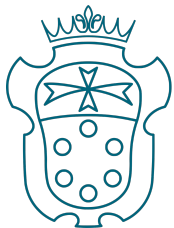


Boostless Cosmological Collider Bootstrap ~ of Tensor Bispectra ~

Carlos Duaso Pueyo

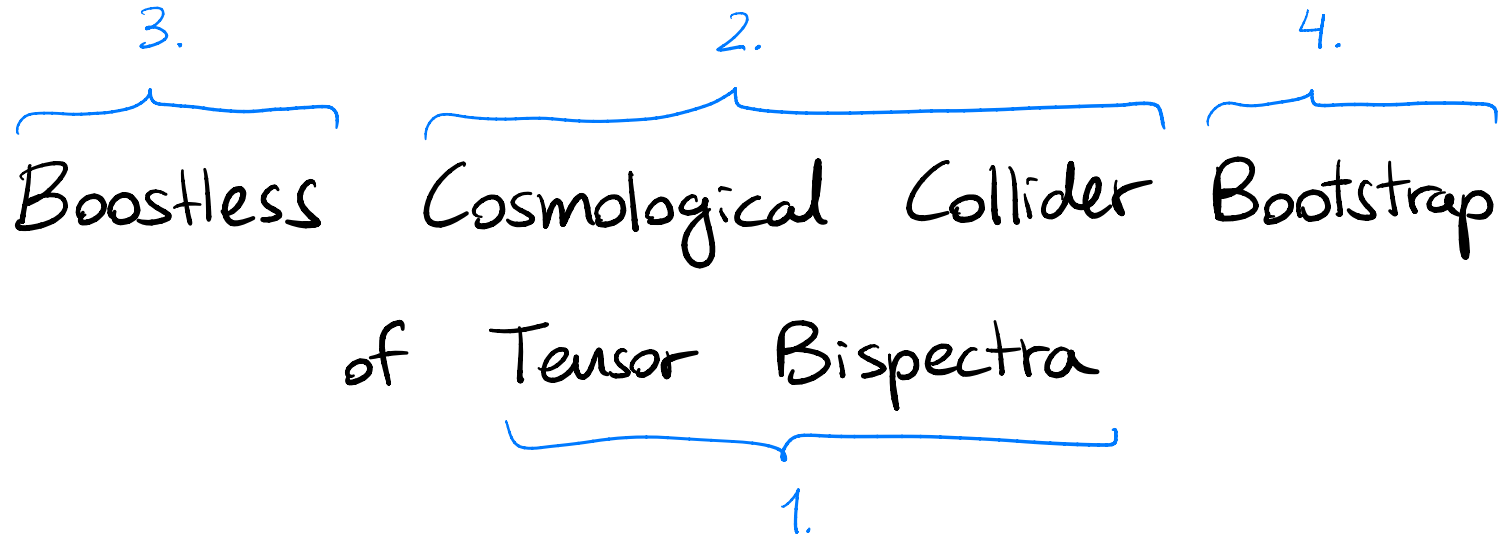
W.I.P. with Kaiyuan Fan, Xin-Chen He
& Dong-Gang Wang



SCUOLA
NORMALE
SUPERIORE

YITP
Nov 2025

Outline



5. Some results

6. Conclusions


Outline

3.  Boostless

2.  Cosmological Collider

4.  Bootstrap

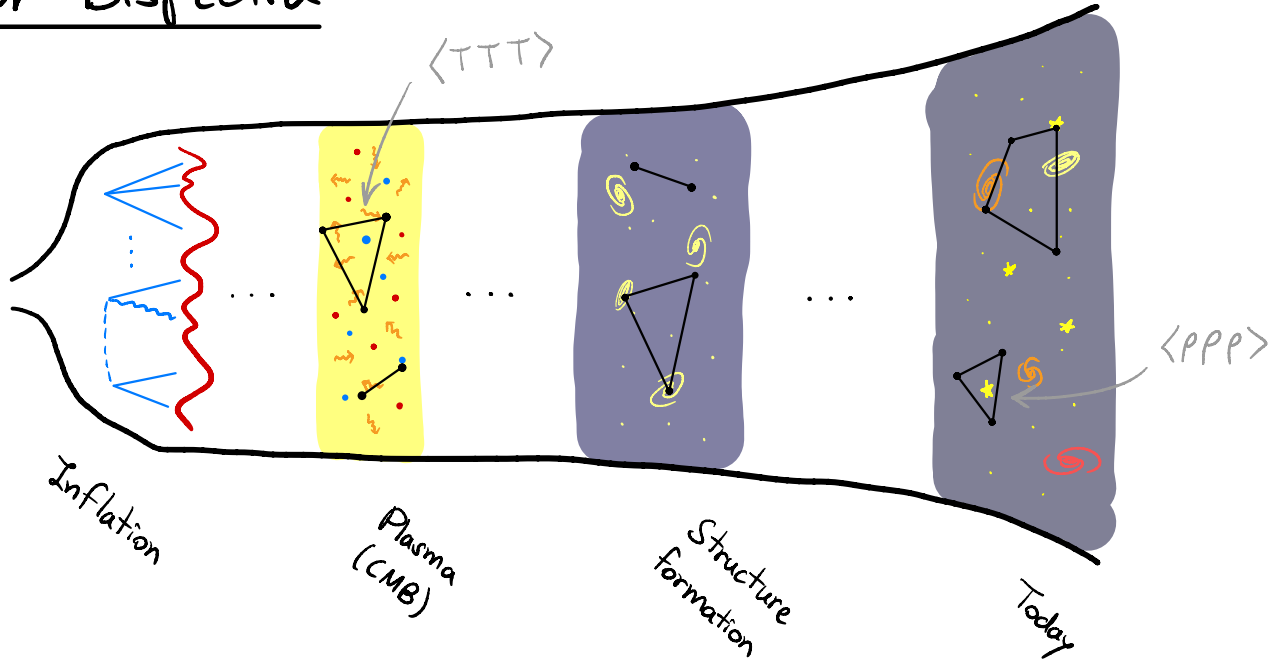
of Tensor Bispectra

 1.

5. Some results

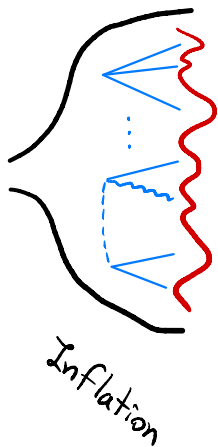
6. Conclusions

Tensor Bispectra



The **primordial perturbations** generated during inflation seeded the late time structure

Tensor Bispectra



Primordial perturbations...

... can be scalar (ζ) or tensor (χ_{ij})

... are small:

$$\Delta_{\zeta}^2 \sim 10^{-9}$$

Planck '23

$$\Delta_{\chi}^2 \lesssim 0.03 \Delta_{\zeta}^2$$

BICEP/Keck '18

3-pt. functions (bispectra) encode the dynamics

$$\langle \zeta \zeta \zeta \rangle$$

$$\langle \chi \zeta \zeta \rangle$$

$$\langle \chi \chi \zeta \rangle$$

$$\langle \chi \chi \chi \rangle$$

Tensor
bispectra

Tensor Bispectra

Current constraints from CMB:

Model		T+E+B
<i>Tensor-Tensor-Tensor</i>		
Squeezed	($\times 10^{-1}$)	4 ± 8
Equilateral	($\times 10^{-2}$)	-0 ± 3
W^3 ($n_{NL} = +1$)	($\times 10^{-3}$)	6 ± 4
W^3 ($n_{NL} = 0$)	($\times 10^{-2}$)	4 ± 4
W^3 ($n_{NL} = -1$)	($\times 10^0$)	3 ± 15
$\tilde{W}W^2$ ($n_{NL} = +1$)	($\times 10^{-3}$)	-4 ± 7
$\tilde{W}W^2$ ($n_{NL} = 0$)	($\times 10^{-2}$)	-2 ± 5
$\tilde{W}W^2$ ($n_{NL} = -1$)	($\times 10^0$)	5 ± 17
$\tilde{F}F$	($\times 10^{-2}$)	3 ± 6
<i>Tensor-Tensor-Scalar</i>		
$\tilde{W}W$	($\times 10^{-2}$)	6 ± 10
<i>Tensor-Scalar-Scalar</i>		
Squeezed	($\times 10^0$)	11 ± 11

- Future improvements:

$$\sigma \left(\int_{\text{NL}}^{\chi\chi\chi} \right) \sim \mathcal{O}(0.1-1)$$

$$\sigma \left(\int_{\text{NL}}^{\chi\chi\chi} \right) \sim \mathcal{O}(10)$$

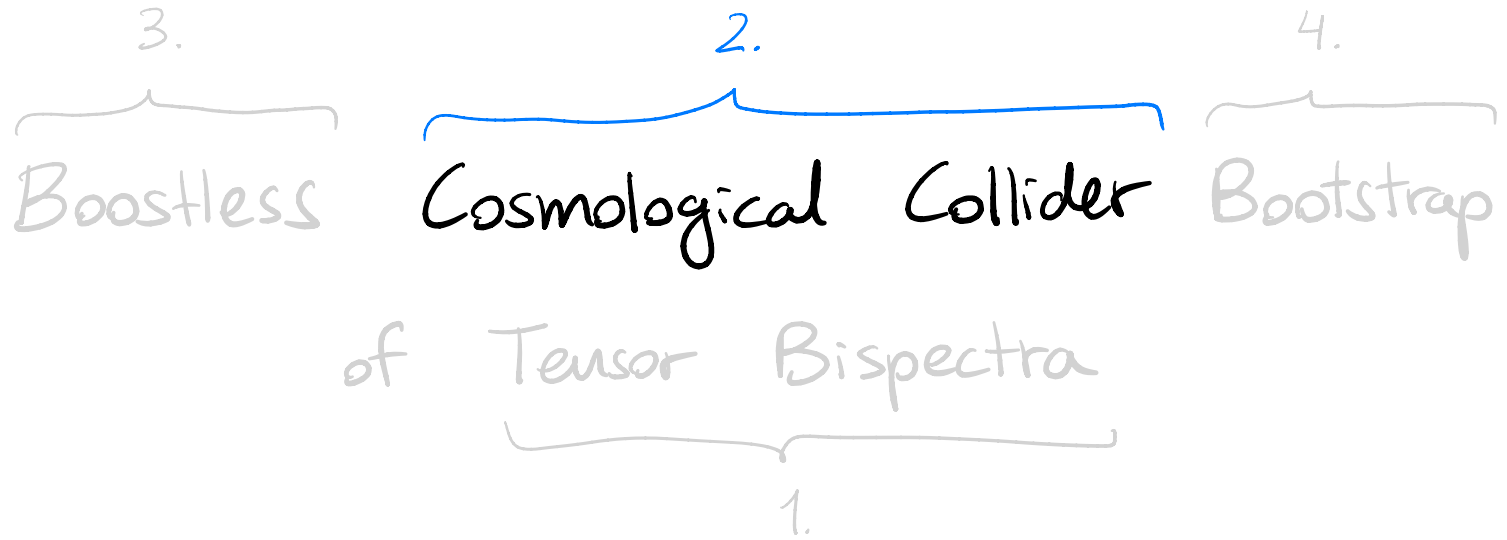
$$\sigma \left(\int_{\text{NL}}^{\chi\chi\chi} \right) \sim \mathcal{O}(1)$$

LiteBird
CMB-S4

- Only 11 models have been constrained, many more to explore!

Philcox, Shiraishi '24

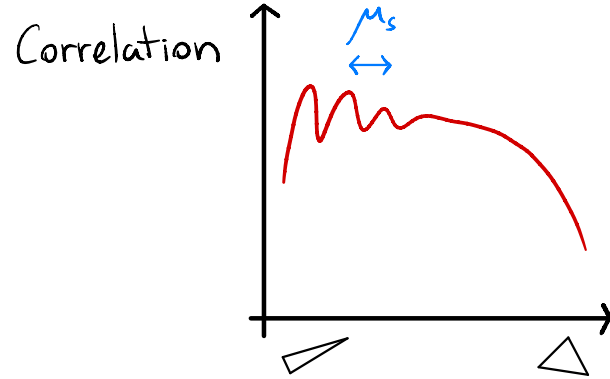
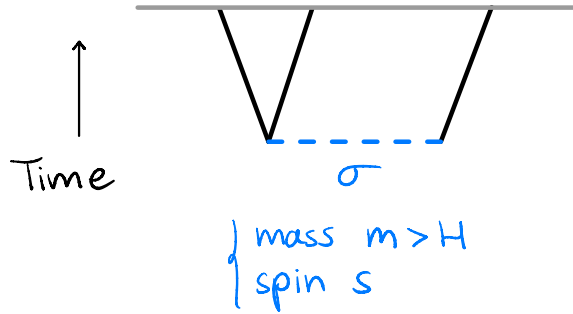
Outline



5. Some results

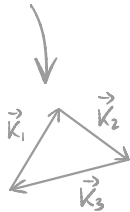
6. Conclusions

Cosmological collider



$$\langle \rho_{\vec{k}_1} \rho_{\vec{k}_2} \rho_{\vec{k}_3} \rangle \xrightarrow[k_3 \ll k_1 = k_2]{\text{Squeezed limit}} P_s(\hat{k}_1, \hat{k}_3) \cdot \left(\frac{k_3}{k_1}\right)^{3/2} \cdot \cos \left[\mu_s \cdot \log \left(\frac{k_3}{k_1}\right) + \text{ph.} \right]$$

Mom. conservation

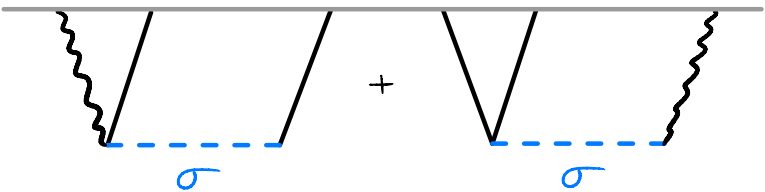


$$\mu_s \equiv \sqrt{\frac{m^2}{H^2} - \left(s - \frac{1}{2}\right)^2}$$

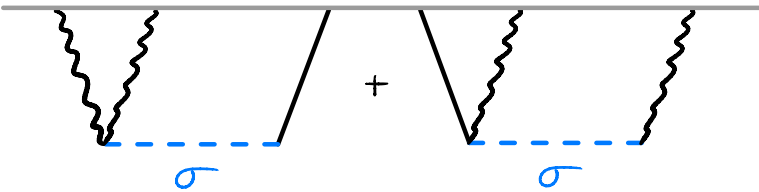
- Arkani-Hamed, Maldacena '15
- Baumann, Lee, Pimentel '16
- Pimentel, Wang '22
- Jazayeri, Renaux-Petel '22

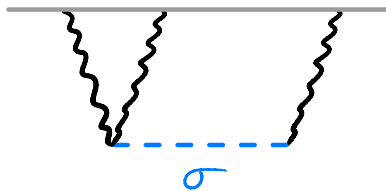
Cosmological collider tensor bispectra

We want to compute:

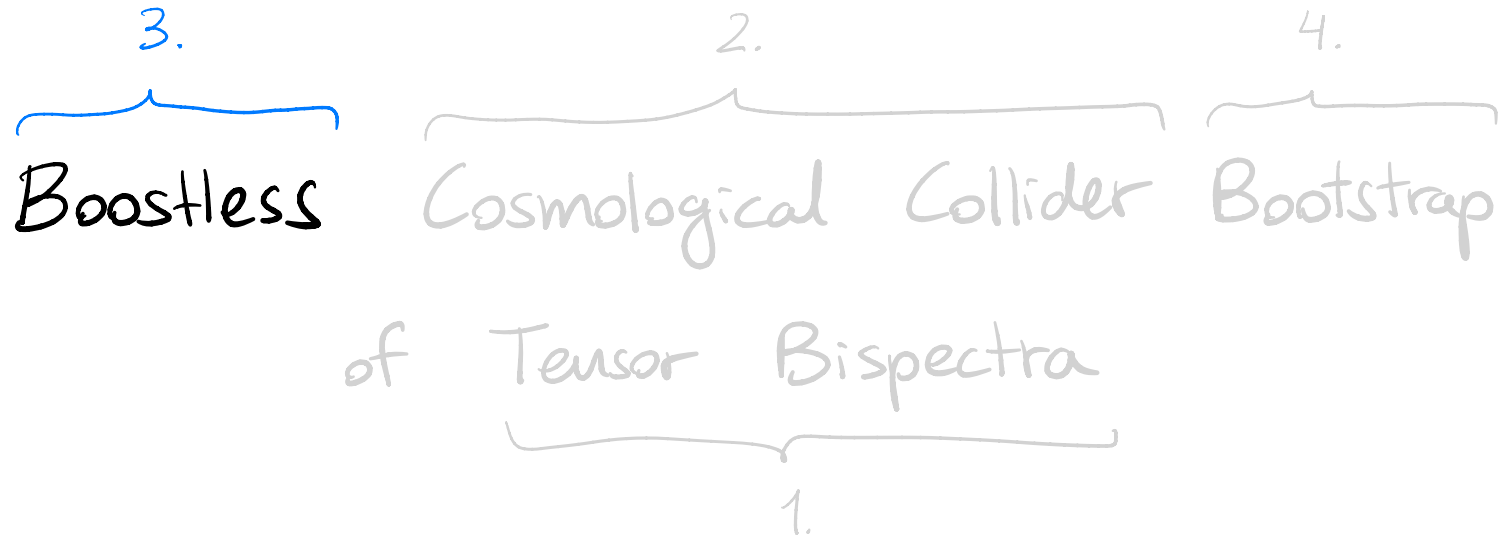
$$\langle \chi \rho \rho \rangle =$$


Baumann, Lee, Pimentel '16
(squeezed limit)

$$\langle \chi \chi \rho \rangle =$$


$$\langle \chi \chi \chi \rangle =$$


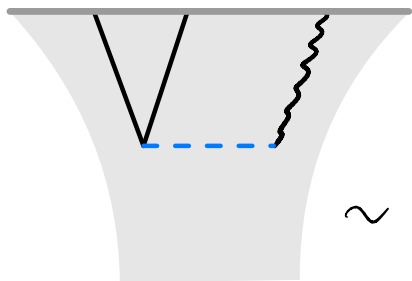
Outline



5. Some results

6. Conclusions

Boostless



\sim de Sitter

dS isometries

Spatial translations

Spatial rotations

Dilatation

~~dS boosts~~

} Observed

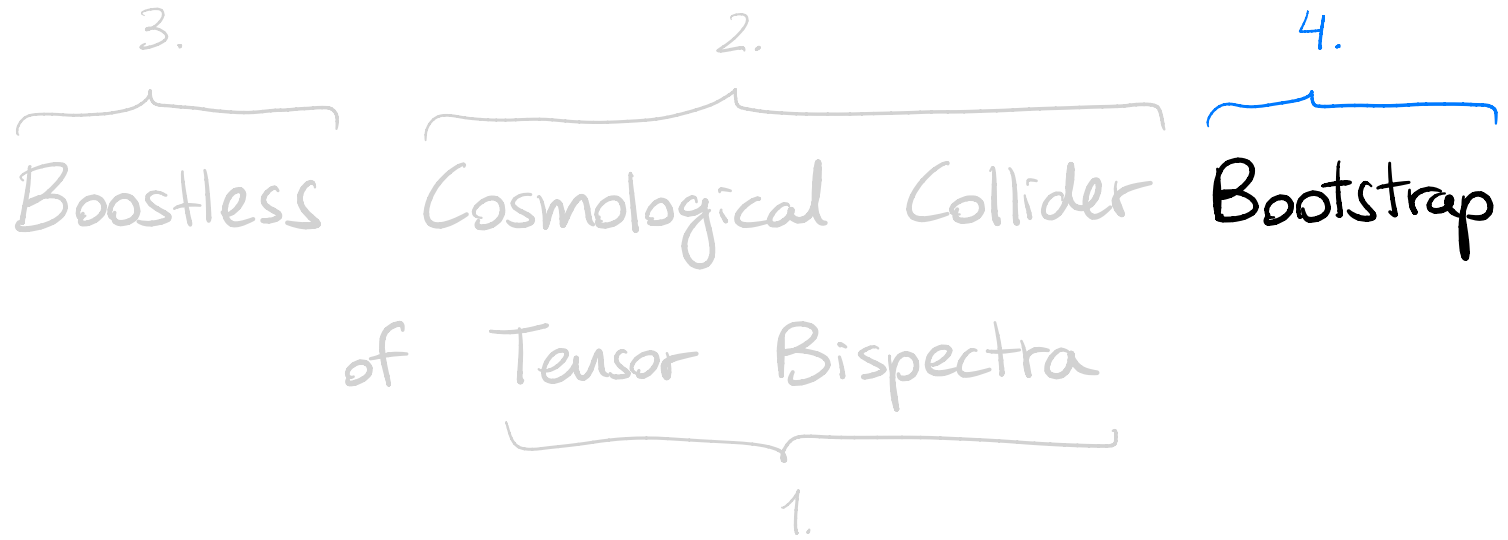
- Free theory: dS mode functions with sound speed $0 < c_s \leq 1$, $c_\sigma \leq 1$, $c_\chi = 1$ (w.l.o.g.)

- Interactions: We use the **EFT of inflation** framework

$$\mathcal{L}(\pi, \chi_{ij}, \sigma^{\mu_1 \dots \mu_s}) \subset \pi \partial_i \pi \sigma_i, \dot{\chi}_{ij} \sigma_{ij}, \dots$$

Cheung et al. '07

Outline



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Bootstrap

Start from a basic "seed" correlator of scalars:

$$\hat{\mathcal{I}}(k_1, k_2, k_3) =$$

ϕ : Conformally coupled scalar

It obeys a boundary diff. eq.:

$$\left[\Delta_u + \left(\mathcal{M}^2 + \frac{1}{4} \right) \right] \hat{\mathcal{I}}(u) = i \frac{u}{1+u}$$

with

$$\begin{cases} \Delta_u = u^2(1-u^2)\partial_u^2 - 2u^3\partial_u \\ u = \frac{k_3}{k_1+k_2} \\ \mathcal{M} = \sqrt{\frac{m^2}{H^2} - \frac{9}{4}} \end{cases}$$

Pimentel, Wang '22

Bootstrap

$$\left[\Delta_u + \left(\mu^2 + \frac{1}{4} \right) \right] \hat{I}(u) = i \frac{u}{1+u}$$

$$\text{with } \begin{cases} \Delta_u = u^2(1-u^2) \partial_u^2 - 2u^3 \partial_u \\ u = \frac{k_3}{k_1 + k_2} \\ \mu = \sqrt{\frac{m^2}{H^2} - \frac{9}{4}} \end{cases}$$

Analytical solution:

$$\hat{I}(u) = \underbrace{i \sum_{n=0}^{\infty} C_n \cdot u^{n+1}}_{\text{Particular sol. (EFT)}} - \underbrace{\frac{i}{2} \sum_{\pm} C_{\pm} \left(\frac{iu}{2\mu} \right)^{\frac{1}{2} \pm i\mu} \cdot {}_2F_1 \left[\frac{1}{4} \pm \frac{i\mu}{2}, \frac{3}{4} \pm \frac{i\mu}{2}; 1 \pm i\mu; u^2 \right]}_{\text{Homogeneous sol. (Particle production)}}$$

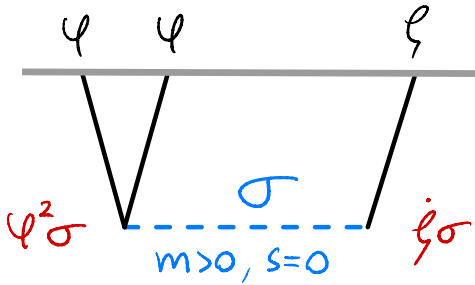
Boundary cond.: match the bulk integral in the squeezed limit



Fixes C_{\pm}

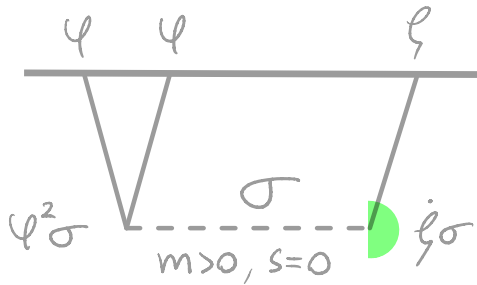
Bootstrap

Then use momentum differential ops. to get tensor bispectra,
e.g. $\langle \chi \xi \xi \rangle$:

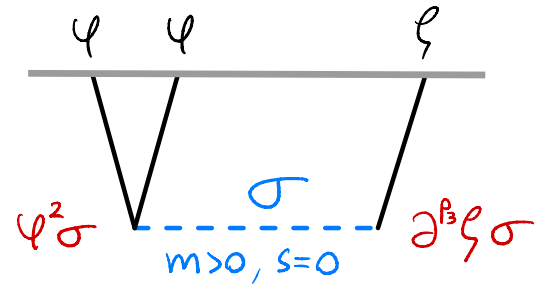


Bootstrap

Then use momentum differential ops. to get tensor bispectra,
e.g. $\langle \chi \zeta \zeta \rangle$:

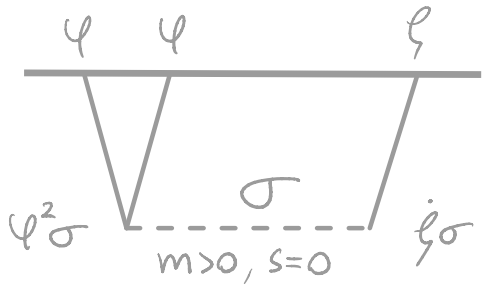


Generalised
 \implies
seed

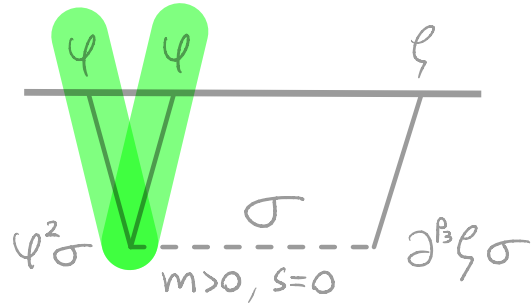


Bootstrap

Then use momentum differential ops. to get tensor bispectra,
e.g. $\langle \chi \xi \xi \rangle$:

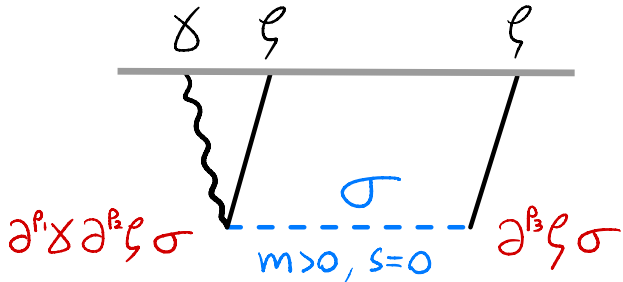


\Rightarrow



Weight

\Leftarrow
shifting

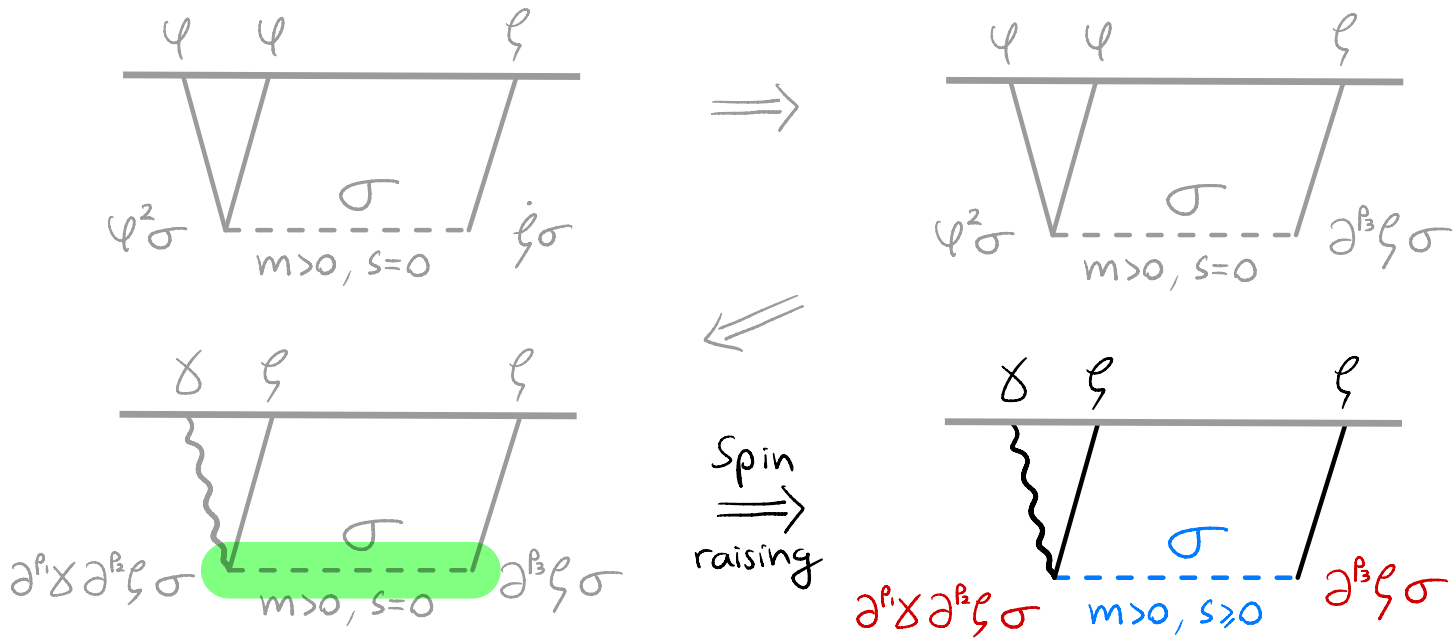


Simple example:

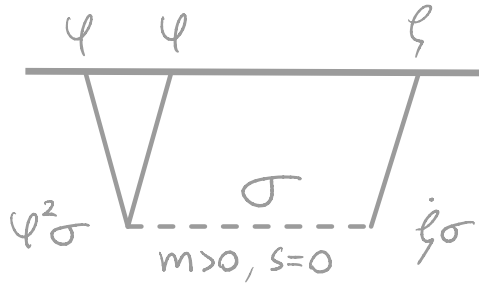
$$\partial_t^p \hat{K}_\xi(\vec{k}, \eta) = \underbrace{K^{p-1} (1 - p - k \partial_k)}_{\text{Diff. op.}} \hat{K}_\psi(\vec{k}, \eta)$$

Bootstrap

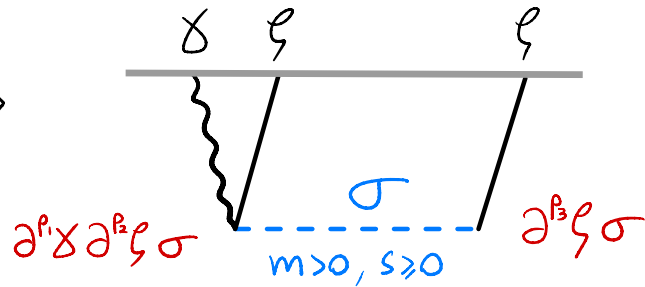
Then use momentum differential ops. to get tensor bispectra,
e.g. $\langle \chi \zeta \zeta \rangle$:



Bootstrap



\Rightarrow



Polarization struc.

Weight shifting

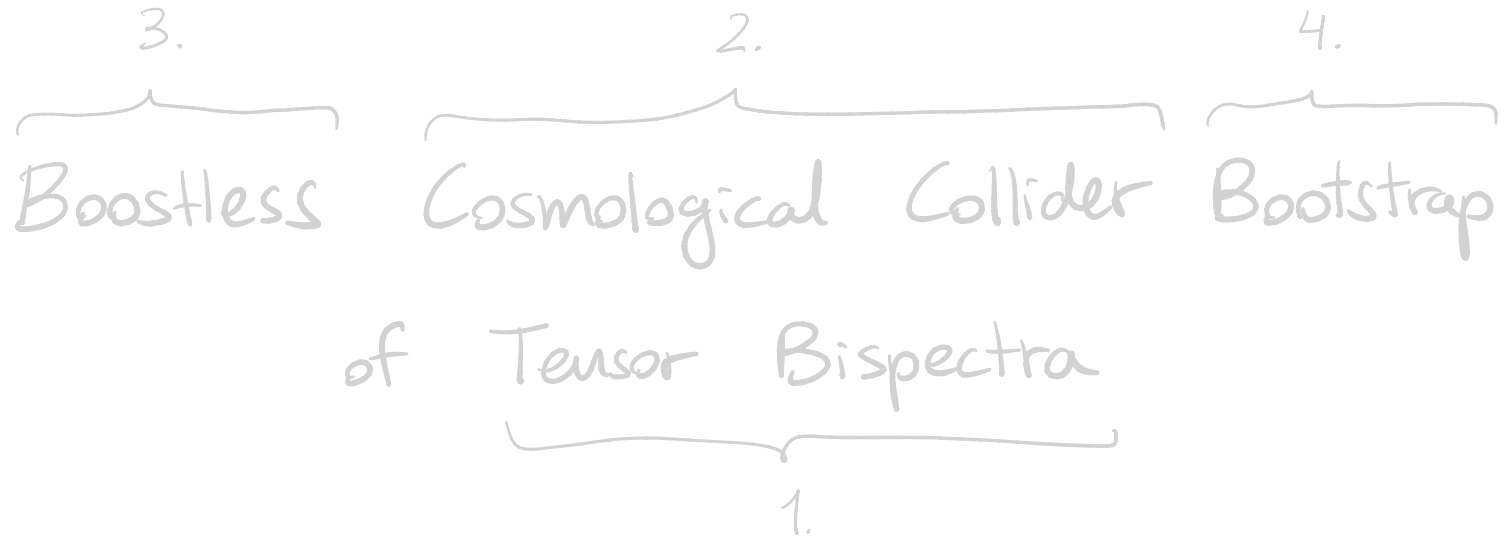
$$\langle \delta_{\vec{k}_1}^\lambda \psi_{\vec{k}_2} \psi_{\vec{k}_3} \rangle = \mathcal{E}^\lambda(\hat{k}_1 \cdot \hat{k}_3) \cdot U_s \cdot W \cdot \hat{I}^{(n)}(u)$$

Spin raising

Generalised seed

... and similarly for $\langle \delta \delta \psi \rangle$ & $\langle \delta \delta \delta \rangle$

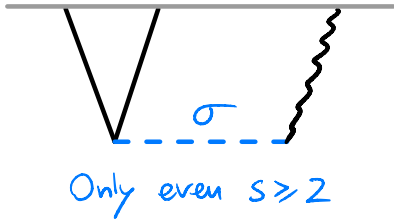
Outline



5. Some results

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Some results



Spin 2 observable if:

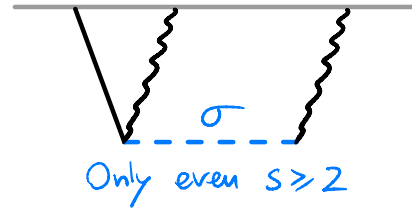
- $m \lesssim \text{few} \times H$
 - $c_g \lesssim 0.4$
 - $r \gtrsim 0.01$
- (assuming $c_\sigma \approx 1$)

$$\lim_{k_3 \ll k_1 = k_2} \langle \hat{e}_{\vec{k}_1} \hat{e}_{\vec{k}_2} \delta_{\vec{k}_3}^\lambda \rangle_{\text{n.l.}} \sim P_S^\lambda(\hat{k}_1, \hat{k}_3) \cdot \left(\frac{k_3}{k_1}\right)^{3/2} \cdot \cos \left[\mu_s \cdot \log \left(\frac{k_3}{k_1}\right) + \text{ph.} \right]$$

$$\lim_{k_3 \ll k_1 = k_2} \langle \hat{e}_{\vec{k}_1} \hat{e}_{\vec{k}_2} \delta_{\vec{k}_3}^\lambda \rangle_1 \sim P_S^\lambda(\hat{k}_1, \hat{k}_3) \cdot \left(\frac{k_3}{k_1}\right)^S$$

Coincides with [Baumann, Lee, Pimentel '16](#), but now we have the full solution!

Some results



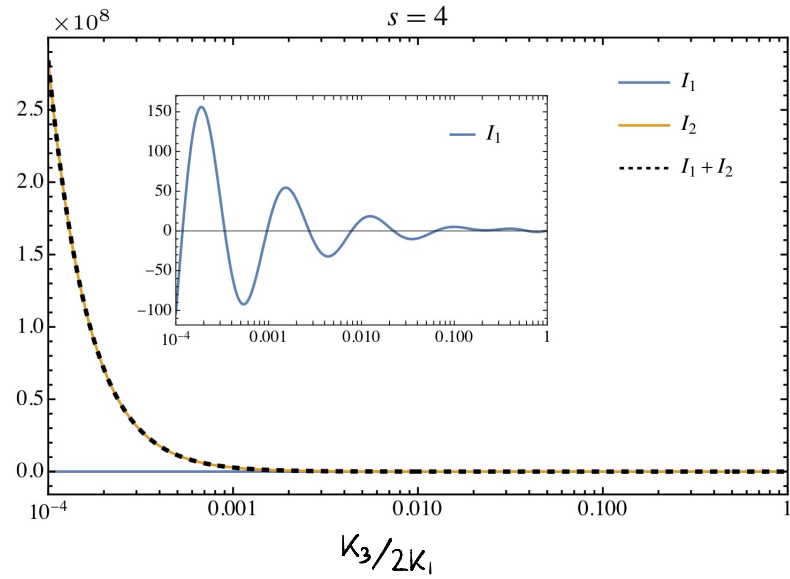
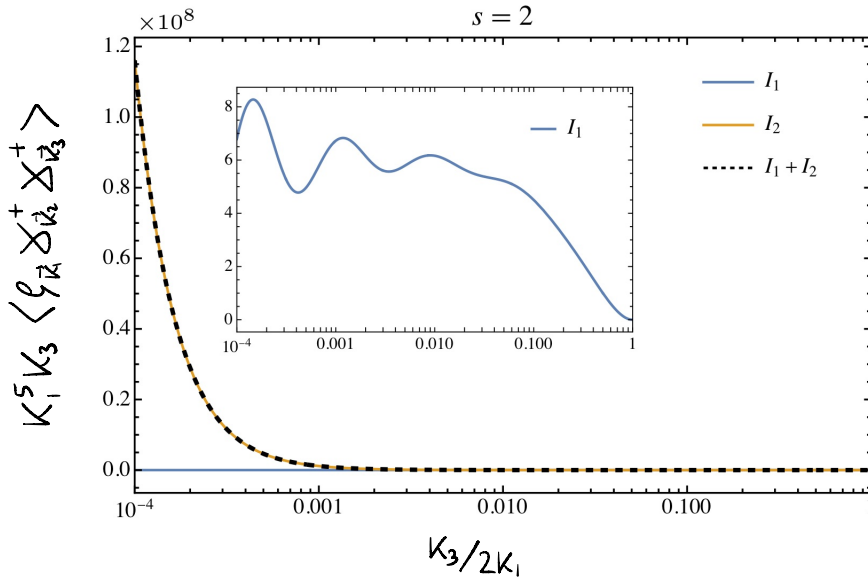
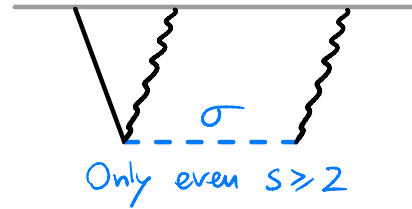
$$\lim_{K_3 \ll K_1 = K_2} \langle e_{\vec{K}_1}^{\lambda_1} \delta_{\vec{K}_2}^{\lambda_2} \delta_{\vec{K}_3}^{\lambda_3} \rangle_{n.l.} \sim \mathcal{E}_s^{\lambda_2 \lambda_3}(\hat{K}_1, \hat{K}_3) \cdot \left(\frac{K_3}{K_1}\right)^{3/2} \cdot \cos \left[\mu_s \cdot \log \left(\frac{K_3}{K_1}\right) + \text{ph.} \right]$$

$$\lim_{K_3 \ll K_1 = K_2} \langle e_{\vec{K}_1}^{\lambda_1} \delta_{\vec{K}_2}^{\lambda_2} \delta_{\vec{K}_3}^{\lambda_3} \rangle_1 \sim \mathcal{E}_s^{\lambda_2 \lambda_3}(\hat{K}_1, \hat{K}_3) \cdot \left(\frac{K_3}{K_1}\right)^0 \leftarrow \text{Dominates!}$$

The oscillations are not visible, the EFT part dominates

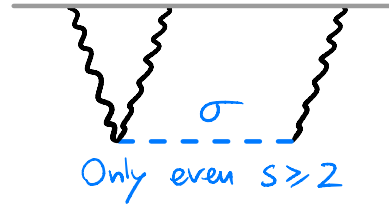
Some results

$\left\{ \begin{array}{l} I_1 = \text{non-local part} \\ I_2 = \text{local part} \end{array} \right.$



The oscillations are not visible, the EFT part dominates

Some results

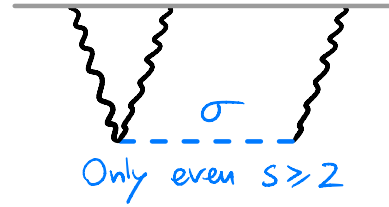


$$\lim_{K_3 \ll K_1 = K_2} \langle \delta_{\vec{k}_1}^{\lambda_1} \delta_{\vec{k}_2}^{\lambda_2} \delta_{\vec{k}_3}^{\lambda_3} \rangle_{n.l.} \sim Q_s^{\lambda_1 \lambda_2 \lambda_3}(\vec{k}_1, \vec{k}_2, \vec{k}_3) \cdot \left(\frac{K_3}{K_1}\right)^{3/2} \cdot \cos \left[\mu_s \cdot \log \left(\frac{K_3}{K_1}\right) + \text{ph.} \right]$$

$$\lim_{K_3 \ll K_1 = K_2} \langle \delta_{\vec{k}_1}^{\lambda_1} \delta_{\vec{k}_2}^{\lambda_2} \delta_{\vec{k}_3}^{\lambda_3} \rangle_1 \sim Q_s^{\lambda_1 \lambda_2 \lambda_3}(\vec{k}_1, \vec{k}_2, \vec{k}_3) \cdot \left(\frac{K_3}{K_1}\right)^0$$

Extra momentum dependence

Some results



$$\lim_{K_3 \ll K_1 = K_2} \langle \delta_{\vec{K}_1}^{\lambda_1} \delta_{\vec{K}_2}^{\lambda_2} \delta_{\vec{K}_3}^{\lambda_3} \rangle_{n.l.} \sim Q_s^{\lambda_1 \lambda_2 \lambda_3}(\vec{K}_1, \vec{K}_2, \vec{K}_3) \cdot \left(\frac{K_3}{K_1}\right)^{3/2} \cdot \cos \left[\mu_s \cdot \log \left(\frac{K_3}{K_1} \right) + \text{ph.} \right]$$

$$\lim_{K_3 \ll K_1 = K_2} \langle \delta_{\vec{K}_1}^{\lambda_1} \delta_{\vec{K}_2}^{\lambda_2} \delta_{\vec{K}_3}^{\lambda_3} \rangle_1 \sim Q_s^{\lambda_1 \lambda_2 \lambda_3}(\vec{K}_1, \vec{K}_2, \vec{K}_3) \cdot \left(\frac{K_3}{K_1}\right)^0$$

The oscillations are not visible in some helicity configurations:

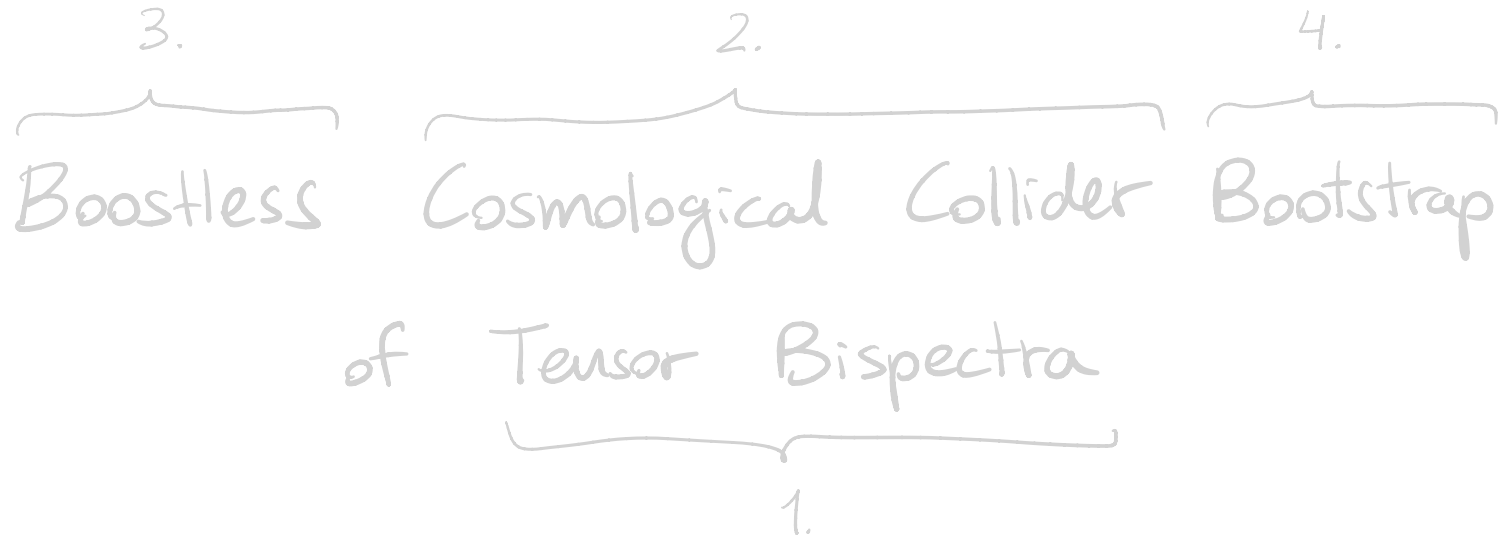
$s=2$

+++	-++	+ - +	++-
✓	✗	✗	✗

$s \geq 4$

+++	-++	+ - +	++-
✓	✓	✗	✗

Outline



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Conclusions

- We bootstrap the **cosmological collider** contributions to $\langle \chi\chi\chi \rangle$, $\langle \chi\chi\chi \rangle$, $\langle \chi\chi\chi \rangle$,
- ... coming from exchange of **massive spinning** fields
- ... with non-trivial **sound speeds** and **boost-breaking** interactions
- We start from simple scalar seeds and build **weight- & spin-shifting operators** that act on them
- The c.c. signal from $h=2$ exchange is **not visible** for $\langle \chi\chi\chi \rangle$ and some helicity choices of $\langle \chi\chi\chi \rangle$
- Other diagrams, f_{NL} estimates, angular and sound-speed dependence **soon!**

Thank you!