Understanding Galactic Dark Matter with Neural Networks



The Frontier of Particle Physics: Exploring Muons, Quantum Science and the Cosmos

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Phenomenology of Dark Matter appears in Various Length Scales!



Particle Physics (small length scale)

Galactic Astrophysics (medium length scale?)

of the second se

Cosmology (large length scale) There are many interesting things but... perhaps, most interested topic in <u>galactic</u> <u>astrophysics</u> to high energy particle physicists is... There are many interesting things but... perhaps, most interested topic in <u>galactic</u> <u>astrophysics</u> to high energy particle physicists is...

about <u>dark matter</u>.

Galaxy rotation curve and dark matter



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Galaxy rotation curve and dark matter



Probably, you heard about the dark matter density on Earth...

How much is the dark matter density at the Solar location?

The local dark matter density at the Solar location (i.e., in the vicinity of the Sun within the Milky Way) is typically estimated to be around:

 $ho_{{
m DM},\odot}pprox 0.3\,{
m GeV/cm}^3$

This value is based on dynamical studies of the Milky Way's rotation curve and stellar kinematics. However, there is some uncertainty, and estimates range from about **0.2 to 0.6 GeV/cm³** depending on the specific model and data used.

Would you observatior



About half-proton in a cubic centimeter box!

Galaxy rotation curve of Milky Way

Ou, et. al., 2303.12838





Figure 4. Comparison between the circular velocity curve measured from Eilers et al. (2019) (black) and this work (red). The best-fit Einasto DM profile, with the baryonic model from de Salas et al. (2019), is also shown here. The grey shaded region represents the bulge region, which we do not model due to the non-axisymmetric potential near the galactic bar. The red shaded region represents the total uncertainty estimate from the dominating systematic sources, as shown in Figure 5.



In galactic dynamics for studying dark matter, one important and interesting task is...

Q: How to use stellar distribution of a galaxy to understand its galactic dark matter density with less assumptions?



https://www.eso.org/public/images/eso1339g/



Mapping Dark Matter in the Milky Way using Normalizing Flows and <u>Gaia DR3</u>

M. R. Buckley, <u>SHL</u>, E. Putney, and D. Shih, arXiv:2205.01129, published in MNRAS <u>SHL</u>, E. Putney, M. R. Buckley, and D. Shih, arXiv:2305.13358, published in JCAP E. Putney, D. Shih, <u>SHL</u>, and M. R. Buckley, arXiv:2412.14236,

Hydrodynamics and Galactic Dynamics

If we consider a galaxy as a hydrodynamic system $N \rightarrow \infty$ consisting of stars, phase-space density of a star (probability of finding a star with given position and velocity) describes the system.



 $f(\vec{x}, \vec{v})$

Equation of motion: Boltzmann Equation





See also Green et. al. arXiv:2011.04673, arXiv:2205.02244

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Normalizing Flows: Neural Network learning a Transformation

Normalizing Flows (NFs) is an artificial neural network that learns a transformation of random variables.



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This formula can be used for training normalizing flows, too: <u>Maximum likelihood estimation</u>

Training Normalizing Flows

$$\mathcal{L}(\theta) = -\frac{1}{N} \sum_{i=1}^{N} \log p_W(\vec{w}^{(i)}; \theta) \qquad p_W(\vec{w}) = p_U(\vec{u}) \cdot \left| \frac{d\vec{u}}{d\vec{w}} \right|$$



Training Normalizing Flows

$$\mathcal{L}(\theta) = -\frac{1}{N} \sum_{i=1}^{N} \log p_W(\vec{w}^{(i)}; \theta) \qquad p_W(\vec{w}) = p_U(\vec{u}) \cdot \left| \frac{d\vec{u}}{d\vec{w}} \right|$$



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Learned transformation



Normalizing Flows: Neural Network learning a Transformation

Normalizing Flows (NFs) is an artificial neural network that learns a transformation of random variables.



Main idea: if we could find out such transformation, we can use the transformation formula for the density estimation:

$$p_W(\vec{w}) = p_U(\vec{u}) \cdot \left| \frac{d\vec{u}}{d\vec{w}} \right|$$

We will use this model for estimating the phase space density f(x,v) from the data. 18 /



See also Green et. al. arXiv:2011.04673, arXiv:2205.02244

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Local DM Mass Density of the Milky Way



 $ho_{\rm DM}(r_{\odot})~(10^{-2}~M_{\odot}/{\rm pc}^3)$

2.0

Blue straggler sc

Nor

Circular

1.5

0.0

This work

Casagrande, (2020) 60

Pato, et al., (2015) 61

Huang, et al., (2016) 62

0.5

1.0

Taking the average of the DM mass density at the Solar radius, we find a local dark matter density: <u>0.47±0.05 GeV/cm³</u> _____



We have an unsupervised ML method to estimate <u>dark matter density</u> given <u>stellar distribution of a galaxy</u>.

END of story?



We have an unsupervised ML method to estimate <u>dark matter density</u> given <u>stellar distribution of a galaxy</u>.

END? \rightarrow Of course not!



Real dirty data analysis Real but clean data analysis

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Galactic Dynamics and Incomplete Datasets



One of main challenge of applying this technique is that the dataset itself is <u>incomplete!</u>

No time derivative information



We only have the current snapshot of the Milky Way!

Radial Velocity Distribution of Gaia DR3



Incompleteness in Spacial Coverage



Intergalactic dust cloud obscuring light from stars!

Dust Clouds



Intergalactic dust cloud obscuring light from stars!

Dust Obscuring Stars





How could we overcome this data <u>incompleteness</u> due to dust clouds (using ML)?

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Intergalactic dust cloud obscuring light from stars!

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Our group's student Eric Putney

Arm



Mapping Dark Matter Through the Dust of the Milky Way Part I: <u>Dust Correction and Phase Space Density</u>

E. Putney, D. Shih, SHL, and M. R. Buckley, arXiv:2412.14236,

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Erasing Dust using Neural Network and Equilibrium Assmptions



Erasing Dust using Neural Network and Equilibrium Assmptions



Intergalactic dust cloud obscuring stars behind!



So far, we have discussed how to deal with dusty environment of the Milky Way.

Milky Way

Q: Are there any dust-free galaxies to make this analysis simple?
Milky Way

Q: Are there any dust-free galaxies to make this analysis simple?



Yes, there are some dust-free satellite galaixes of the Milky Way!

Where are they?

Milky Way

So far, we have been focused on the analysis on <u>our corner</u> of the Milky Way.

If you go further away...



So far, we have been focused on the analysis on <u>our corner</u> of the Milky Way.

If you go further away, you see

whole Milky Way, but it is difficult to get **all the kinematic information** of stars visible here.

No local dark matter density estimate on the **opposite corner**!





So far, we have been focused on the analysis on our corner of the Milky Way. If you go further further away, Milky Way You see other 100 000 ly Ursa Maior I satellite galaxies! Boč Ursa Minor Dwar Draco Dwarf Dwarl a Major I Cloue Carina Dwarf Small Local Group **Fornax Dwarf**

http://www.atlasoftheuniverse.com/sattelit.html

we will focus on a type of satellite galaxy called **dwarf speheroidal galaxy**.



Dwarf Spheroidal Galaxy?

- A round and faint satellite galaxy, orbiting the Milky Way.
- Almost no gas and dust obscuring stars. Whole galaxy is clearly visible.



Fornax Dwarf



Dwarf spheroidal galaxy is a dark matter laboratory!

Clean signal source as dsph exhibits less baryon activity.

Indirect Detection experiments





Understanding the dark matter halo shape → insights on DM interactions?





Navarro-Frenk-White (NFW) profile

A commonly used dark matter halo model empirically identified in N-body simulations

$$\rho(r) = \frac{\rho_0}{\frac{r}{R_s} \left(1 + \frac{r}{R_s}\right)^2}$$

If dark matter exhibits non-trivial interactions, the **halo shape may vary**.



Self-interacting dark matter, wave dark matter

https://en.wikipedia.org/wiki/Navarro%E2%80%93Frenk%E2%80%93White_profile 44 / 70

Example: Wave Dark Matter

If DM mass is so light (e.g. very light axions) so that

inter-particle spacing << de Broglie wavelength

DM exhibits wave-like behavior.



Smoking gun signatures



Fig. from talk by Teodori Luca, IBS Let there be light (particles) Workshop

Need for model-independent analysis



As many non-trivial DM halos are considered nowadays, we need a <u>free-form DM density estimation</u> in order to do a <u>model-indepdent</u> DM halo analysis.

Again, unsupervised machine learning can help solving this type of problem!

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Is the ML technique easily applicable to any of <u>distant dust-free galaxies</u>, <u>like dwarf spheroidal galaxy?</u> <u>Answer: both yes and no</u>





JFlow: Model-Independent Spherical Jeans Analysis using Equivariant Continuous Normalizing Flows

Collaboration with

K. Hayashi (NIT, Sendai College), S. Horigome (Tohoku),

S. Matsumoto (IPMU), M. M. Nojiri (KEK),

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New Paper!

JFlow: Model-Independent Spherical Jeans Analysis using Equivariant Continuous Normalizing Flows

Sung Hak Lim, Kohei Hayashi, Shun'ichi Horigome, Shigeki Matsumoto, Mihoko M. Nojiri

The kinematics of stars in dwarf spheroidal galaxies have been studied to understand the structure of dark matter halos. However, the kinematic information of these stars is often limited to celestial positions and line-of-sight velocities, making full phase space analysis challenging. Conventional methods rely on projected analytic phase space density models with several parameters and infer dark matter halo structures by solving the spherical Jeans equation. In this paper, we introduce an unsupervised machine learning method for solving the spherical Jeans equation in a model-independent way as a first step toward model-independent analysis of dwarf spheroidal galaxies. Using equivariant continuous normalizing flows, we demonstrate that spherically symmetric stellar phase space densities and velocity dispersions can be estimated without model assumptions. As a proof of concept, we apply our method to Gaia challenge datasets for spherical models and measure dark matter mass densities given velocity anisotropy profiles. Our method can identify halo structures accurately, even with a small number of tracer stars.

Comments:9 pages, 3 figures, 1 tableSubjects:Astrophysics of Galaxies (astro-ph.GA); Cosmology and Nongalactic Astrophysics (astro-ph.CO
Physics - Experiment (hep-ex); High Energy Physics - Phenomenology (hep-ph)Report number:CTPU-PTC-25-15Cite as:arXiv:2505.00763 [astro-ph.GA]
(or arXiv:2505.00763v1 [astro-ph.GA] for this version)

https://doi.org/10.48550/arXiv.2505.00763

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Check it out!

Challenges in Analyzing dSphs

- Faint galaxy
 → less number of observed stars O[100] ~ O[1000]
- Available kinematic information is <u>limited</u>!
 - Position of stars on the sky (x, y) (phot.)
 - Distance to the stars (z)
 - Proper motion of stars on the sky (v_x, v_y)
 - Radial velocity (v_z) (spec.)
- Phase space density of stars are not accessible, and hence we cannot solve the equation of motion yet.. (Jeans equation)

$$\frac{\partial n \langle v_j \rangle}{\partial t} + n \frac{\partial \Phi}{\partial x_j} + n \frac{\partial n \langle v_i v_j \rangle}{\partial x_i} = 0$$

Can we recover the full 6D information somehow?

Radon Transformation

- Can we recover the full 6D information somehow?
 - \rightarrow Yes, if we have a 3D projected snapshot of the dSph from all the direction





- This tomographic reconstruction is possible (e.g. MRI imaging),
- but we only have a snapshot from only one direction...
 - \rightarrow Classic solution: assume <u>spherical symmetry</u>.

Spherical Jeans Equation

Introducing spherical symmetry simplifies the Jeans equation, too.

$$\frac{d}{dr}n\overline{v_r^2} + \frac{2\beta}{r}n\overline{v_r^2} = -n\frac{d\Phi}{dr}$$

List of functions needed for inferring gravitational field (Φ)

- Number density n(r)
- Radial velocity dispersion (variance) $\overline{v_r^2}(r)$
- Velocity anisotropy

$$\beta(r) = 1 - \frac{\overline{v_{\theta}^2}(r) + \overline{v_{\phi}^2}(r)}{2\overline{v_r^2}(r)}$$

Note: velocity anisotropy cannot be determined only using line-ofsight velocity distribution, we will provide the function (can be true or not) by hand.

Need to estimate 2 functions from data:

$$n(r) \quad \overline{v_r^2}(r)$$

Normalizing Flows: Neural Density Estimator

Normalizing Flows (NFs) is an artificial neural network that learns a transformation of random variables.





Main idea: if we could find out such transformation, we can use the transformation formula for the density estimation:

$$p_W(\vec{w}) = p_U(\vec{u}) \cdot \left| \frac{d\vec{u}}{d\vec{w}} \right|$$

We will use this model for estimating the phase space density f(x,v) from the data.

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Equivariant Continous Normalizing Flows

How to model spherically symmetric density using normalizing flows? → Use Equivariant Continuous Normalizing Flows!

$$\frac{d\vec{x}}{dt} = \vec{F}(\vec{x}, t) \longrightarrow \frac{d\vec{x}}{dt} = \hat{r}f(\vec{x}, t)$$
- Invariant (Gaussian) base distribution
- Equivariant vector field
$$\int_{0}^{1} \int_{0}^{1} \int_$$

n(r

Normalizing Flows: How it works?



n(r)

* result of a continuous normalizing flow learning infinitesimal transformations

Cored Spherical Density Model

In dSph analysis, we may further constrain the density model as conventional analysis often only consider the following type of densities.

- Cored density (constant density at r << 0)
- Cuspy density

ex) plummer sphere:

Equivariant CNF for modeling cored density profile

$$p(r) = \left(1 + \frac{r^2}{r_0^2}\right)^{-5/2}$$

$$\frac{d\vec{x}}{dt} = \hat{r}f(\vec{x},t) \longrightarrow \frac{d\vec{x}}{dt} = \hat{r} \tanh\left(\frac{|\vec{x}|}{r_0}\right) f(\vec{x},t)$$

Transformation at the origin is suppressed, remaining as Gaussian-shape. \rightarrow cored density n(r

Cuspy Spherical Density Model

In dSph analysis, we may further constrain the density model as conventional analysis often only consider the following type of densities.

- <u>Cored</u> density (constant density at r << 1)
- Cuspy density

Equivariant CNF for modeling cuspy density profile ex

ex) NFW profile:

$$p(r) = \left(\frac{r}{r_0}\right)^{-1} \left(1 + \frac{r}{r_0}\right)^{-2} \to \frac{1}{r}$$

Apply power-law transform to radial component

$$|r| \rightarrow |r|^{c+1}$$
 Jacobian $\propto r^{-\frac{3c}{1+c}}$

to cored spherical symmetric density model

Velocity Dispersion Estimation

The velocity dispersion can be simply estimated using Gaussian model conditioned on position, as the MLE on variance parameter of Gaussian is a variance estimator.

$$\Sigma(r;\theta) = \begin{pmatrix} \overline{v_r^2}(r;\theta) & 0 & 0\\ 0 & \overline{v_\theta^2}(r;\theta) & 0\\ 0 & 0 & \overline{v_\phi^2}(r;\theta) \end{pmatrix}$$

Note that only radial velocity dispersion is modeled by a neural network, others are given by velocity anisotropy function provided.

$$\overline{v_{\theta}^2}(r;\theta) = \overline{v_{\phi}^2}(r;\theta) = \overline{v_{r}^2}(r;\theta) \cdot (1 - \beta(r))$$

Here is a 6D density model, but...

Now we have a full 6D phase-space density model ready for solving spherical Jeans equation.

$$\begin{split} p(\vec{r}) &= n(r;\theta) \quad \text{modeled by equivariant CNF for cuspy halos} \\ p(\vec{v}|\vec{r}) &= \text{GaussPDF}(\vec{v};\mu=0,\Sigma(r;\theta)) \\ f(\vec{r},\vec{v}) &= p(\vec{r}) \times p(\vec{v}|\vec{r}) \end{split}$$

STOP Wait, w How c We ca

Wait, we only have x, y, vz. <u>How can we train</u> this network by MLE? We cannot use a conventional loss function.

How to train this model?



Loss Function for Modeling Dwarf Spheroidal Galaxy

 In order to train the normalizing flow with spherical symmetry using limited kinematic information, we minimize the following entropy:

$$\mathcal{L}(\theta) = \int d\vec{w}_{\perp} \ p * K_h(\vec{w}_{\perp}) \ \log \hat{p} * K_h(\vec{w}_{\perp};\theta)$$

 Importance sampling: N_T training sample (stars) ~ p, N_K noise samples ~ K_h

$$\mathcal{L}(\theta) = \frac{1}{NN_K} \sum_{a=1}^N \sum_{b=1}^{N_K} \log \hat{p} * K_h(\vec{w}_\perp^{(a)} + \vec{\epsilon}^{(b)}; \theta)$$

 KDE for the smeared likelihood model: N_G generated stars from the normalizing flows~ \hat{p}

$$\mathcal{L}(\theta) = \frac{1}{NN_K} \sum_{a=1}^{N} \sum_{b=1}^{N_K} \log \frac{1}{N_G} \sum_{c=1}^{N_G} K_h \left[\vec{w}_{\perp}^{(a)} + \vec{\epsilon}^{(b)} - \vec{T}(\vec{z}^{(c)}; \theta) \right]_{\mathbf{b}}$$

Results: stellar number density & radial velocity dispersion



Results: dark matter mass density



Dataset: simulated dwarf spherodal galaxy from Gaia Challenge Dataset https://astrowiki.surrey.ac.uk/doku.php?id=tests:sphtri 64 / 70

Conclusions

- We introduce a model-independent and unbinned spherical Jeans analysis using **normalizing flows**, a neural density estimator utilizing transformation of random variables.
- We <u>invented a loss function</u> for training normalizing flows modeling dSphs only using projected information, <u>without performing Abel</u> <u>transformation</u>.
- Using a mock spherical galaxy from Gaia Challenge dataset, we demonstrated that normalizing flows are capable of estimating <u>phase-</u> <u>space density</u> information for required solving Jeans equation.
- To do?:
 - Generalizing the framework to axisymmetric system.
 - Applying our analysis to real dwarf spheroidal galaxies, and estimate the effect to J-factors when the assumptions are relaxed.



Awesome collaborators of my projects:





Prof. David Shih Prof. Matthew Buckley (Rutgers) (Rutgers)



Eric Putney (Ph.D. student at Rutgers)





Prof. Mihoko Nojiri Prof. Kohei Hayashi (KEK) (NIT, Sendai College)



Prof. Shigeki Matsumoto (IPMU)



Dr. Shunichi Horigom<u>e</u> (Tohoku)67 / 70

Buliding a regional community:

AI+HEP in East Asia

About Organizers Workshops Seminars Journal Clubs Curriculum Project Board

Organizers

- Tianji Cai
- Sung Hak Lim
- Vinicius Mikuni
- Huilin Qu

AI+HEP in East Asia

AI+HEP in East Asia



Page under construction :)

AI WANTSYOU TO CONTRIBUTE

Thank you for listening!



Backups

Various challenging incompleteness!

Disequilibrium



Intergalactic Dust



Spatial Incompleteness



Lack of information



Only 3D info. available, not the full 6D PS info.

More challenges are waiting!

How we infer mass density? → Gravity!


Stellar Streams and Machine Learning

Nibauer, Belokurov, Cranmer, Goodman, Ho, arXiv:2205.11767



Preliminary: Dust Correction

Boltzmann equation also provides us an alternative way of measuring intergalactic dust clouds.



Preliminary: Dust Correction

Boltzmann equation also provides us an alternative way of measuring intergalactic dust clouds.



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Credit: Eric Putney (Rutgers)

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Preliminary: Dust Correction

Boltzmann equation also provides us an alternative way of measuring intergalactic dus $d = 3.25 \, \text{kpc}$ $f_{\text{obs}}(\vec{x}, \vec{v})$



Credit: Eric Putney (Rutgers)

Magic Dust Eraser

-15

-30

180.0

135.0

90.0

Boltzmann equati intergalactic dus

 $\left[\vec{v}\cdot\frac{\partial}{\partial\vec{x}} + \vec{a}\cdot\frac{\partial}{\partial\vec{\imath}}\right]$



45.0

0.0

l (deg)

315.0

270.0

Work in progress!

225.0

180.0

-3.5

-4.0

Milky Way vs. Distant Galaxy



(+) Stars are closer, we can observe full kinematics in high precision.(-) Stars with full kinematics info. are limited to nearby stars.



Milky Way vs. Distant Galaxy



(+) Stars are closer, we can observe full kinematics in high precision.(-) Stars with full kinematics info. are limited to nearby stars. (+) Whole galaxy is visible(-) Only limited kinematic information is available:

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- position on the sky
- radial velocity

Example: Stellar Distribution and Merger History of the Milky Way



Example: Stellar Distribution and Merger History of the Milky Way

