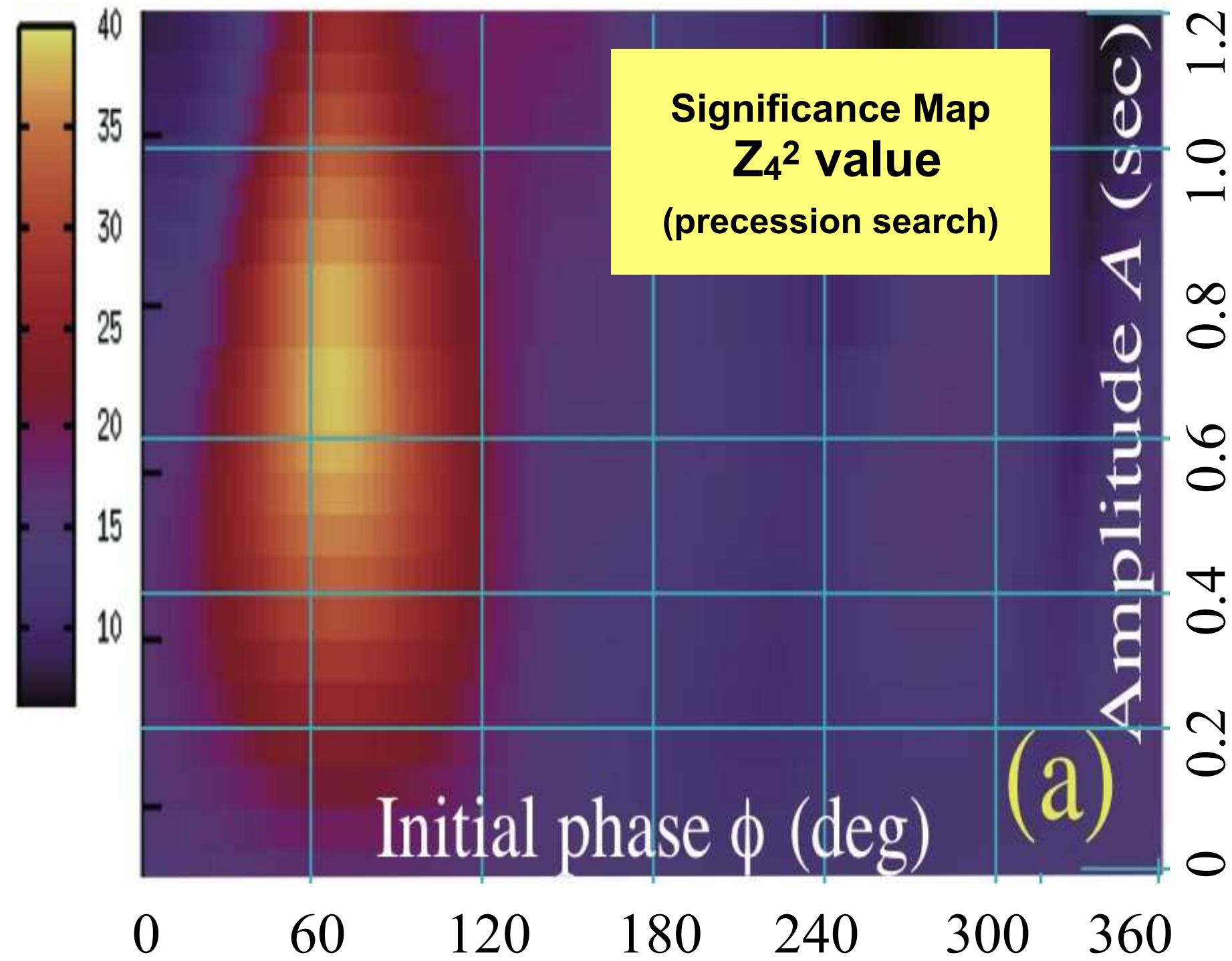
$X_3 \neq \xi$

$$Q = \frac{P_{\text{spin}}}{\epsilon}$$

(see., e.g., Landau & Lifshitz textbook)

Evidence for NS precession?

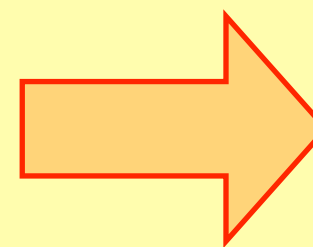
Prototypical AXP 4U 0142+61 ($P=8.69$ s, Poloidal field $B_d \sim 1.3 \times 10^{14}$ G)



Hard X-ray shows a sinusoidal, $T=1.5$ hour, phase modulation (amplitude 0.7 s)

Makishima, TE et al., PRL, 2014

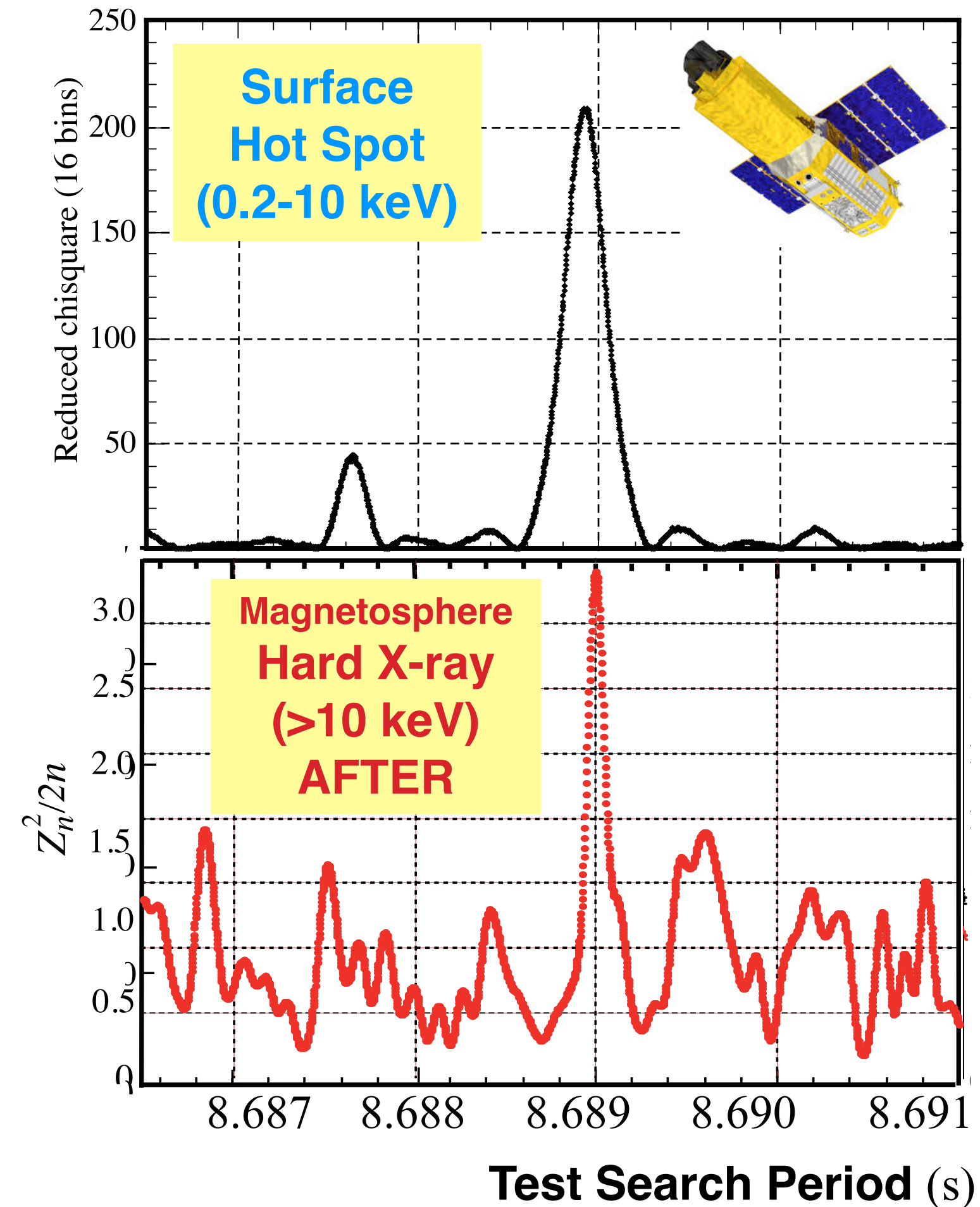
$$\epsilon \sim \frac{8.69 \text{ s}}{1.5 \text{ h}} \sim 1.6 \times 10^{-4}$$



Toroidal B -field $B_t \sim 10^{16}$ G

$$\epsilon \sim 10^{-4} (B/10^{16} \text{ G})^2$$

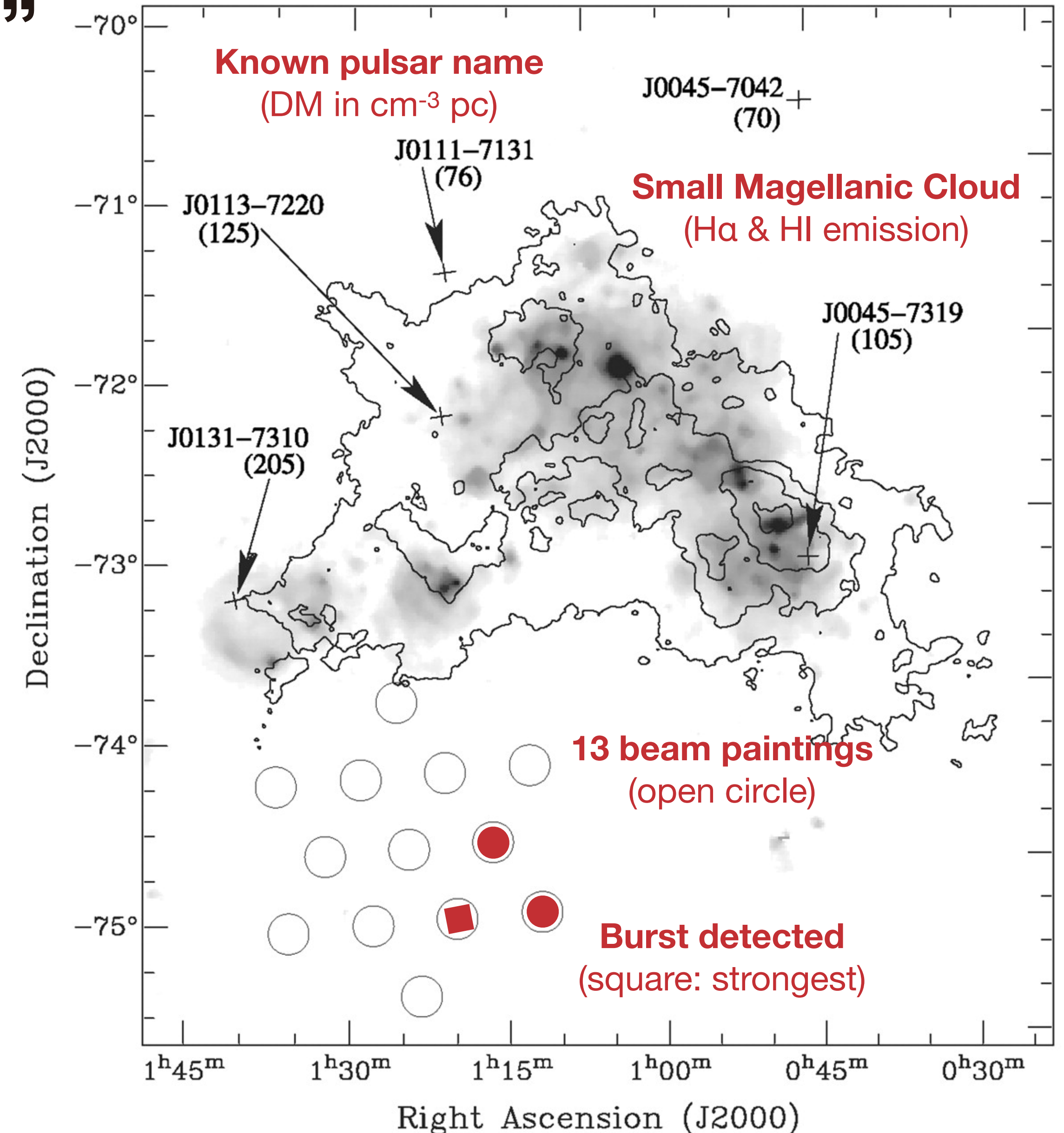
Significance of Pulsation



Confirmation with NuSTAR (Makishima+2019), Similar signature was detected from 1E 1547.0-5408 (Makishima+2020)

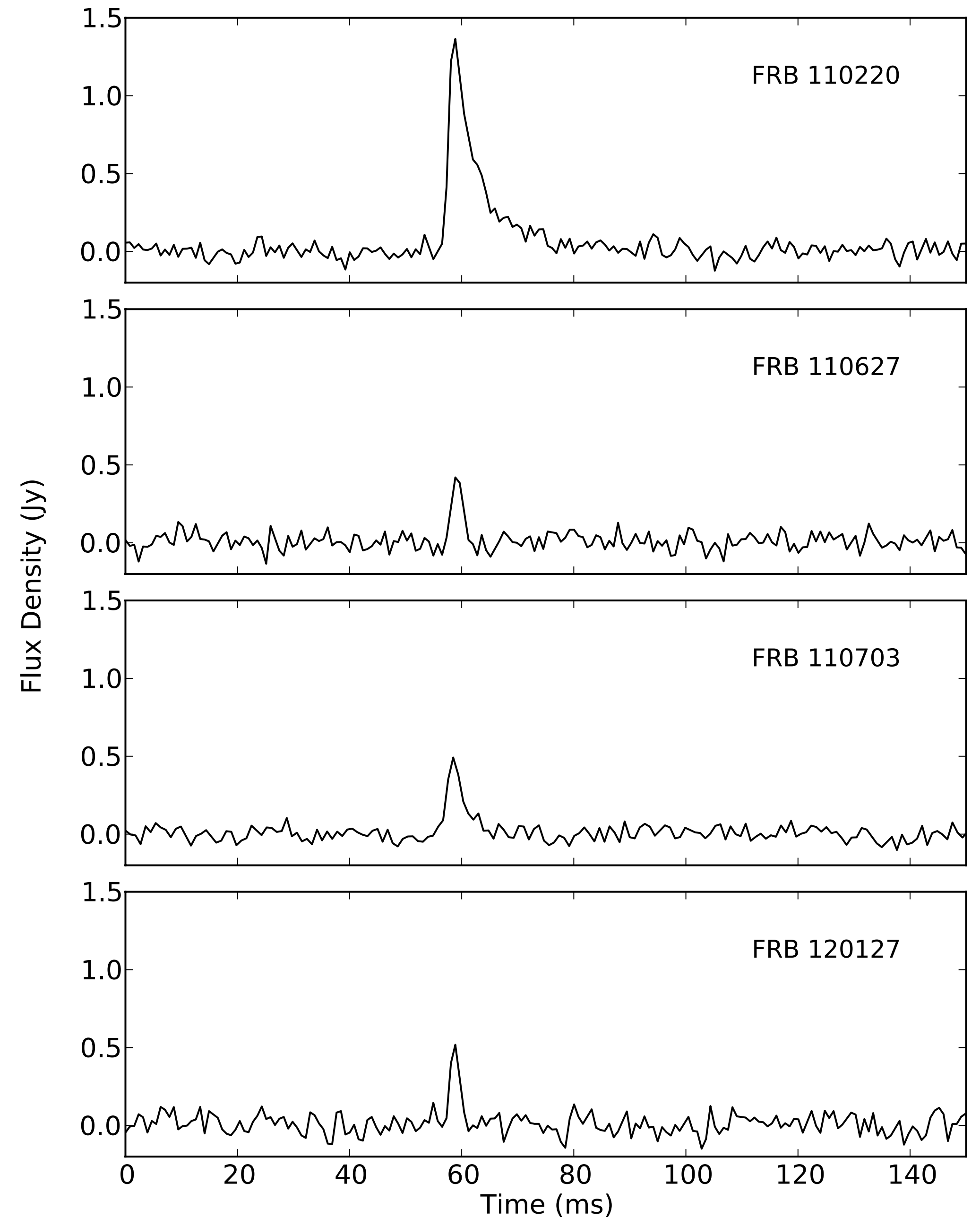
Mysterious “Lorimer burst”

- Motivated by transient pulse of pulsars
- Archival data of 1.4 GHz survey of the Magellanic Cloud using the 64-m Parkes Radio Telescope in Australia
- Mysterious burst on 24 August, 2001
 - Located 3 degree from the SMC
 - Single event, not recursive
 - Bright 30 Jy ($1 \text{ Jy} = 10^{-26} \text{ W m}^{-2} \text{ Hz}^{-1}$)
 - Short duration $< 5 \text{ msec}$
 - $\text{DM} = 375 \text{ cm}^{-3} \text{ pc}$ (distant? $< \sim 1 \text{ Gpc}$)



Fast radio bursts (FRBs)

- Four FRBs were further reported in 2013.
- Short duration: ~a few ms or less
- Fluence $S = 0.6\text{-}8.0$ Jy ms @ 1.3 GHz
- High Galactic latitude $|b| > 41$ deg
- $R_{\text{FRB}} \sim 10^{-3}$ / galaxy / year
 - $R_{\text{GRB}} \sim 10^{-6}$ / galaxy / year
 - $R_{\text{CCSN}} \sim 10^{-2}$ / galaxy / year
- DM = 553-1103 cm^{-3} pc
 - Cosmological distance: $z = 0.45\text{-}0.81$



Dispersion Measure (DM)

$$DM = \int_0^d n_e dl \quad (\text{cm}^{-3} \text{ pc})$$

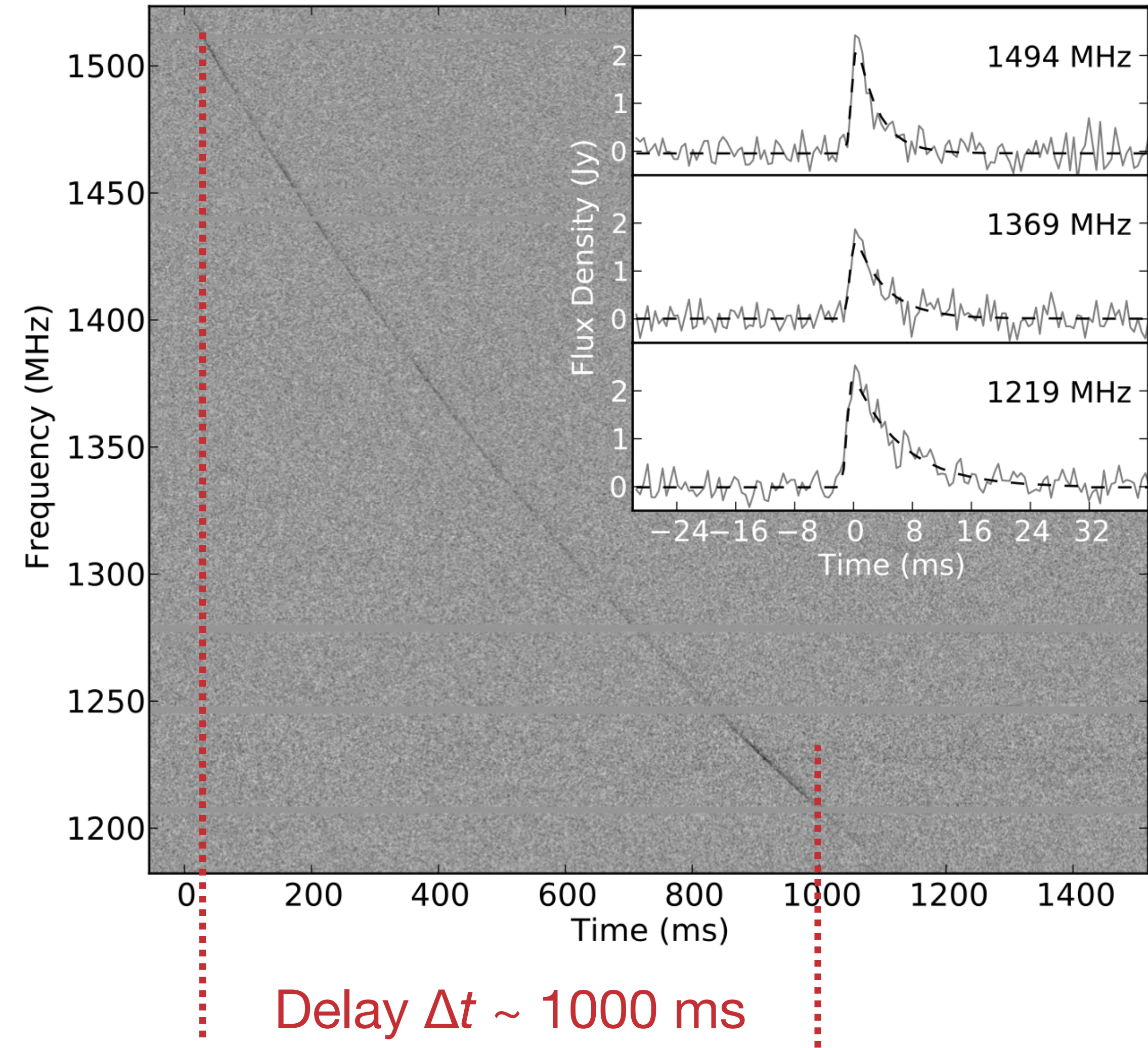
- Integrated column density (n_e) of free electrons along the line of sight
- This makes a frequency-dependent dispersive delay Δt through a plasma

$$\Delta t = \frac{e^2}{2\pi m_e c} \frac{DM}{\nu^2}$$

$$= 4.14 \times 10^3 \text{ sec} \left(\frac{DM}{\text{cm}^{-3} \text{ pc}} \right) \left(\frac{\nu}{1 \text{ MHz}} \right)^{-2}$$

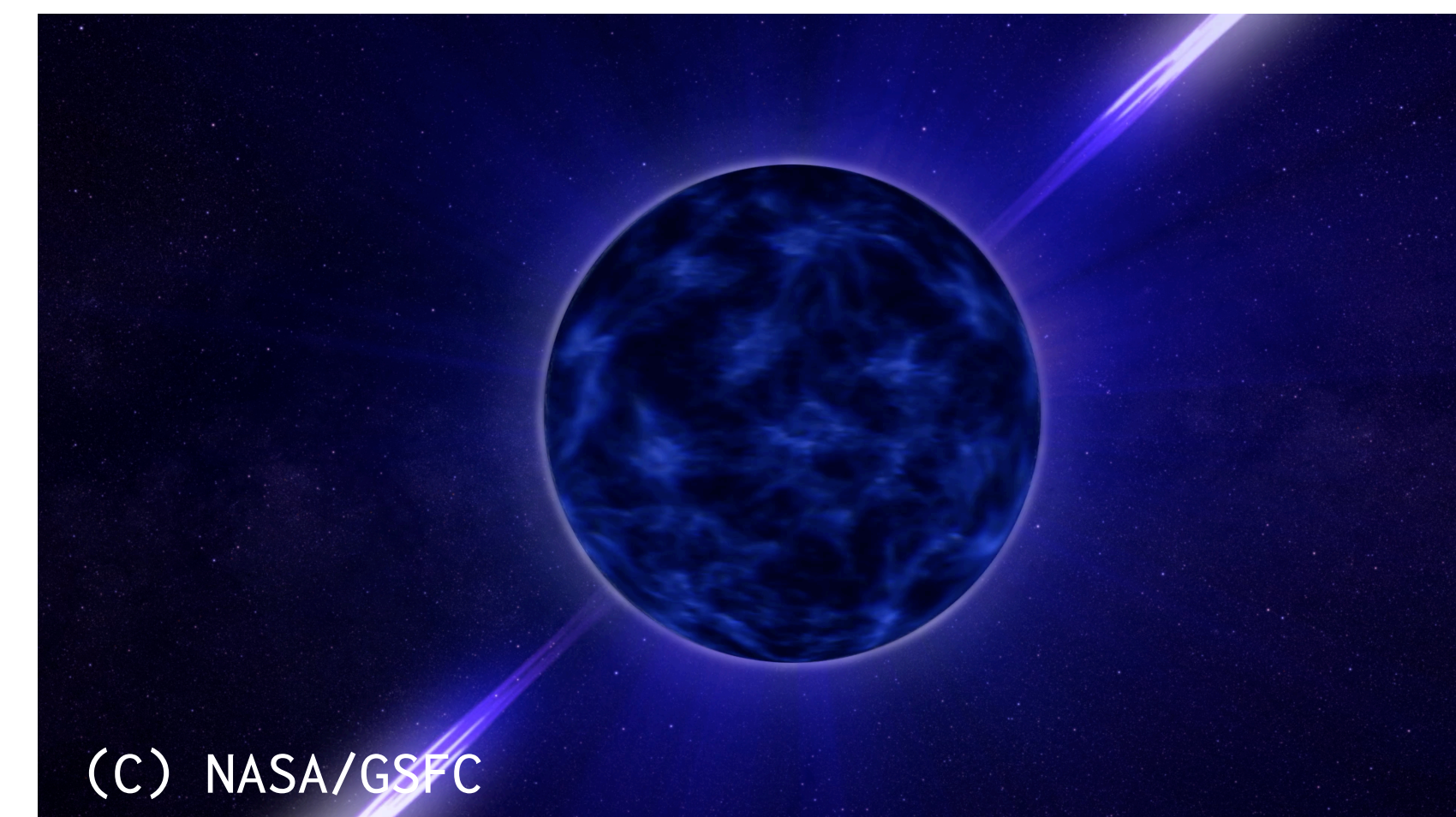
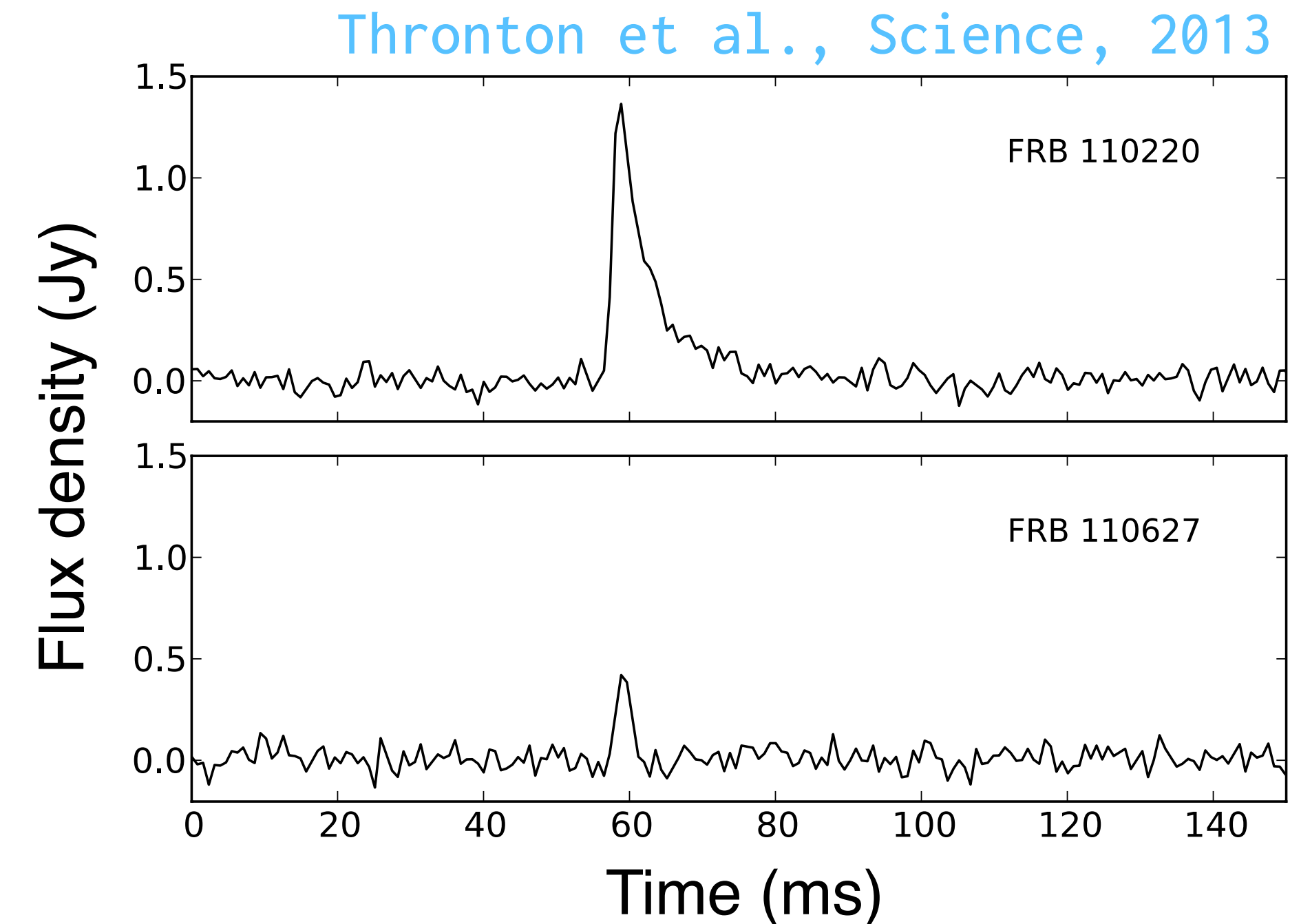
- DM (delay) is a good indicator of a source distance!

Thronton et al., Science, 2013



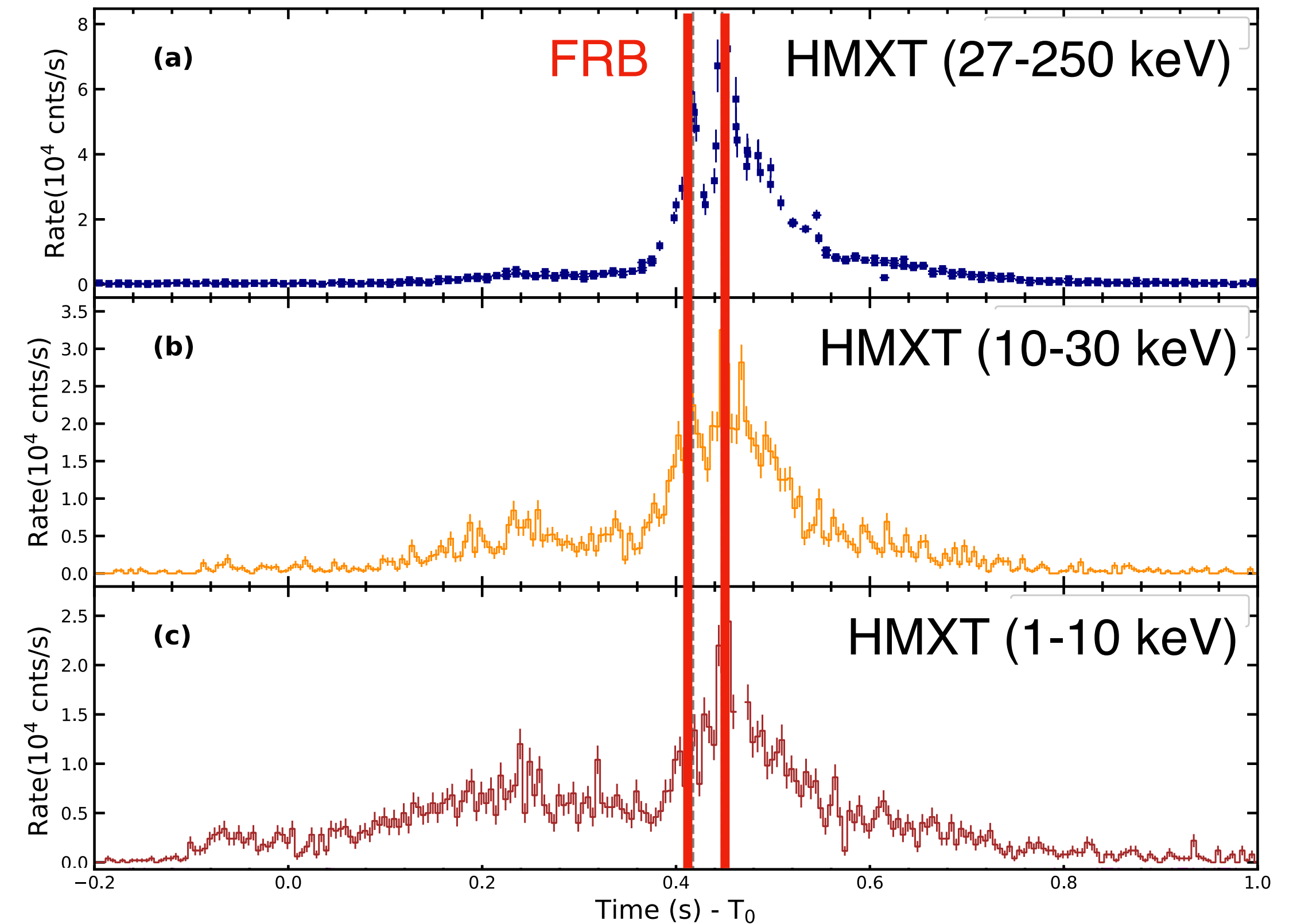
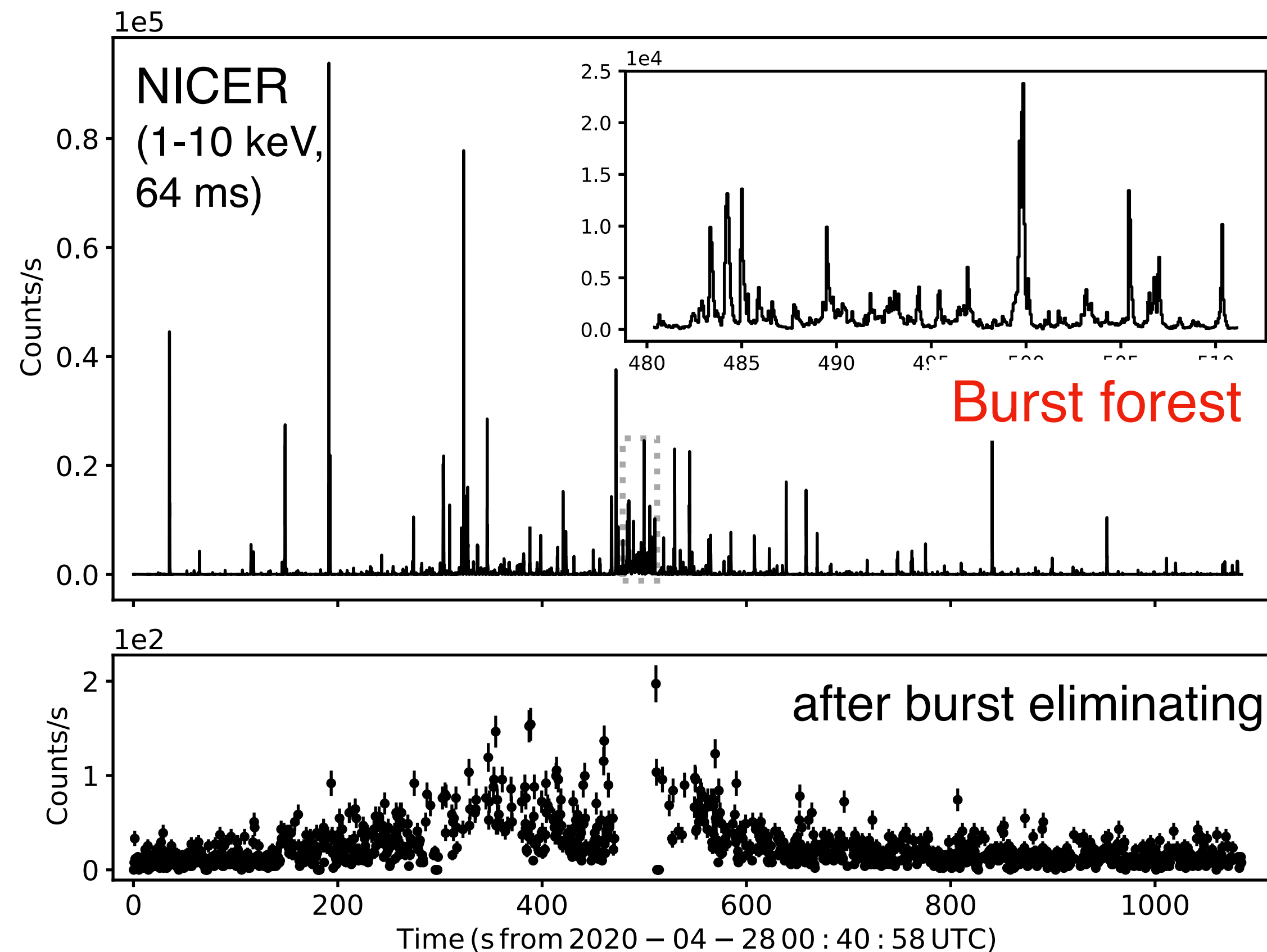
Unsolved origin(s) & emission mechanism of FRB

- Fast radio burst (FRB) characteristics:
 1. Bright radio emission $F \sim 0.2\text{-}120$ Jy @ ~ 1 GHz
 2. Large DM $\sim 300\text{-}1600$ cm⁻³ pc
→ Cosmological distance ($z < \sim 1$)
 3. Brightness temperature $T_b = 10^{33\text{-}37}$ K
→ Coherent radio emission
 4. Short duration $\Delta t < 1$ ms
→ Compact origin? ($R \sim c\Delta t \sim 3 \times 10^2$ km $\sim 30R_{\text{NS}}$)
 5. Fluence $S = F \Delta t = 1\text{-}10$ Jy ms
→ Energetics $E \sim 4 \times 10^{39}$ erg ($d / 1$ Gpc)²
 6. High event rate $R_{\text{FRB}} \sim 10^4$ / sky / day
→ $R_{\text{FRB}} \sim 0.1 R_{\text{SN}} \sim 10^4 R_{\text{GRB}}$ (Common star?)
- Neutron star (NS) related phenomena as the promising candidate of FRBs?



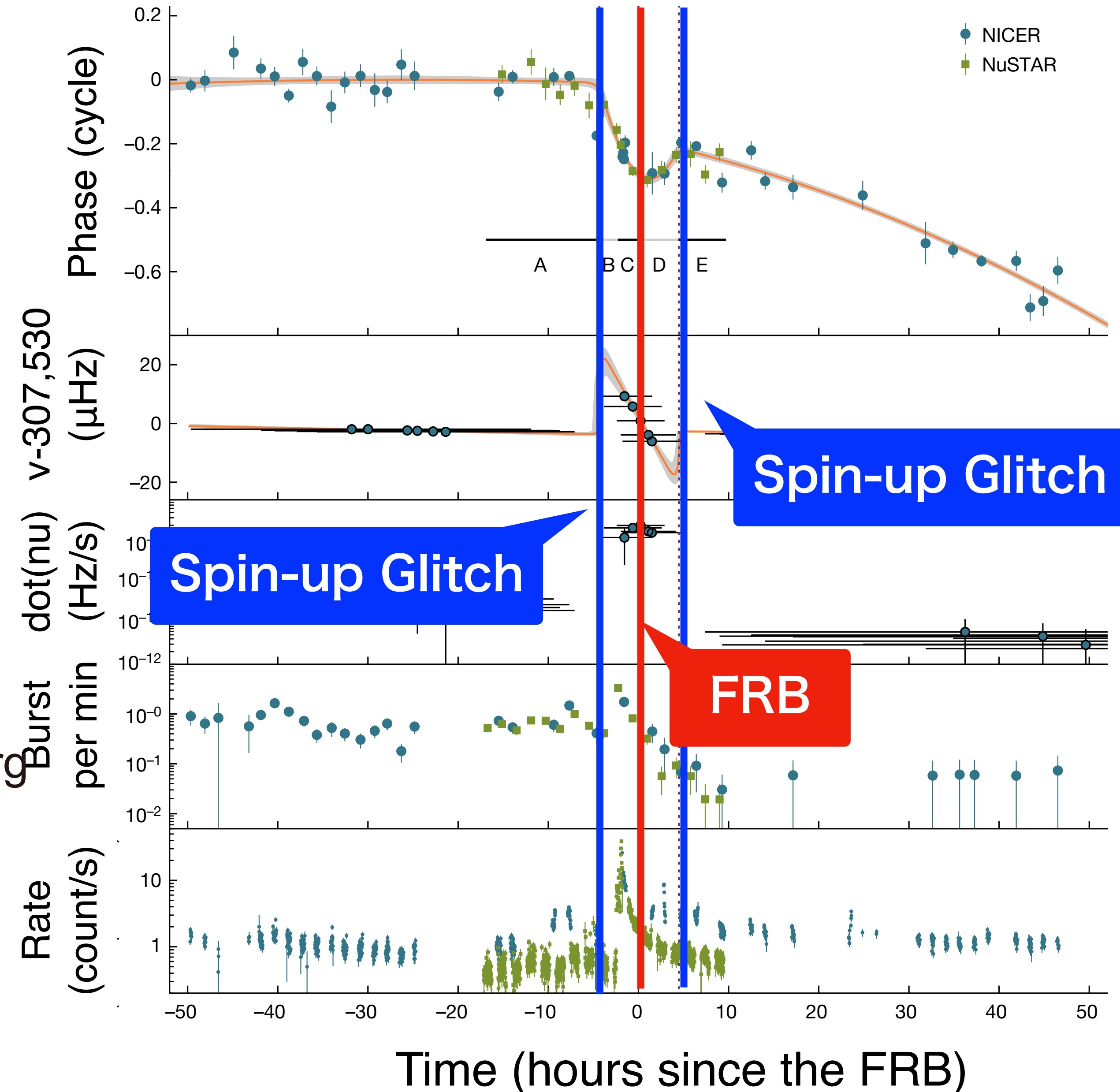
Galactic magnetar SGR 1935+2154 w/ a faint FRB

- SGR 1935+2154 (~ 9 kpc?) — $P=3.24$ s, $P_{\text{dot}}=1.43\text{e-}11$ s/s $\rightarrow B \sim 2.2\text{e+}14$ G
- A burst detected with Swift/BAT on April 27, 2020. Magnetar outburst with an intense bursting activity for at least 7 hours, e.g., burst forest, 217+ bursts in 20 min. [e.g., CHIME/FRB Collab. Nature, 2020](#)
- Two-peak FRB coincided with a magnetar X-ray burst (HMXT, INTEGRAL, AGILE, and Konus-Wind)
- Cutoff energy of the FRB-associated burst is higher than others [\(Younes et al., Nature astronomy, 2021\)](#)

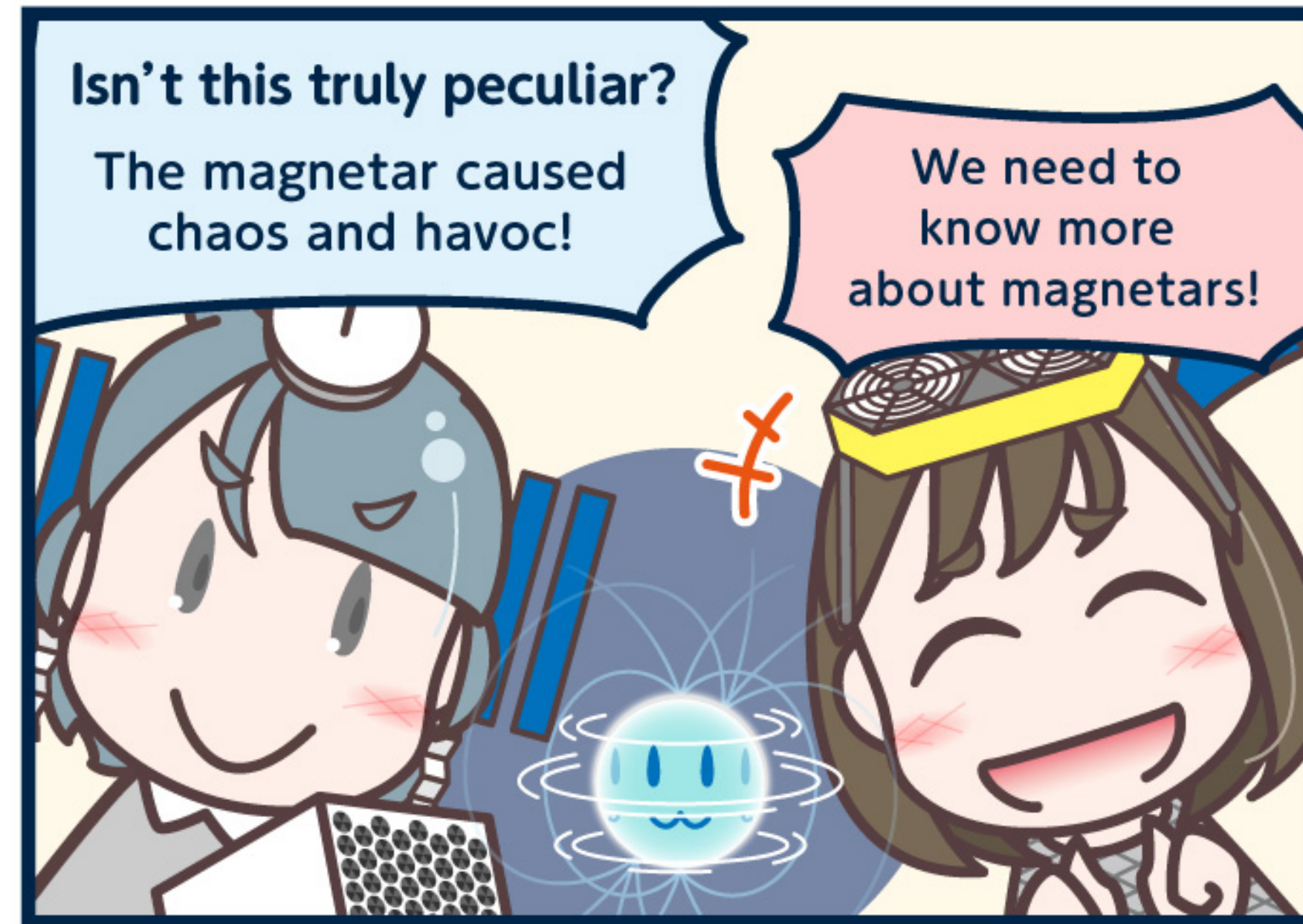
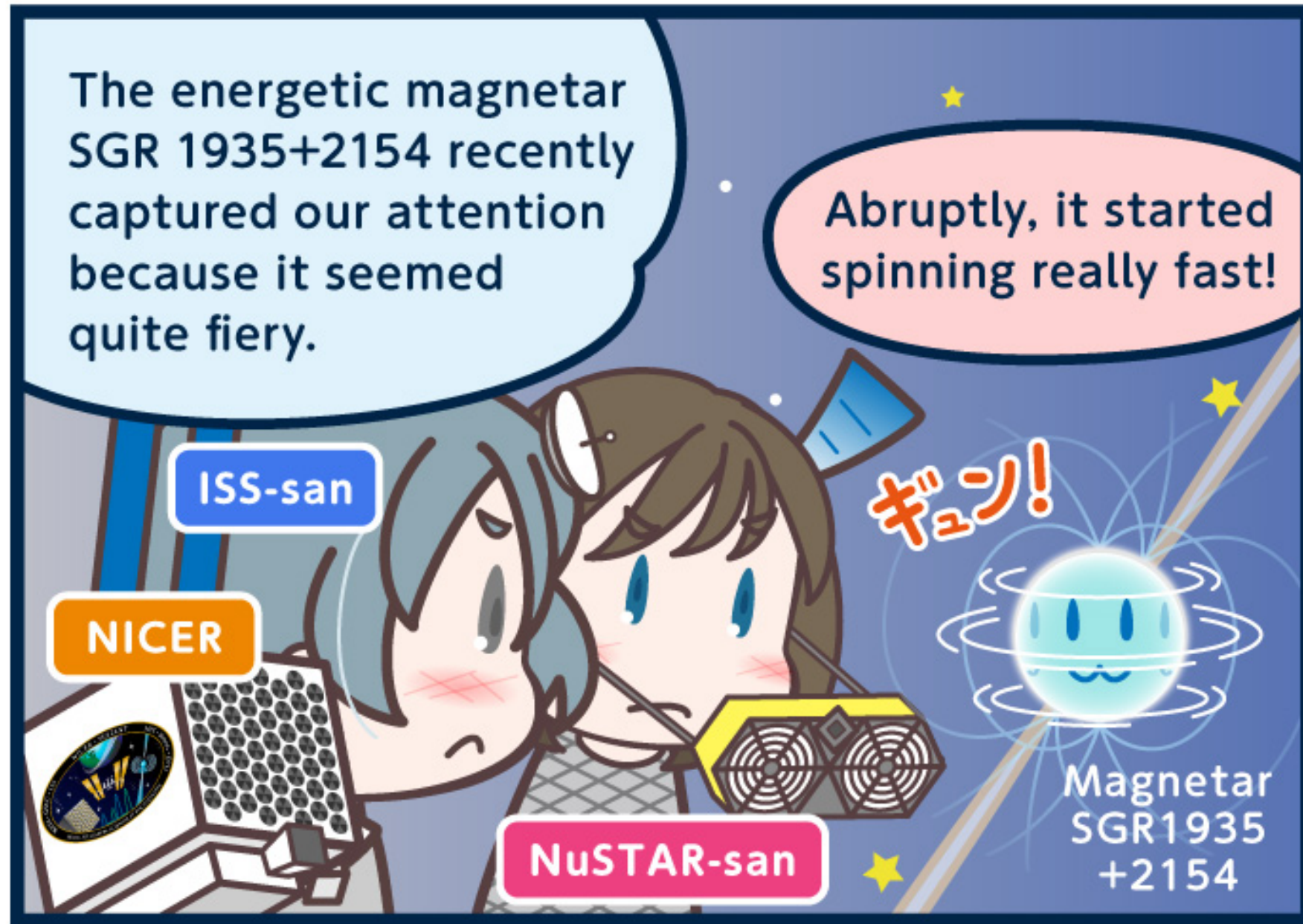


Double glitch around a FRB from SGR 1935+2154

- Another magnetar outburst in 2022 October.
- Our high-cadence ToO monitoring with NICER and NuSTAR serendipitously covered a FRB occurrence (e.g., ATel 15697).
- We detected two strong spin-up glitches and a rapid spin-down between them.
- Released rotational energies at the glitches, $E_{\text{glitch}} = 4\pi^2 I \nu \Delta \nu$, are 3.9×10^{41} erg and 2.6×10^{41} erg (comparable), respectively!!
- Rotational energy loss between the glitches is $dE_{\text{rot}} = \int L_{\text{sd}} dt = \int (4\pi^2 I \nu \dot{\nu}) dt = 6.5 \times 10^{41}$ erg
- Twin double glitches show almost the same intensity and energy release.

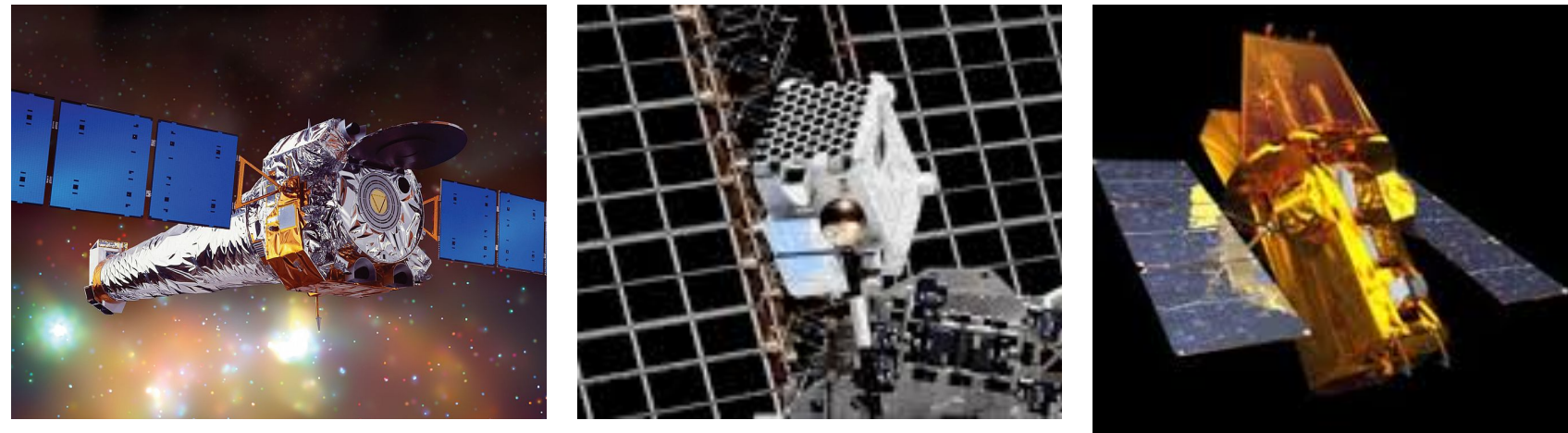


The Case of the Mysterious Magnetar SGR 1935+2154



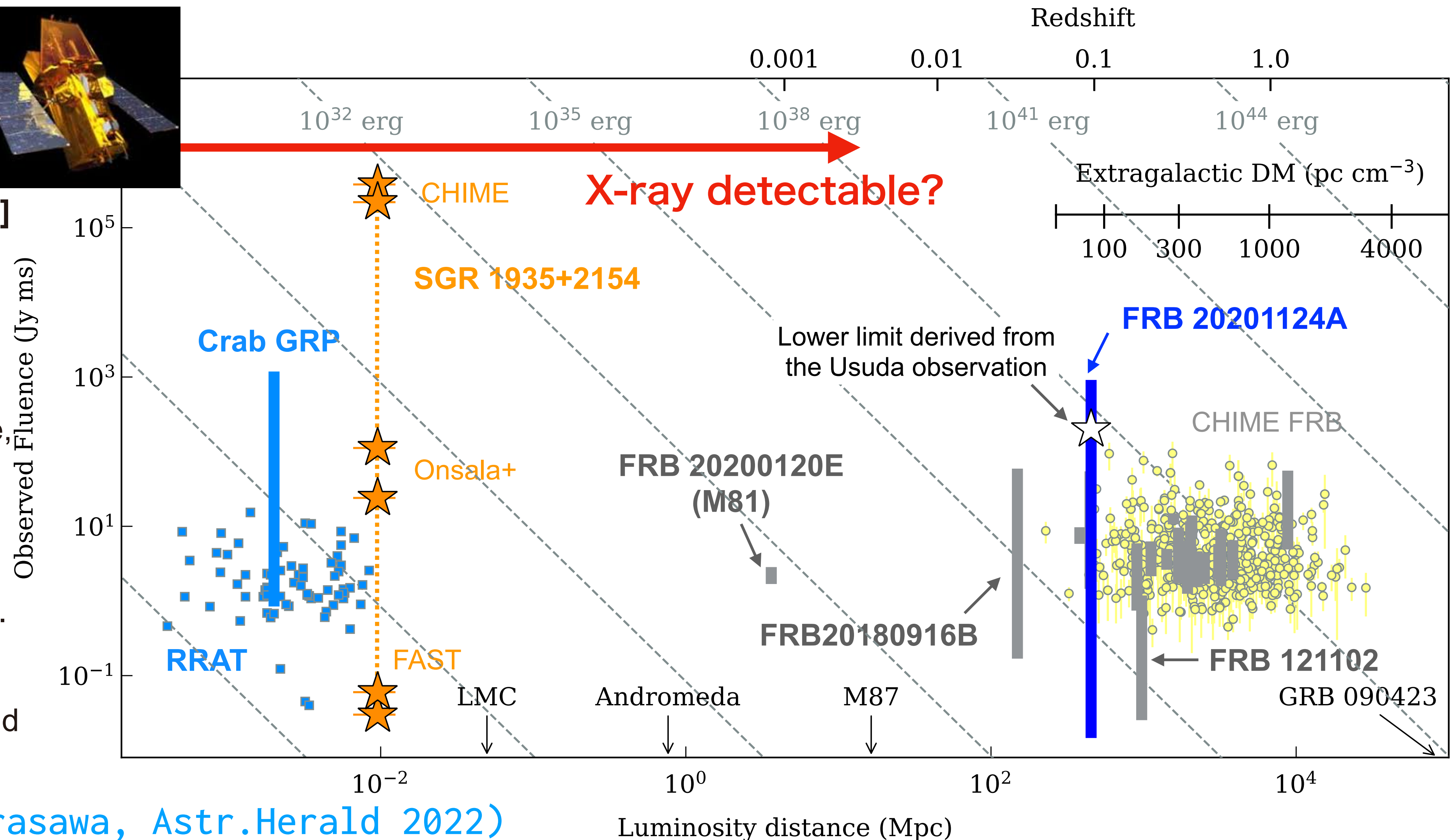
Waiting for nearby repeating FRB discoveries!

- X-ray follow-up observations become very important for nearby repeating FRBs closer than 50 Mpc. We are looking forward to receive alerts from the BURSTT!



[Back-of-envelope calculation]

Assuming persistent X-ray luminosity of $L_x \sim 10^{39}$ erg/s for FRB-related sources or phenomena, the Chandra/ACIS sensitivity, $F_x = 4 \times 10^{-15}$ erg/s/cm² (0.4-6 keV) for a 10 ks exposure, corresponds with reachable distance up to 50 Mpc. For the Swift/XRT of $F_x = 8 \times 10^{-14}$ erg/s/cm² (0.2-10 keV) for a 10-ks exposure, this becomes 10 Mpc. On the X-ray burst detection associated with we need systematic studies of background event properties.



Summary: message to theoreticians from an astronomer

- Neutron stars are observationally diverse. In order to determine the internal equation of state, it is necessary to deeply understand the uncertainty associated with this diversity. Furthermore, we should further consider to use other observational quantities (temperature, B-field, ...) in the future.
- There are several methods for measuring the mass and radius of neutron stars, including measuring the motion of binary stars, X-ray bursts, gravitational redshifts due to absorption lines and light bending, and gravitational waves. NICER is updating the latest EoS measurements.
- Magnetars are a new target for observing the interior of neutron stars. X-ray outbursts from magnetars can be used to measure the response to the release of internal energy deposit. Glitches related to fast radio bursts can be used to learn about angular momentum transfer in the stellar interior.