

## Mesic-Nuclei Bound States

Arpita Mondal\*, Amruta Mishra

*Indian Institute of Technology, Delhi, India*



*based on..*

- AM and Amruta Mishra, Phys. Rev. C 109, 025201 (2024);Phys. Rev. C 110, 055201 (2024);arXiv:2502.08320

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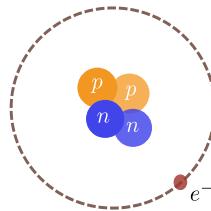
- Overview
- Theoretical Background
- Results & Discussions

# Overview

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# Overview

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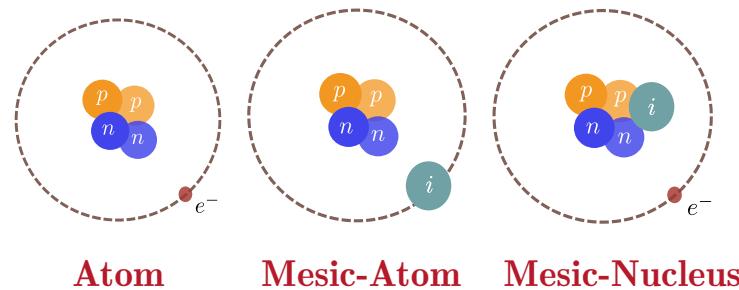
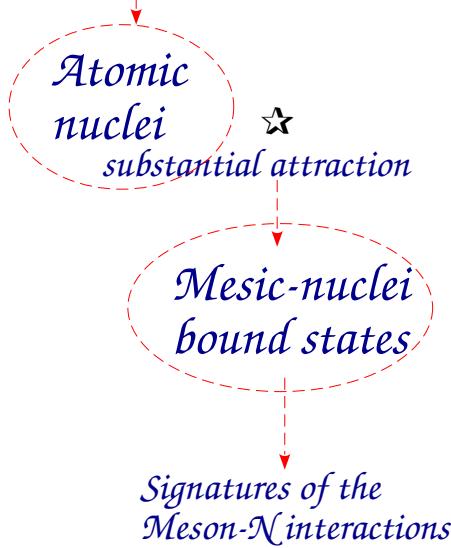


Atom

# Overview

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## Mesons

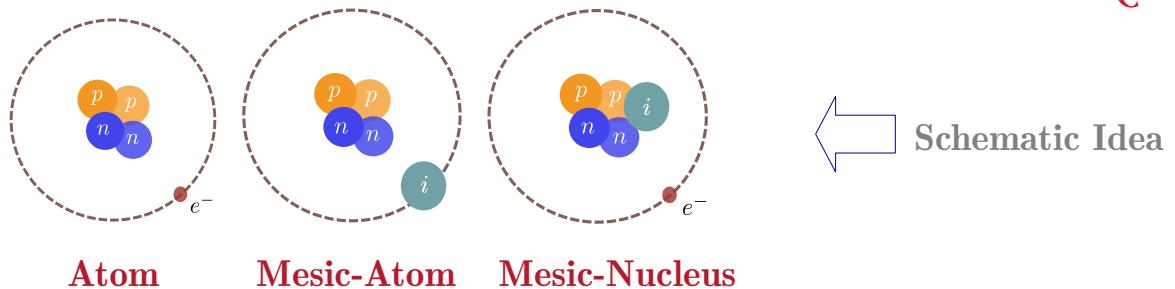
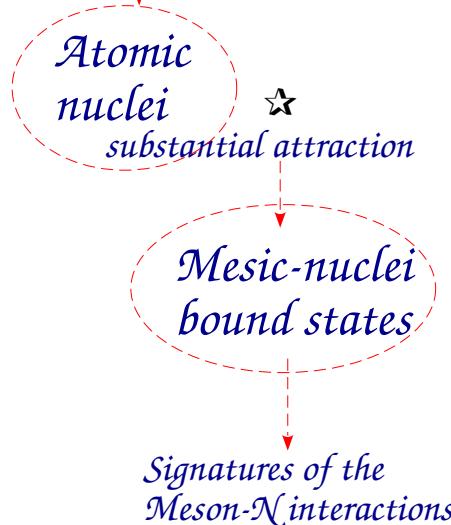


← Schematic Idea

# Overview

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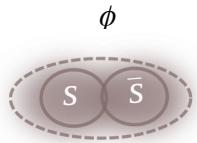
## Mesons



- 1950s (Pionic Atoms): Stearns et al., Phys. Rev. 105, 1573 (1957)
  - 1988 ( $\eta$ -Mesic): BNL : Chrien et al., Phys. Rev. Lett. 60, 2595 (1988)
  - 1996 (Deeply Bound Pionic States): GSI : Yamazaki et al., Z. Phys. A 355, 219 (1996)
  - 2005 (Kaonic nuclei): KEK, FINUDA : Agnello et al., Phys. Rev. Lett. 94, 212303 (2005);  
Suzuki et al., Nucl. Phys. A 754, 375c (2005)
  - 2013–14 ( $\eta$ -Mesic): COSY : Smyrski et al., Phys. Rev. C 87, 015201 (2013);  
Adlarson et al., Phys. Rev. Lett. 112, 202301 (2014)
  - 2020s: (Kaonic nuclei) : J-PARC E15 : Prog. Theor. Exp. Phys. 2021, 051J01 (2021);  
: ( $\eta'$ -Mesic) : MAMI : Metag et al., Eur. Phys. J. A 59, 183 (2023)
- Upcominng: J-PARC, JLab, and FAIR

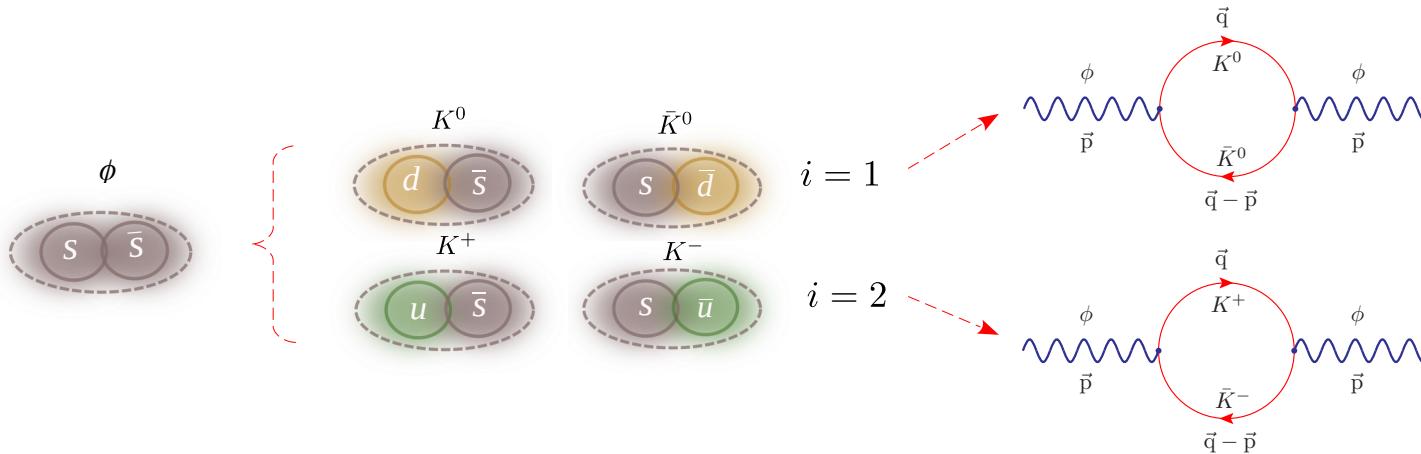
# What's in our mind?

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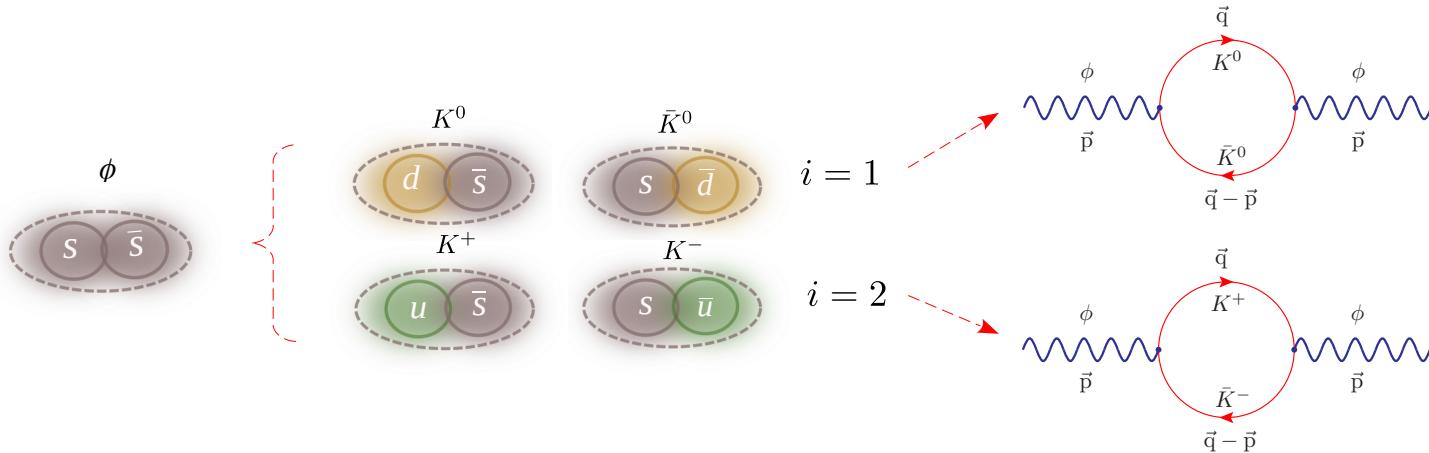
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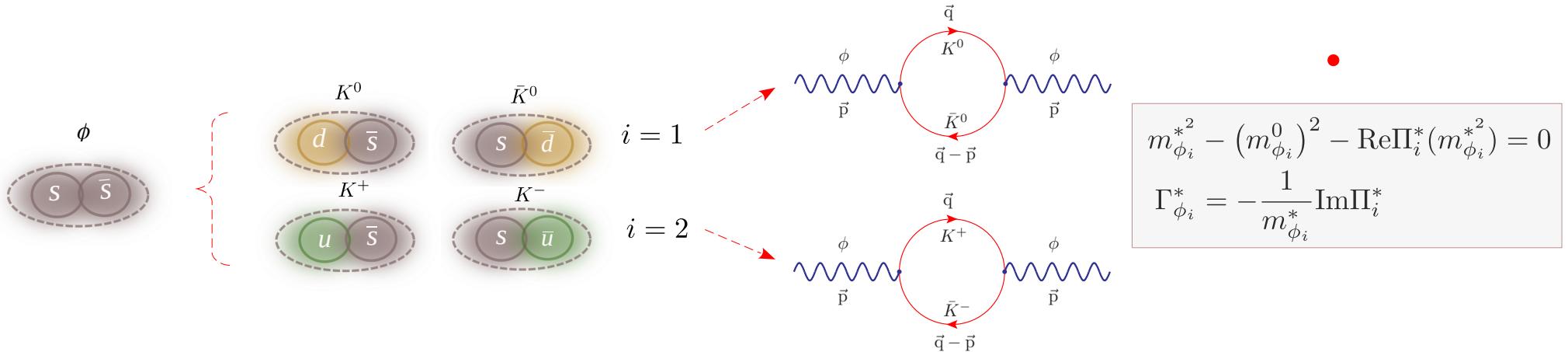
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- $D_i(\omega_i, |\vec{p}| \rightarrow 0, \rho) = \frac{1}{\omega_i^2 - m_{\phi_i}^{0^2} - \Pi_i(\omega_i, |\vec{p}| \rightarrow 0, \rho)}$
- $\Pi_i^*(p) = i \frac{8}{3} g_i^2 \int \frac{d^4 q}{(2\pi)^4} \vec{q}^2 \frac{1}{(q^2 - m_{K_i}^{*2} + i\epsilon)} \frac{1}{((q-p)^2 - m_{K_i}^{*2} + i\epsilon)}$

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$$m_{\phi_i}^{*2} - (m_{\phi_i}^0)^2 - \text{Re}\Pi_i^*(m_{\phi_i}^{*2}) = 0$$

$$\Gamma_{\phi_i}^* = -\frac{1}{m_{\phi_i}^*} \text{Im}\Pi_i^*$$

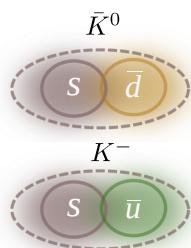
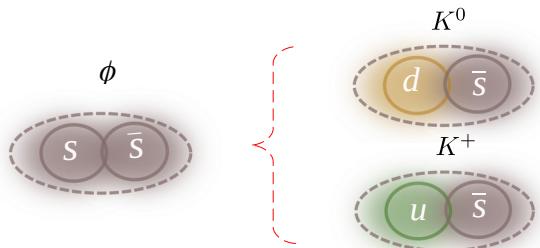
- $D_i(\omega_i, |\vec{p}| \rightarrow 0, \rho) = \frac{1}{\omega_i^2 - m_{\phi_i}^{02} - \Pi_i(\omega_i, |\vec{p}| \rightarrow 0, \rho)}$
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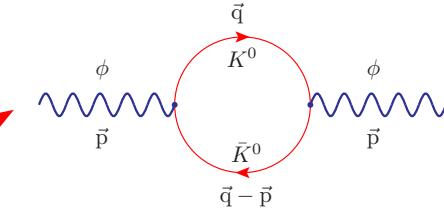
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## Quark Meson Coupling Model

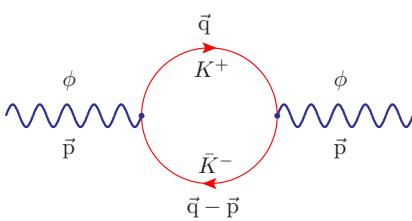
P. A. M. Guichon, Phys. Lett. B 200, 235 (1988)



$i = 1$



$i = 2$



$$m_{\phi_i}^{*2} - (m_{\phi_i}^0)^2 - \text{Re}\Pi_i^*(m_{\phi_i}^{*2}) = 0$$

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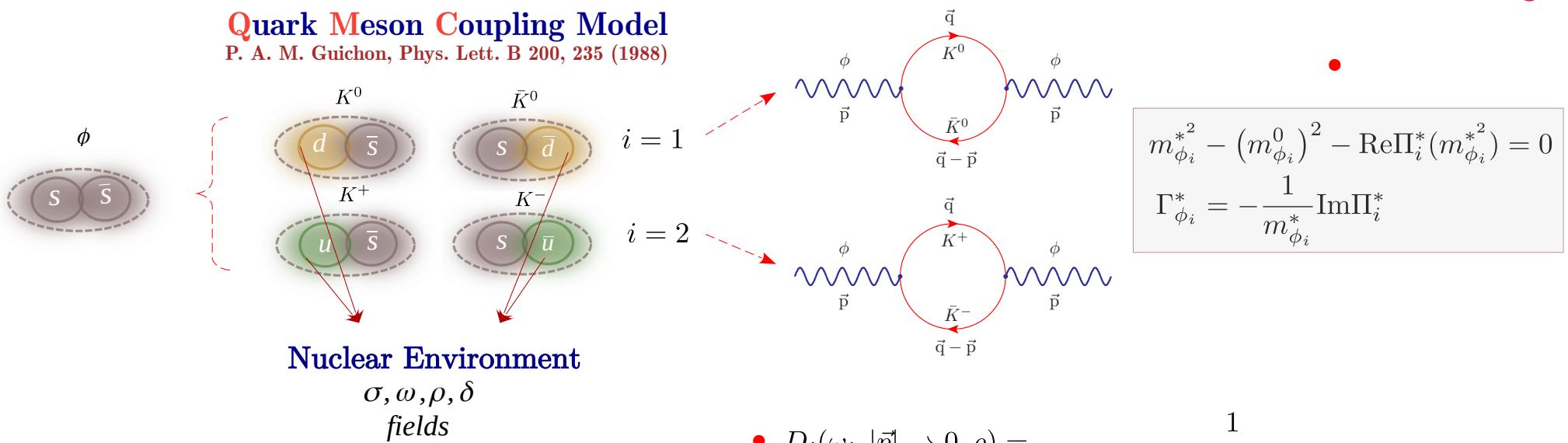
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P. A. M. Guichon, Phys. Lett. B 200, 235 (1988)



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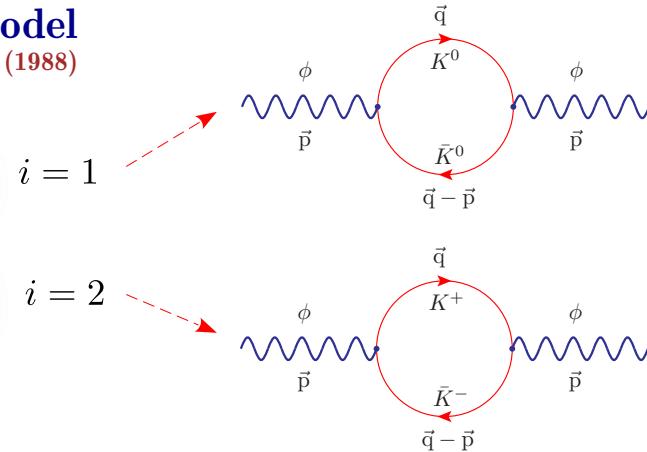
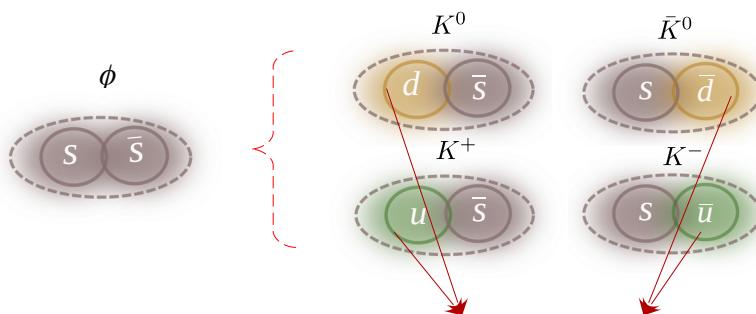
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- $m_u^* = m_u - g_\sigma^q \sigma - \frac{1}{2} g_\delta^q \delta_3,$
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- $m_d^* = m_d - g_\sigma^q \sigma + \frac{1}{2} g_\delta^q \delta_3,$
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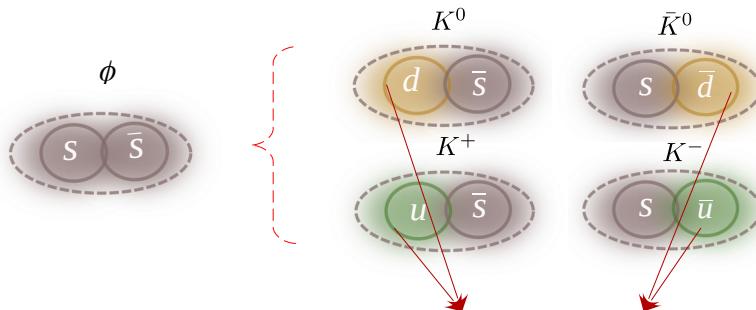
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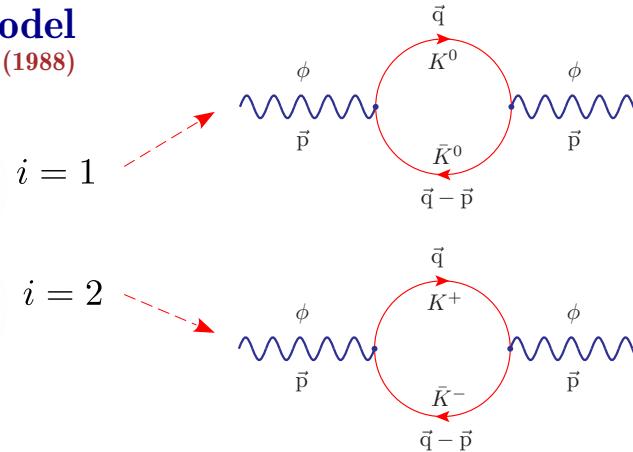
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## Nuclear Environment

$\sigma, \omega, \rho, \delta$   
fields

- $m_u^* = m_u - g_\sigma^q \sigma - \frac{1}{2} g_\delta^q \delta_3,$
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$$m_{\phi_i}^{*2} - (m_{\phi_i}^0)^2 - \text{Re}\Pi_i^*(m_{\phi_i}^{*2}) = 0$$

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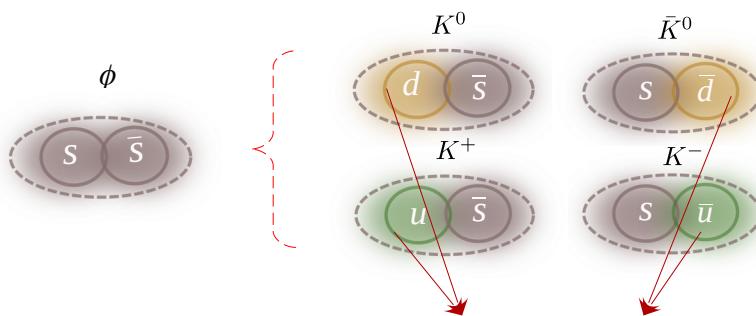
$$m_h^*(\sigma, \delta) = \frac{\sum_f n_{fh} \Omega_{fh}^* - Z_h}{R_h^*} + \frac{4}{3} \pi R_h^{*3} B, \quad \Omega_{fh}^* = \sqrt{x_{fh}^{*2} + (R_h^* m_{fh}^*)^2}$$

# What's in our mind?

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## Quark Meson Coupling Model

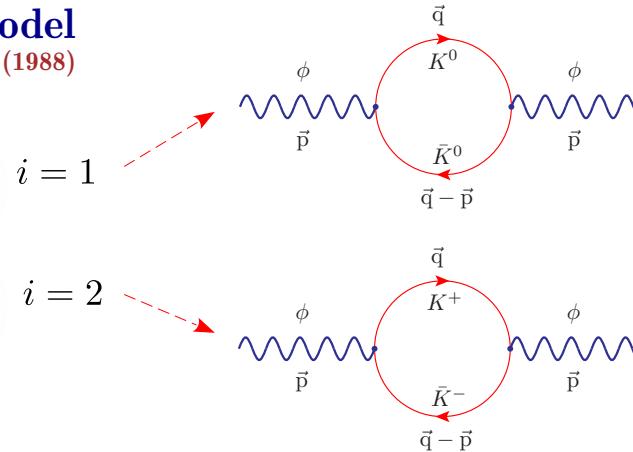
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$$m_{\phi_i}^{*2} - (m_{\phi_i}^0)^2 - \text{Re}\Pi_i^*(m_{\phi_i}^{*2}) = 0$$

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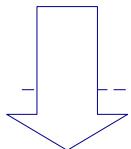
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$$m_h^*(\sigma, \delta) = \frac{\sum_f n_{fh} \Omega_{fh}^* - Z_h}{R_h^*} + \frac{4}{3} \pi R_h^{*3} B, \quad \Omega_{fh}^* = \sqrt{x_{fh}^{*2} + (R_h^* m_{fh}^*)^2}$$

# Framework: QMC Model

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$$\begin{aligned} \mathcal{L} = & \bar{\psi} \left[ i\gamma.\partial - \left( m_N - \underline{\tilde{g}_\sigma(\sigma)\sigma} - \underline{\tilde{g}_\delta(\delta)} \frac{\tau^a}{2} \delta^a \right) - \gamma^\mu \left( g_\omega \omega_\mu + \underline{g_\rho} \frac{\tau^a}{2} \rho_\mu^a \right) \right] \psi \\ & + \frac{1}{2} (\partial_\mu \sigma \partial^\mu \sigma - m_\sigma^2 \sigma^2) + \frac{1}{2} (\partial_\mu \delta^a \partial^\mu \delta^a - m_\delta^2 \delta^a \delta^a) - \left[ \frac{1}{4} \omega_{\mu\nu} \omega^{\mu\nu} - \frac{1}{2} m_\omega^2 \omega_\mu \omega^\mu \right] \\ & - \left( \frac{1}{4} \rho_{\mu\nu}^a \rho^{\mu\nu,a} - \frac{1}{2} m_\rho^2 \rho_\mu^a \rho^{\mu,a} \right) \end{aligned}$$



## Nuclear Matter

$$(i) \quad \phi = \frac{1}{m_\phi^2} \sum_{N=p,n} \left( -\frac{\partial m_N^*(\phi)}{\partial \phi} \right) \rho_N^s, \quad \text{where, } \phi = \sigma, \delta^3,$$

$$(ii) \quad \omega_0 = \sum_{N=p,n} \frac{g_\omega}{m_\omega^2} \rho_N = \frac{g_\omega}{m_\omega^2} \rho_B,$$

$$(iii) \quad \rho_0^3 = \sum_{N=p,n} \frac{g_\rho}{m_\rho^2} \frac{(\tau^3 \rho)_N}{2} = -\frac{g_\rho}{m_\rho^2} \eta \rho_B,$$

## Scalar densities and number densities:

$$\rho_N^s = \frac{2}{(2\pi)^3} \int d^3 \vec{k} \Theta(k_{FN} - |\vec{k}|) \frac{m_N^*(\sigma, \delta^3)}{\sqrt{m_N^{*2}(\sigma, \delta^3) + |\vec{k}|^2}},$$

$$\rho_N = \frac{2}{(2\pi)^3} \int d^3 \vec{k} \Theta(k_{FN} - |\vec{k}|) = \frac{k_{FN}^3}{3\pi^2}$$

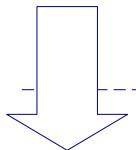
$$\eta = (\rho_n - \rho_p)/(2\rho_B) \quad \text{Asymmetry Parameter}$$

$$\begin{aligned} \tilde{g}_{\sigma,\delta}(\sigma, \delta) &= g_{\sigma,\delta}^q \sum_q n_{qN} S_{qN}(\sigma, \delta) \\ S_{qN}(\sigma) &= \mathcal{I}_N^s, \quad S_{qN}(\delta^3) = \frac{\tau_q^3}{2} \mathcal{I}_N^s, \\ \mathcal{I}_N^s &= \frac{\Omega_{qN}/2 + m_{qN}^* R_N^*(\Omega_{qN} - 1)}{\Omega_{qN}(\Omega_{qN} - 1) + m_{qN}^* R_N^*/2} \\ g_\omega &= g_\omega^q \sum_q n_{qN}, \quad g_\rho = g_\rho^q \end{aligned}$$

# Framework: QMC Model

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$$\begin{aligned} \mathcal{L} = \bar{\psi} & \left[ i\gamma.\partial - \left( m_N - \underline{\tilde{g}_\sigma(\sigma)\sigma} - \underline{\tilde{g}_\delta(\delta)} \frac{\tau^a}{2} \delta^a \right) - \gamma^\mu \left( g_\omega \omega_\mu + \underline{g_\rho} \frac{\tau^a}{2} \rho_\mu^a \right) \right] \psi \\ & + \frac{1}{2} (\partial_\mu \sigma \partial^\mu \sigma - m_\sigma^2 \sigma^2) + \frac{1}{2} (\partial_\mu \delta^a \partial^\mu \delta^a - m_\delta^2 \delta^a \delta^a) - \left[ \frac{1}{4} \omega_{\mu\nu} \omega^{\mu\nu} - \frac{1}{2} m_\omega^2 \omega_\mu \omega^\mu \right] \\ & - \left( \frac{1}{4} \rho_{\mu\nu}^a \rho^{\mu\nu,a} - \frac{1}{2} m_\rho^2 \rho_\mu^a \rho^{\mu,a} \right) - \frac{e}{2} \psi \gamma^\mu (1 + \tau^a) A_\mu - \frac{1}{4} A_{\mu\nu} A^{\mu\nu} \end{aligned}$$



## Finite Nucleus

$$\left( -\frac{d^2}{dr^2} - \frac{2}{r} \frac{d}{dr} + m_M^2 \right) M(r) = \mathcal{J}_M(r)$$



$$\begin{cases} g_\sigma \left[ \rho_p^s(r) \left( -\frac{\partial m_p^*(r)}{\partial \sigma} \right) + \rho_n^s(r) \left( -\frac{\partial m_n^*(r)}{\partial \sigma} \right) \right] & \text{for } \sigma \text{ field} \\ \frac{g_\delta}{2} \left[ \rho_p^s(r) \left( -\frac{\partial m_p^*(r)}{\partial \delta^3} \right) + \rho_n^s(r) \left( -\frac{\partial m_n^*(r)}{\partial \delta^3} \right) \right] & \text{for } \delta^3 \text{ field} \\ g_\omega \left[ \rho_p(r) + \rho_n(r) \right] & \text{for } \omega_0 \text{ field} \\ \frac{g_\rho}{2} \left[ \rho_p(r) - \rho_n(r) \right] & \text{for } \rho_0^3 \text{ field} \\ e \rho_p(r) & \text{for Coulomb field} \end{cases}$$

$$\begin{aligned} \tilde{g}_{\sigma,\delta}(\sigma, \delta) &= g_{\sigma,\delta}^q \sum_q n_{qN} S_{qN}(\sigma, \delta) \\ S_{qN}(\sigma) &= \mathcal{I}_N^s, \quad S_{qN}(\delta^3) = \frac{\tau_q^3}{2} \mathcal{I}_N^s, \\ \mathcal{I}_N^s &= \frac{\Omega_{qN}/2 + m_{qN}^* R_N^*(\Omega_{qN} - 1)}{\Omega_{qN}(\Omega_{qN} - 1) + m_{qN}^* R_N^*/2} \\ g_\omega &= g_\omega^q \sum_q n_{qN}, \quad g_\rho = g_\rho^q \end{aligned}$$

## Scalar densities and number densities:

$$\rho_p^s(r) = \sum_p^Z \frac{(2j_p + 1)}{4\pi r^2} (|G_p(r)|^2 - |F_p(r)|^2),$$

$$\rho_n^s(r) = \sum_n^N \frac{(2j_n + 1)}{4\pi r^2} (|G_n(r)|^2 - |F_n(r)|^2),$$

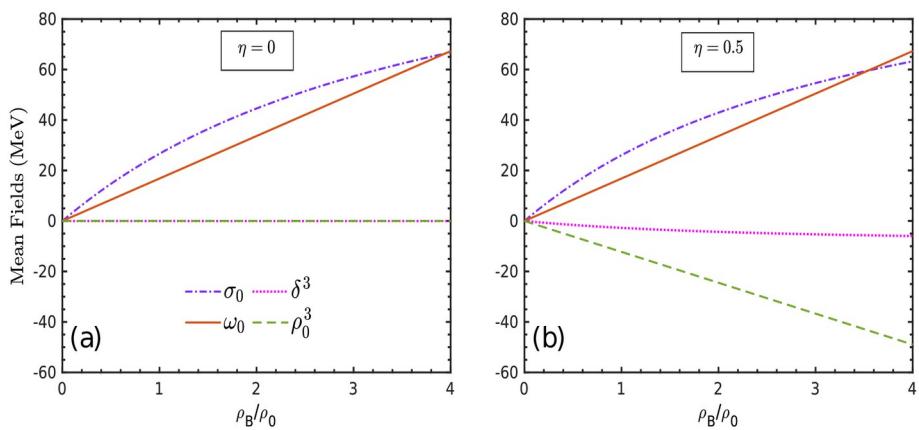
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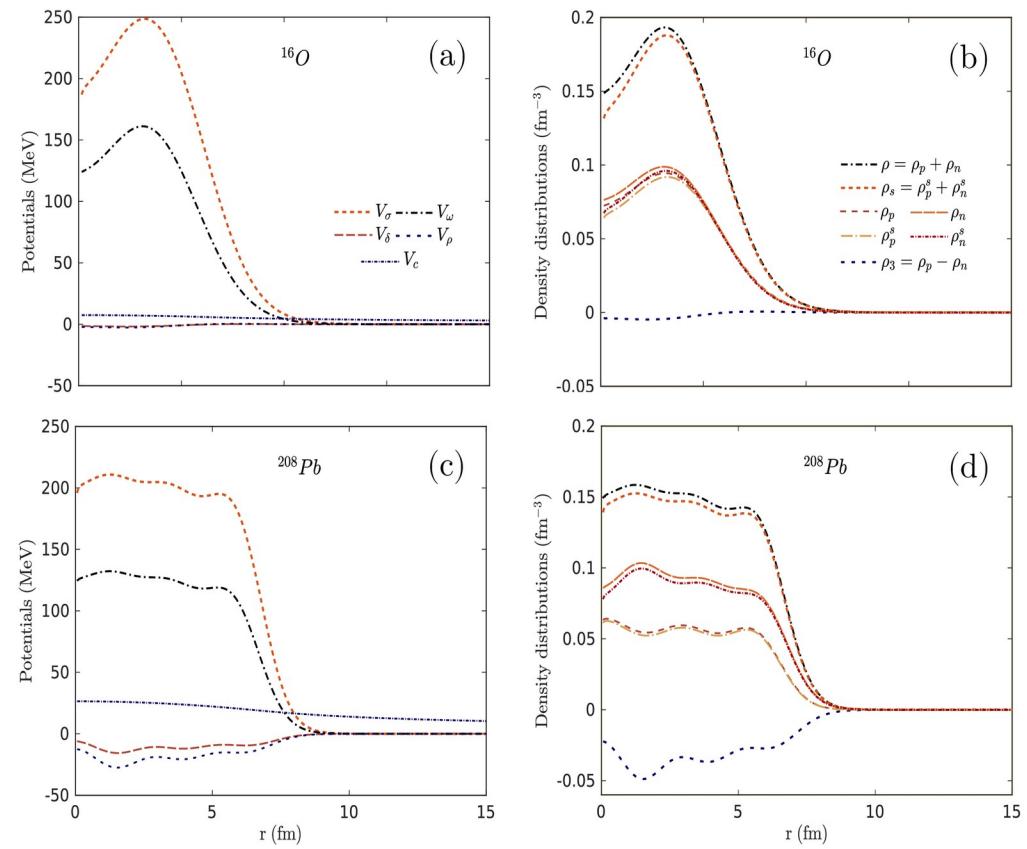
# Potentials in different nuclear environment

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## Nuclear Matter

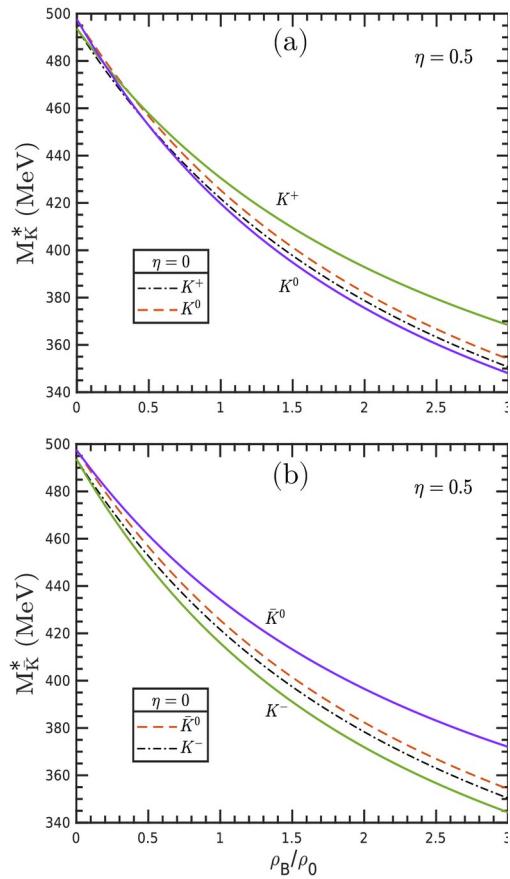


## Finite Nucleus

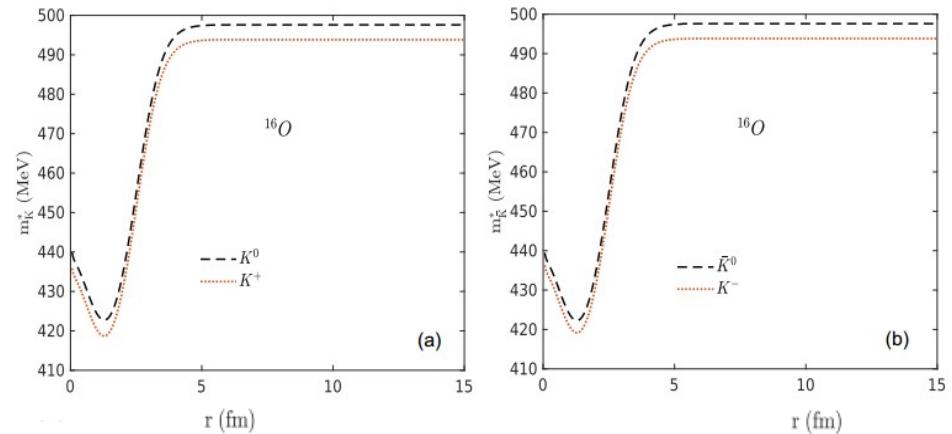


# Masses of K mesons

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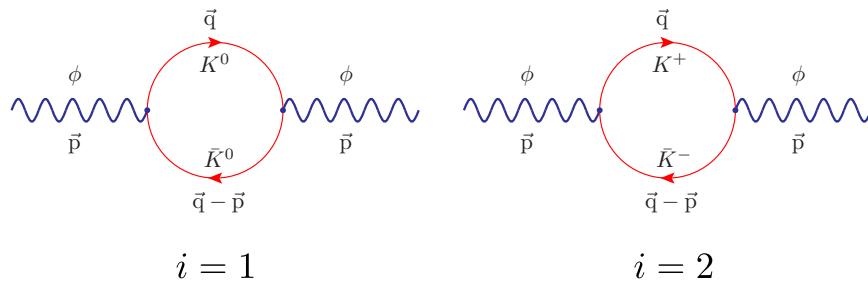
## Mass Splittings



# Phi in nuclear environment

•  $\phi$  meson  kaons

$\mathcal{HIN}25$



$$\bullet \quad \Pi_i^*(p) = i \frac{8}{3} g_i^2 \int \frac{d^4 q}{(2\pi)^4} \vec{q}^2 \frac{1}{(q^2 - m_{K_i}^{*2} + i\epsilon)} \frac{1}{((q-p)^2 - m_{\bar{K}_i}^{*2} + i\epsilon)}$$

$$\text{Re}\Pi_i^* = -\frac{4}{3} g_i^2 \mathcal{P} \int_0^{\Lambda_K} \left[ \frac{d^3 q}{(2\pi)^3} q^2 \left( \frac{\Lambda_K^2 + m_{\phi_i}^{*2}}{\Lambda_K^2 + 4E_{K_i}^{*2}} \right)^2 \left( \frac{\Lambda_K^2 + m_{\phi_i}^{*2}}{\Lambda_K^2 + 4E_{\bar{K}_i}^{*2}} \right)^2 \frac{(E_{K_i}^* + E_{\bar{K}_i}^*)}{E_{K_i}^* E_{\bar{K}_i}^* ((E_{K_i}^* + E_{\bar{K}_i}^*)^2 - m_{\phi_i}^{*2})} \right], E_{K(\bar{K})_i}^* = (q^2 + m_{K(\bar{K})_i}^{*2})^{1/2}$$

$$\text{Im}\Pi_i^* = \frac{2}{3\pi} g_i^2 |\vec{q}_i|^3 \quad |\vec{q}_i| = \frac{1}{2m_\phi^*} \left( (m_{\phi_i}^{*2} - (m_{K_i}^* + m_{\bar{K}_i}^*)^2)(m_{\phi_i}^{*2} - (m_{K_i}^* - m_{\bar{K}_i}^*)^2) \right)^{1/2}$$

$i$	$\phi \rightarrow K_L^0 K_S^0$	$\phi \rightarrow K^+ K^-$
$\Gamma_{\phi_i}/\Gamma_\phi^{tot}$	33.9 %	49.1 %
$\Gamma_{\phi_i}$ (MeV)	1.440	2.086
$g_i$	3.3212	3.2281

●

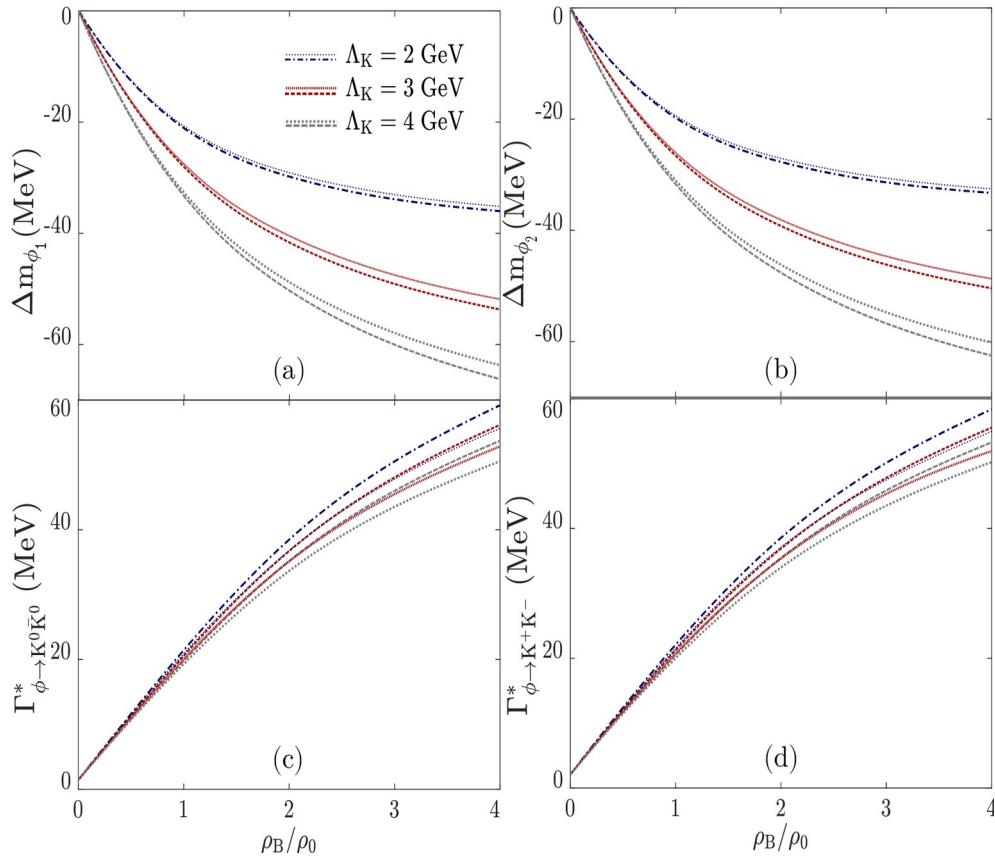
$m_{\phi_i}^{*2} - (m_{\phi_i}^0)^2 - \text{Re}\Pi_i^*(m_{\phi_i}^{*2}) = 0$ 
 $\Gamma_{\phi_i}^* = -\frac{1}{m_{\phi_i}^*} \text{Im}\Pi_i^*$

$\Lambda_K$ (GeV)	$m_{\phi_i}^0$ (MeV) ( $i = 1$ )	$m_{\phi_i}^0$ (MeV) ( $i = 2$ )
2	1074.0	1073.2
3	1133.6	1130.7
4	1215.2	1209.4

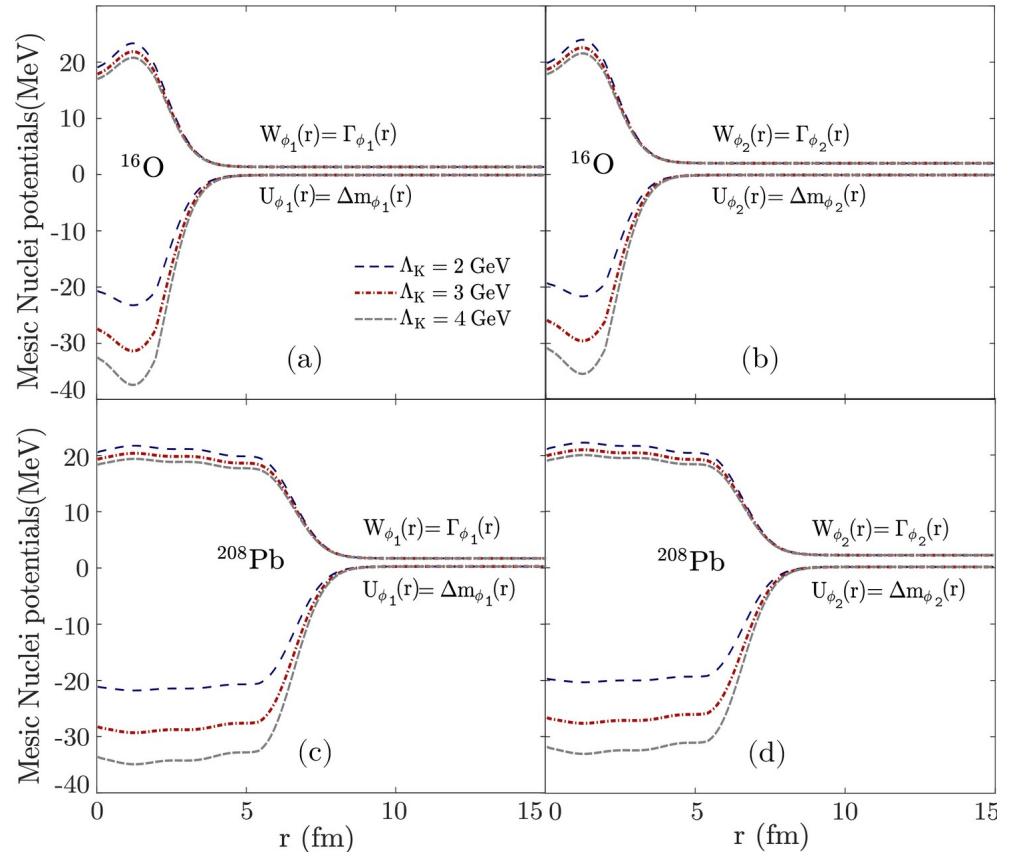
# Phi in nuclear environment

HIN25

## Nuclear Matter



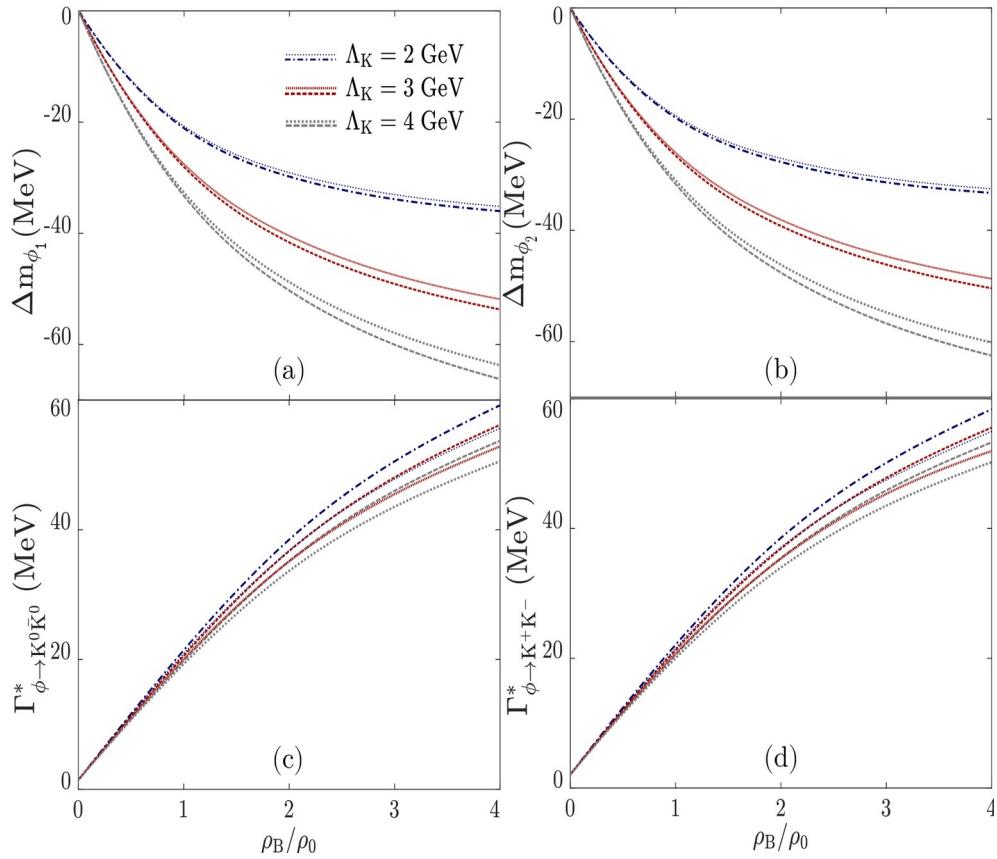
## Finite Nuclei



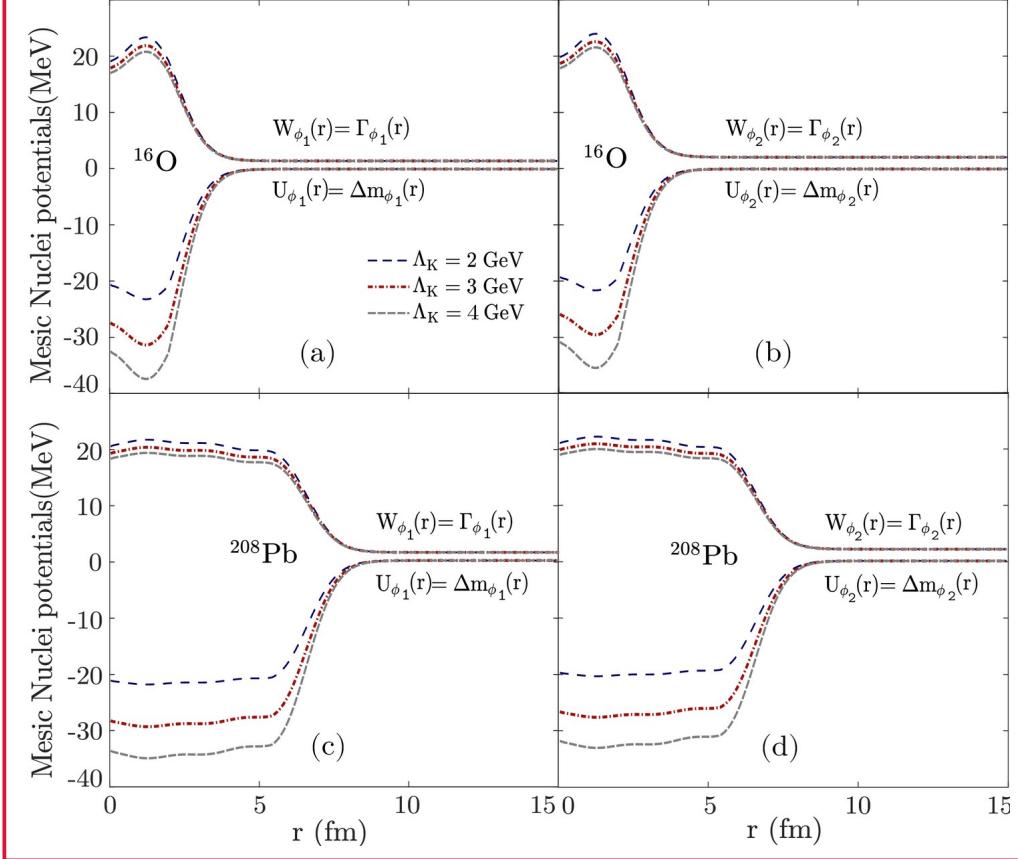
# Phi in nuclear environment

HIN25

## Nuclear Matter



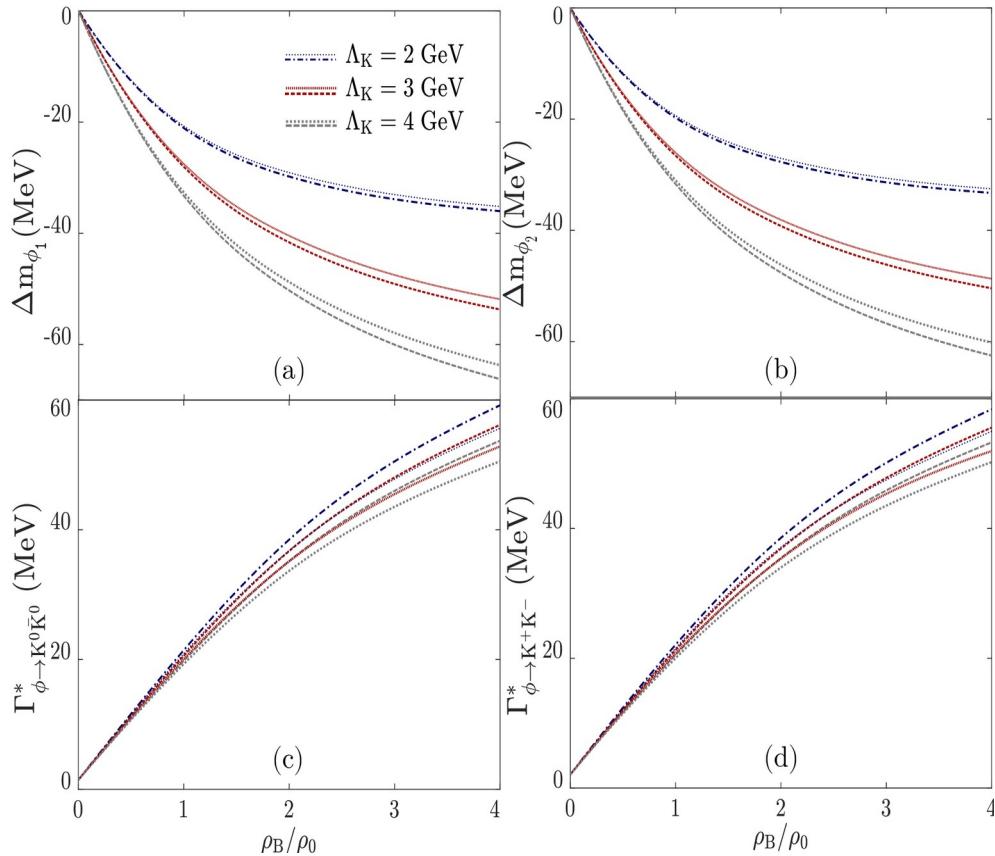
## Finite Nuclei



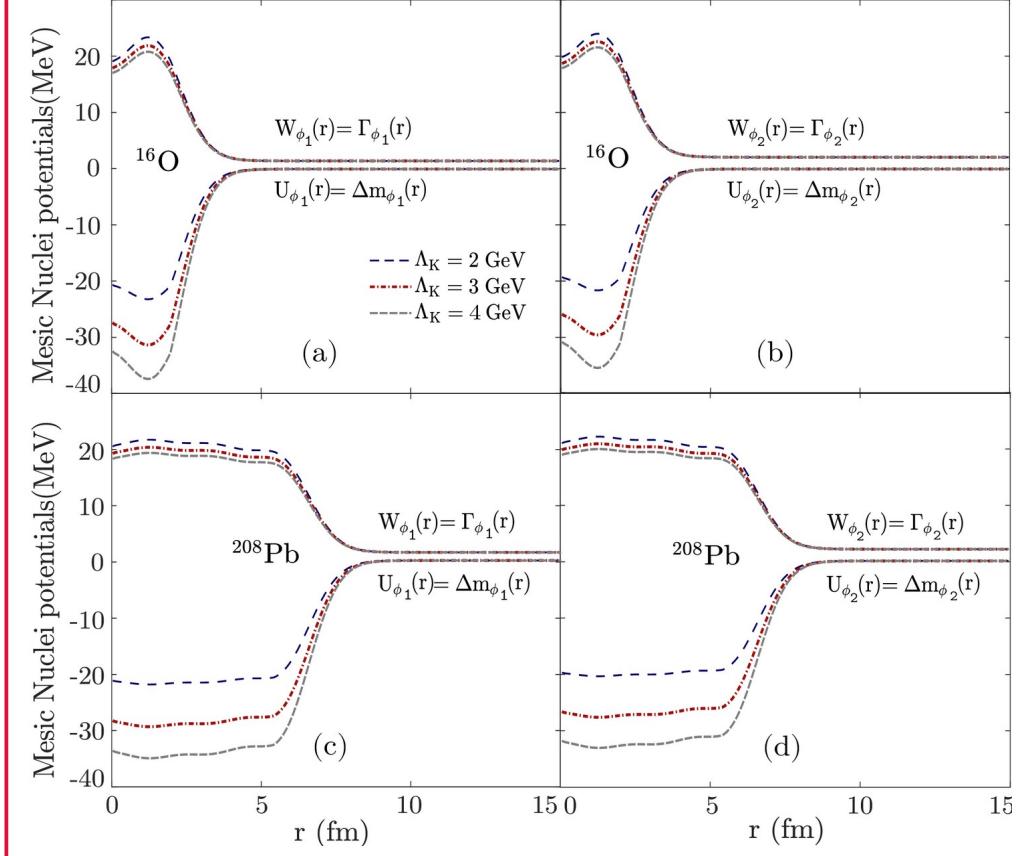
# Phi in nuclear environment

HIN25

## Nuclear Matter



## Finite Nuclei



$$\checkmark V_{\phi_i}(r) = U_{\phi_i}(r) - \frac{i}{2} W_{\phi_i}(r)$$

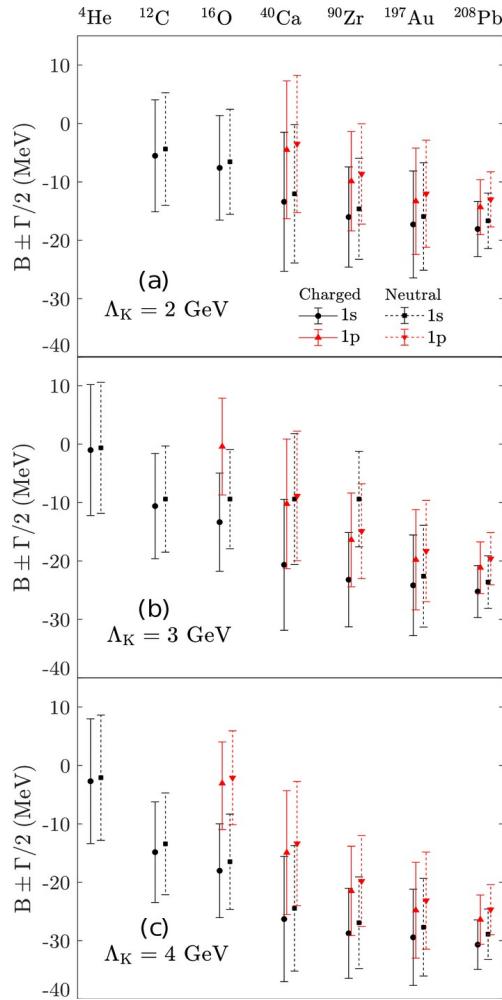
# Formation of Meson-Nucleus bound states

HIN25

$$\left( -\nabla^2 + (\mu + V_{\phi_i}(r))^2 \right) \Phi_i(r) = \epsilon_i^2 \Phi_i(r)$$
$$B_i = \text{Re}(\epsilon_i) - \mu \quad \Gamma_i = -2\text{Im}(\epsilon_i)$$

# Phi in atomic nucleus

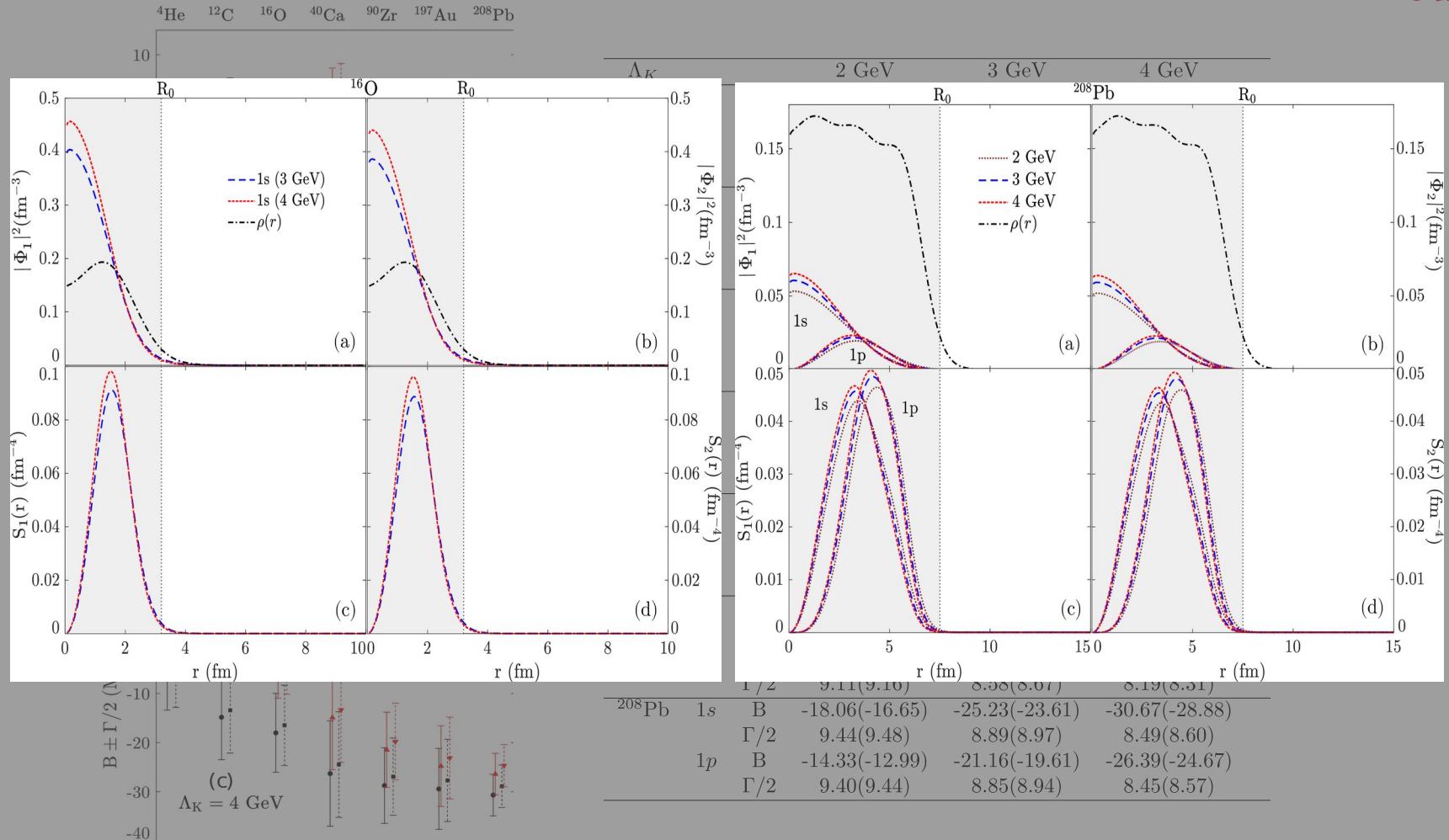
HIN25



$\Lambda_K$		2 GeV	3 GeV	4 GeV	
${}^4\text{He}$	1s	B Γ/2	×	(x)	-1.02(-0.64) 11.21(11.21)
	1p	B Γ/2	×	(x)	10.68(10.72) ×
	1s	B Γ/2	×	(x)	×
	1p	B Γ/2	×	(x)	×
${}^{12}\text{C}$	1s	B Γ/2	-5.53(-4.63) 9.59(9.63)	-10.61(-9.41) 9.02(9.09)	-14.84(-13.42) 10.68(10.72)
	1p	B Γ/2	×	(x)	×
	1s	B Γ/2	×	(x)	×
	1p	B Γ/2	×	(x)	×
${}^{16}\text{O}$	1s	B Γ/2	-7.60(-6.55) 8.94(8.99)	-13.36(-12.02) 8.41(8.50)	-18.02(-16.48) 8.03(8.15)
	1p	B Γ/2	×	(x)	-0.42(×) 8.30(×)
	1s	B Γ/2	-	-	-
	1p	B Γ/2	-	-	-
${}^{40}\text{Ca}$	1s	B Γ/2	-13.40(-12.04) 11.90(11.84)	-20.66(-19.03) 11.21(11.21)	-26.29(-24.45) 10.72(10.75)
	1p	B Γ/2	-4.51(-3.49) 11.79(11.74)	-10.22(-8.88) 11.09(11.09)	-14.92(-13.36) 10.59(10.63)
	1s	B Γ/2	-	-	-
	1p	B Γ/2	-	-	-
${}^{90}\text{Zr}$	1s	B Γ/2	-16.01(-14.61) 8.57(8.64)	-23.21(-21.59) 8.07(8.18)	-28.73(-26.92) 7.71(7.84)
	1p	B Γ/2	-9.88(-8.64) 8.51(8.59)	-16.39(-14.90) 8.02(8.12)	-21.48(-19.80) 7.65(7.78)
	1s	B Γ/2	-	-	-
	1p	B Γ/2	-	-	-
${}^{197}\text{Au}$	1s	B Γ/2	-17.28(-15.92) 9.15(9.20)	-24.17(-22.61) 8.62(8.71)	-29.42(-27.69) 8.23(8.35)
	1p	B Γ/2	-13.31(-12.03) 9.11(9.16)	-19.79(-18.31) 8.58(8.67)	-24.78(-23.13) 8.19(8.31)
	1s	B Γ/2	-	-	-
	1p	B Γ/2	-	-	-
${}^{208}\text{Pb}$	1s	B Γ/2	-18.06(-16.65) 9.44(9.48)	-25.23(-23.61) 8.89(8.97)	-30.67(-28.88) 8.49(8.60)
	1p	B Γ/2	-14.33(-12.99) 9.40(9.44)	-21.16(-19.61) 8.85(8.94)	-26.39(-24.67) 8.45(8.57)
	1s	B Γ/2	-	-	-
	1p	B Γ/2	-	-	-

# Phi in atomic nucleus

HIN(25)



- We study the probable interactions of  $\phi$  meson in different nuclear environment.
- $\phi$  meson-nucleus bound states are studied with the mass modification of  $\phi$  meson using the charged as well as neutral kaon loops with the modified masses of  $K$  and  $\bar{K}$  mesons as calculated within the QMC model.

Thank you for your attention



**Back Ups**

Bag Parameters							Coupling Constants				in MeV	
$M_p$ (MeV)	$R_p$ (fm)	$B^{1/4}$ (MeV) $^{1/4}$	$Z_p$	$M_n$ (MeV)	$R_n$ (fm)	$Z_n$	$g_\sigma^q$	$g_\delta^q$	$g_\omega^q$	$g_\rho^q$	$m_u = 2.16$	$m_s = 93.4$
938.272	0.6	211.238	4.0015	939.565	0.6003	4.0012	5.98	12.60	2.98	12.59	$m_d = 4.67$	$m_c = 1270$

A.M. and Amruta Mishra, Phys. Rev. C 109 025201(2024)

[ A. M. Santos et al., Phys. Rev. C 79, 045805 (2009) ]

For the vacuum masses and constant B

	$M$ (MeV) (I)	$R$ (fm)	$Z$
$K^0 (\bar{K}^0)$	497.611	0.4824	3.2860
$K^+ (K^-)$	493.677	0.4811	3.2924
$D^0 (\bar{D}^0)$	1864.84	0.5798	1.8423
$D^+ (D^-)$	1869.66	0.5808	1.8319
$B^0 (\bar{B}^0)$	5279.66	0.6508	-0.2609
$B^+ (B^-)$	5279.34	0.6507	-0.2638

$$M_i^\star(\sigma, \delta^3) = \frac{\sum_f n_{fi} \Omega_{fi}^\star - Z_i}{R_i^\star} + \frac{4}{3} \pi R_i^{\star 3} B$$

$$\left( \frac{d}{dr} + \frac{\kappa}{r} \right) G_\alpha(r) - [\epsilon_\alpha -$$

## Initial Guess :

$$\rho_p^s(r) = \sum_p^Z \frac{(2j_p + 1)}{4\pi r^2} (|G_p(r)|^2 - |F_p(r)|^2),$$

$$\rho_n^s(r) = \sum_n^N \frac{(2j_n + 1)}{4\pi r^2} (|G_n(r)|^2 - |F_n(r)|^2),$$

$$\rho_p(r) = \sum_p^Z \frac{(2j_p + 1)}{4\pi r^2} (|G_p(r)|^2 + |F_p(r)|^2),$$

$$\rho_n(r) = \sum_n^N \frac{(2j_p + 1)}{4\pi r^2} (|G_n(r)|^2 + |F_n(r)|^2),$$

•  $(-\frac{d^2}{dr^2} - \frac{2}{r}\frac{d}{dr} + m_M^2)M(r) = \mathcal{J}_M(r)$

$$\left\{ \begin{array}{l} g_\sigma \left[ \rho_p^s(r) \left( -\frac{\partial m_p^*(r)}{\partial \sigma} \right) + \rho_n^s(r) \left( -\frac{\partial m_n^*(r)}{\partial \sigma} \right) \right] \\ \frac{g_\delta}{2} \left[ \rho_p^s(r) \left( -\frac{\partial m_p^*(r)}{\partial \delta^3} \right) + \rho_n^s(r) \left( -\frac{\partial m_n^*(r)}{\partial \delta^3} \right) \right] \\ g_\omega \left[ \rho_p(r) + \rho_n(r) \right] \\ \frac{g_\rho}{2} \left[ \rho_p(r) - \rho_n(r) \right] \\ e\rho_p(r) \end{array} \right.$$

Y.K.Gambhir et.al.,  
Annals of Phys, 198,  
132 (1990)

$$S(r) = V_\sigma(r) + \frac{\tau^3}{2} V_\delta(r) \frac{(+1)}{r^2} (|G_p(r)|^2 - |F_p(r)|^2),$$

$$V(r) = V_\omega(r) + \frac{\tau^3}{2} V_\rho(r) + \frac{(1+\tau^3)}{2} V_C(r)$$

$$V(r) = V_\omega(r) + \frac{\gamma}{2} V_\rho(r) + \frac{(1+\gamma)}{2} V_C(r)$$

$$\rho_n^s(r) = \sum_n \frac{(-)^{n+1}}{4\pi r^2} (|G_n(r)|^2 - |F_n(r)|^2),$$

$$\left( -\partial m^*(n) \right) = \left( -\partial m^*(n) \right) \boxed{Z_{\alpha}(\partial m^*(n))}$$

for  $\sigma$  field  $+ |F_p(r)|^2),$

$$(r) \left( -\frac{\partial m_p^*(r)}{\partial \delta^3} \right) + \rho_n^s(r) \left( -\frac{\partial m_n^*(r)}{\partial \delta^3} \right) \quad \text{for } \delta^3 \text{ field}$$

$$(r) + \rho_n(r)] \quad \text{for } \omega_0 \text{ field} \quad + |F_n(r)|^2),$$

(r) -  $\rho_n(r)$  Y.K.Gambhir et.al., for  $\rho_0^3$  field

for  $\rho_0$  field  
for Coulomb field

$$\psi_{\alpha,k,m} = \begin{pmatrix} i \frac{G_\alpha^k(r)}{r} Y_{jm}^l(\theta, \phi, s) \\ -\frac{F_\alpha^k(r)}{r} \dot{Y}_{jm}^l(\theta, \phi, s) \end{pmatrix} \chi_{t_a}(t)$$

$$V_{ws} = \frac{V_0}{1 + \exp\left(\frac{r - R_0}{a}\right)}$$

Adjusted with the nuclear matter results at  $r \rightarrow 0$

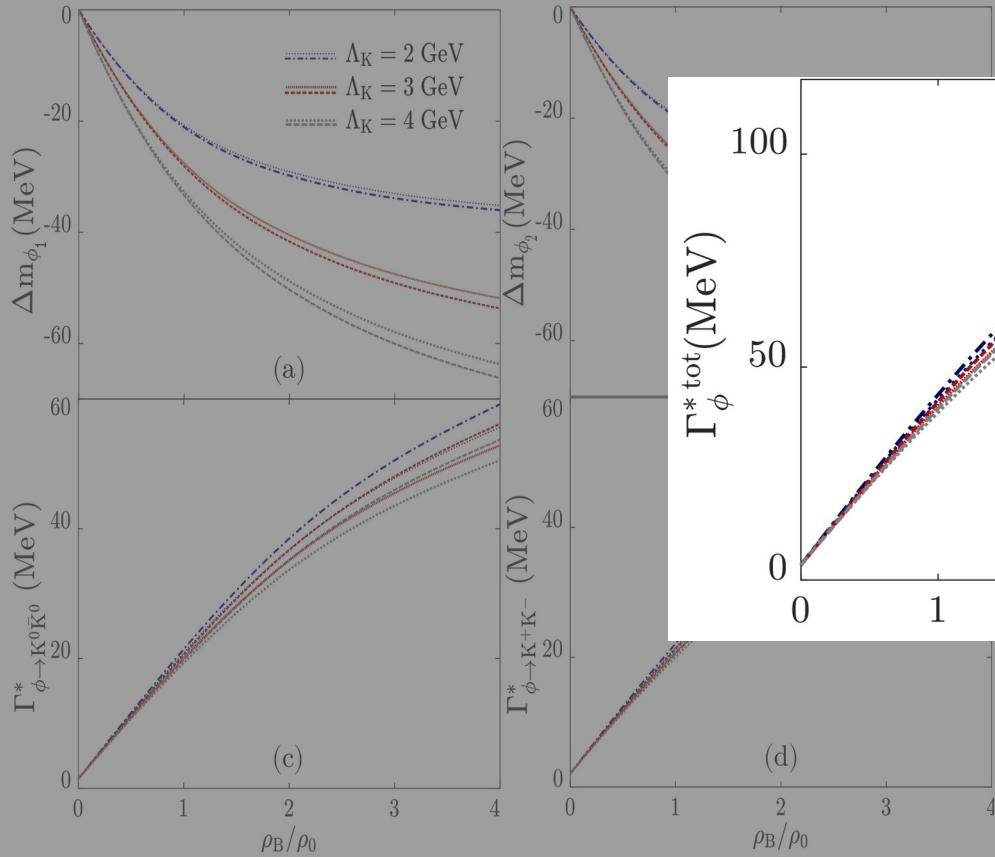
Adjusted with the nuclear matter results at  $r \rightarrow 0$

- for  $\sigma$  field
- for  $\delta^3$  field
- for  $\omega_0$  field
- for  $\rho_0^3$  field
- for Coulomb field

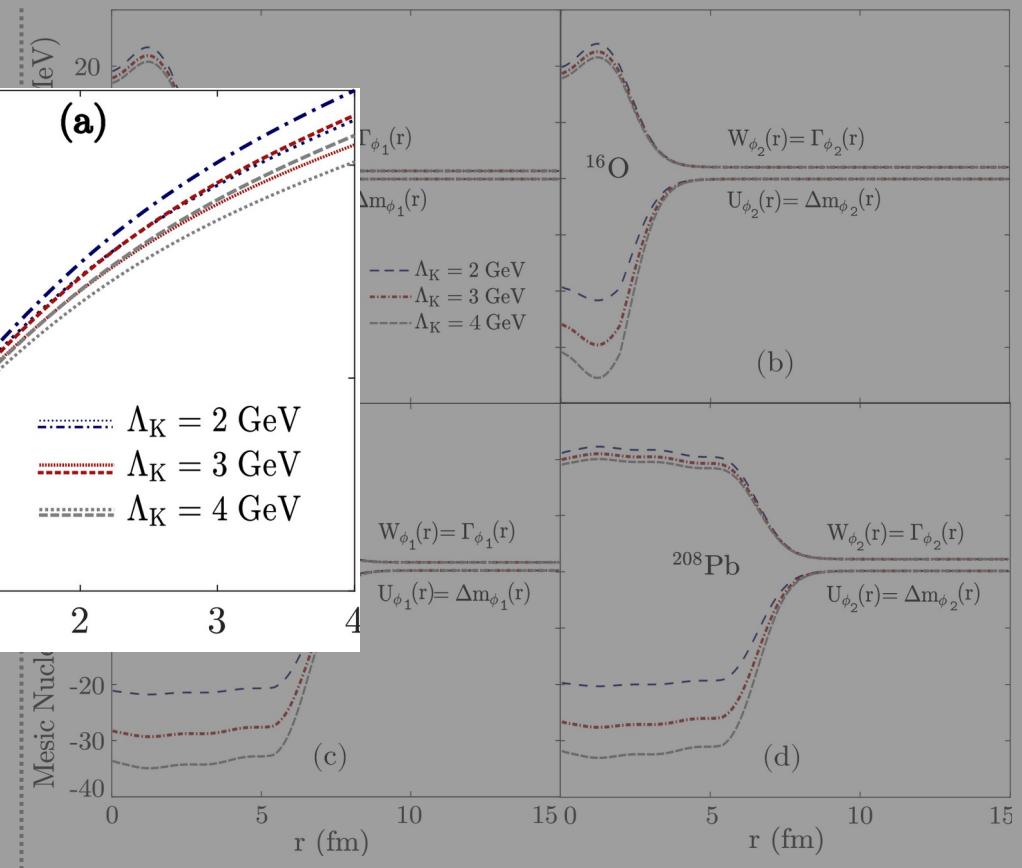
# How phi is introduced to nuclear environment ?

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## Nuclear Matter



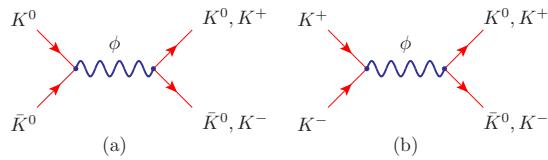
## Finite Nuclei



✓  $V_{\phi_i}(r) = U_{\phi_i}(r) - \frac{i}{2} W_{\phi_i}(r)$

# Phi in nuclear matter

HIN25



- $\sigma_i(K\bar{K} \rightarrow \phi; M^2) = 6\pi^2 \frac{\Gamma_i^*}{|\vec{q}_i|^2} A_{\phi_i}(M^2)$
- $A_{\phi_i}(M^2) = C_i \frac{2}{\pi} \frac{M^2 \Gamma_\phi^{*tot}}{(M^2 - m_{\phi_i}^{*2})^2 (M \Gamma_\phi^{*tot})^2}$
- $\int_0^\infty A_{\phi_i}(M^2) dM = 1$

