

重陽子- π -散乱における πNN 三体バリオン力の効果



Gen Uratsu (M2)
at the Helm



Target

2-baryon force + 3-baryon force + ...

Terra incognita

Main message

ΞNN 3BFs:
Derived from SU(3) chiral EFT

Correlation functions:
Very limited sensitivity to 3BFs

Elastic cross sections:
Possibly visible 3BF effect

Uratsu +, PRC 113, 015204 (2026)

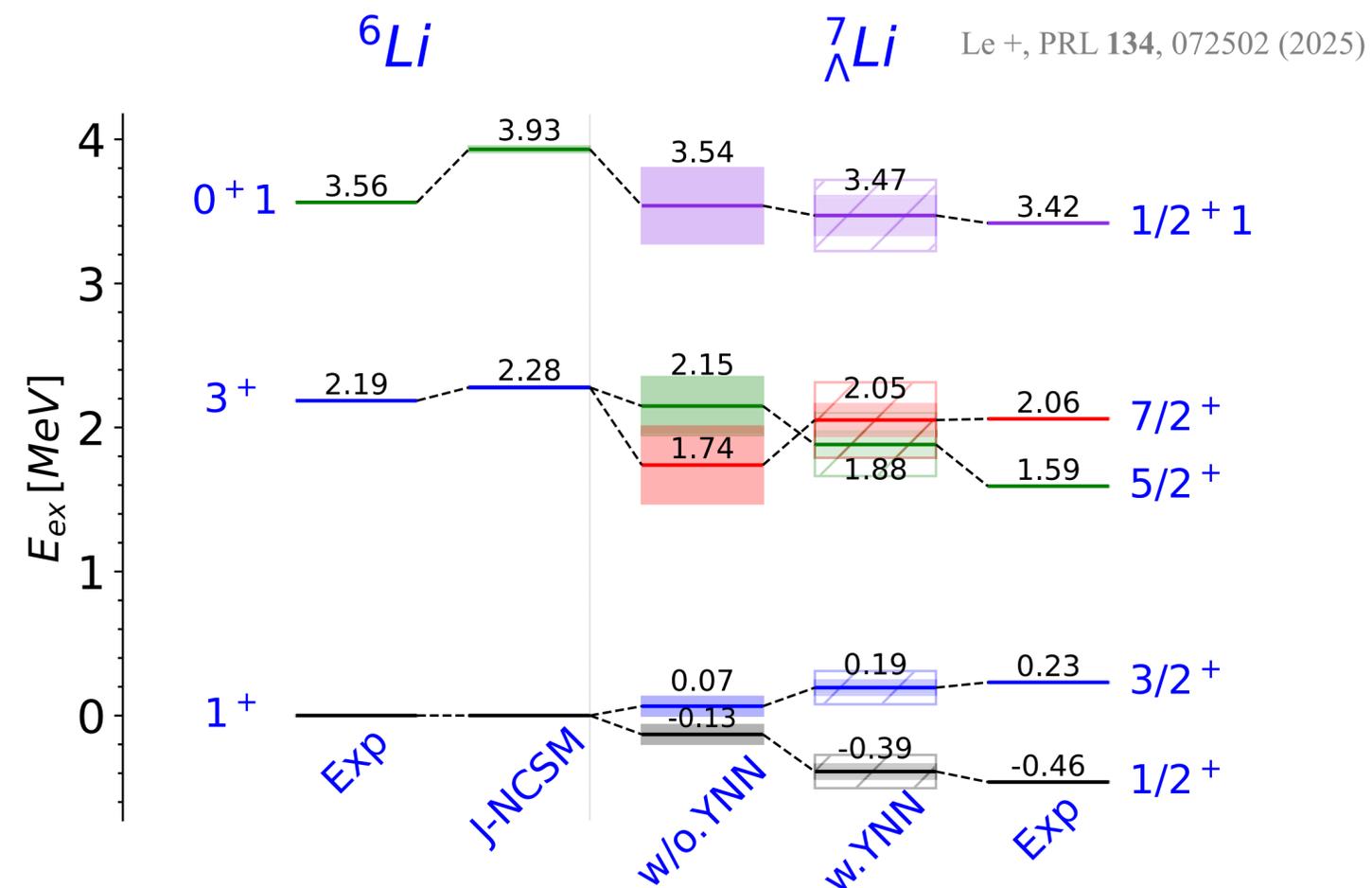
Benchmark calculations

Le +, EPJA **61**, 21 (2025)

		w/o Λ NN	w. 2π -ex Λ NN	w. 1π -ex Λ NN	w. ct Λ NN	Exp. [52]
NCSM	${}^3_{\Lambda}\text{H}$	0.080 ± 0.006	0.153 ± 0.004	0.121 ± 0.005	0.076 ± 0.007	0.164 ± 0.043
FY		0.087	0.152	0.129	0.080	
NCSM	${}^4_{\Lambda}\text{He}(0^+)$	1.432 ± 0.010	1.810 ± 0.006	1.619 ± 0.007	1.400 ± 0.010	2.347 ± 0.036
	${}^4_{\Lambda}\text{He}(1^+)$	1.164 ± 0.014	1.744 ± 0.007	1.427 ± 0.009	1.117 ± 0.016	0.942 ± 0.036
	${}^5_{\Lambda}\text{He}$	3.174 ± 0.020	4.618 ± 0.011	3.757 ± 0.034	2.961 ± 0.031	3.102 ± 0.030

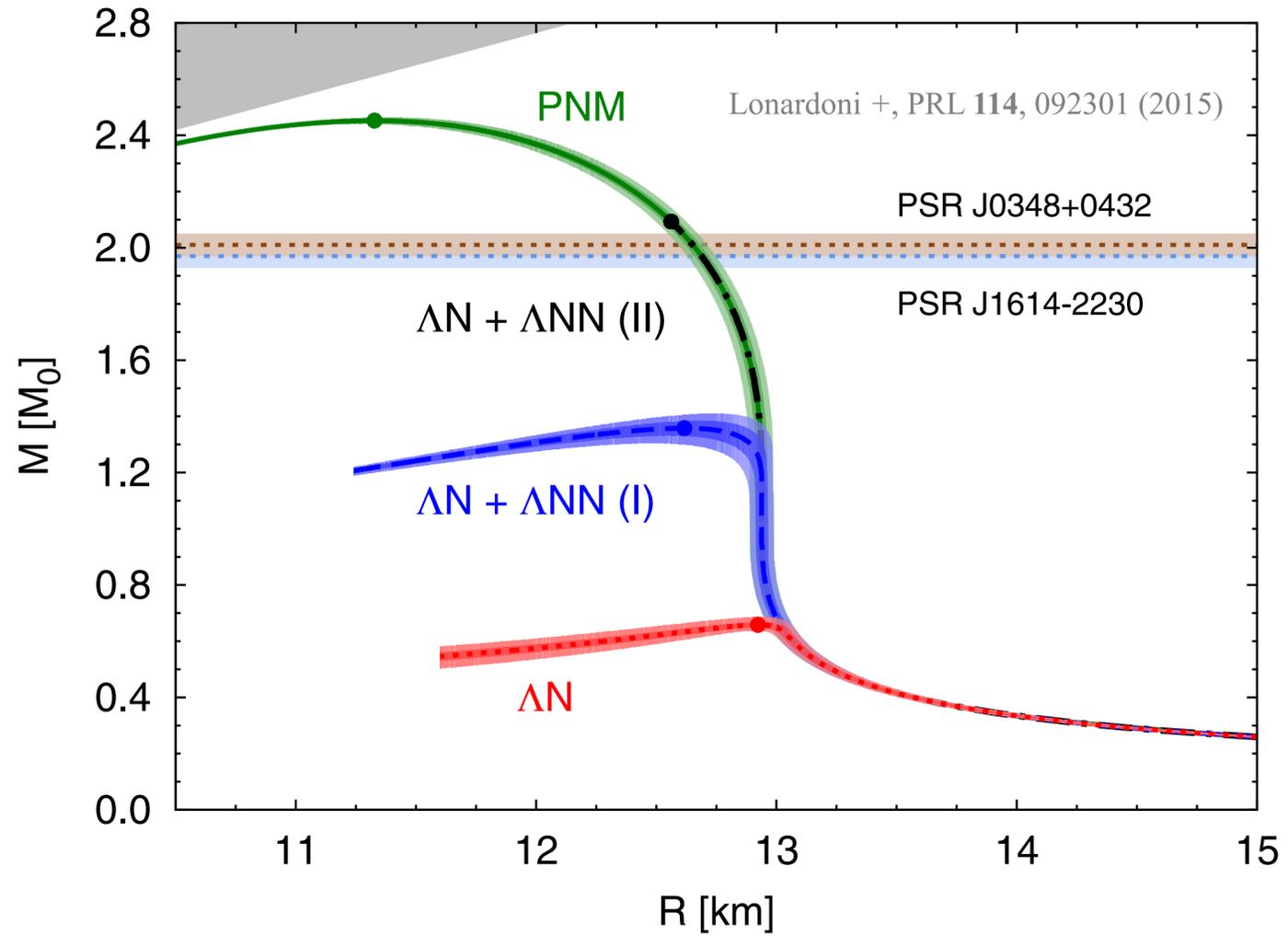
- Sizable 3BF effect
- Λ NN 3BFs from chiral EFT

No-core shell model

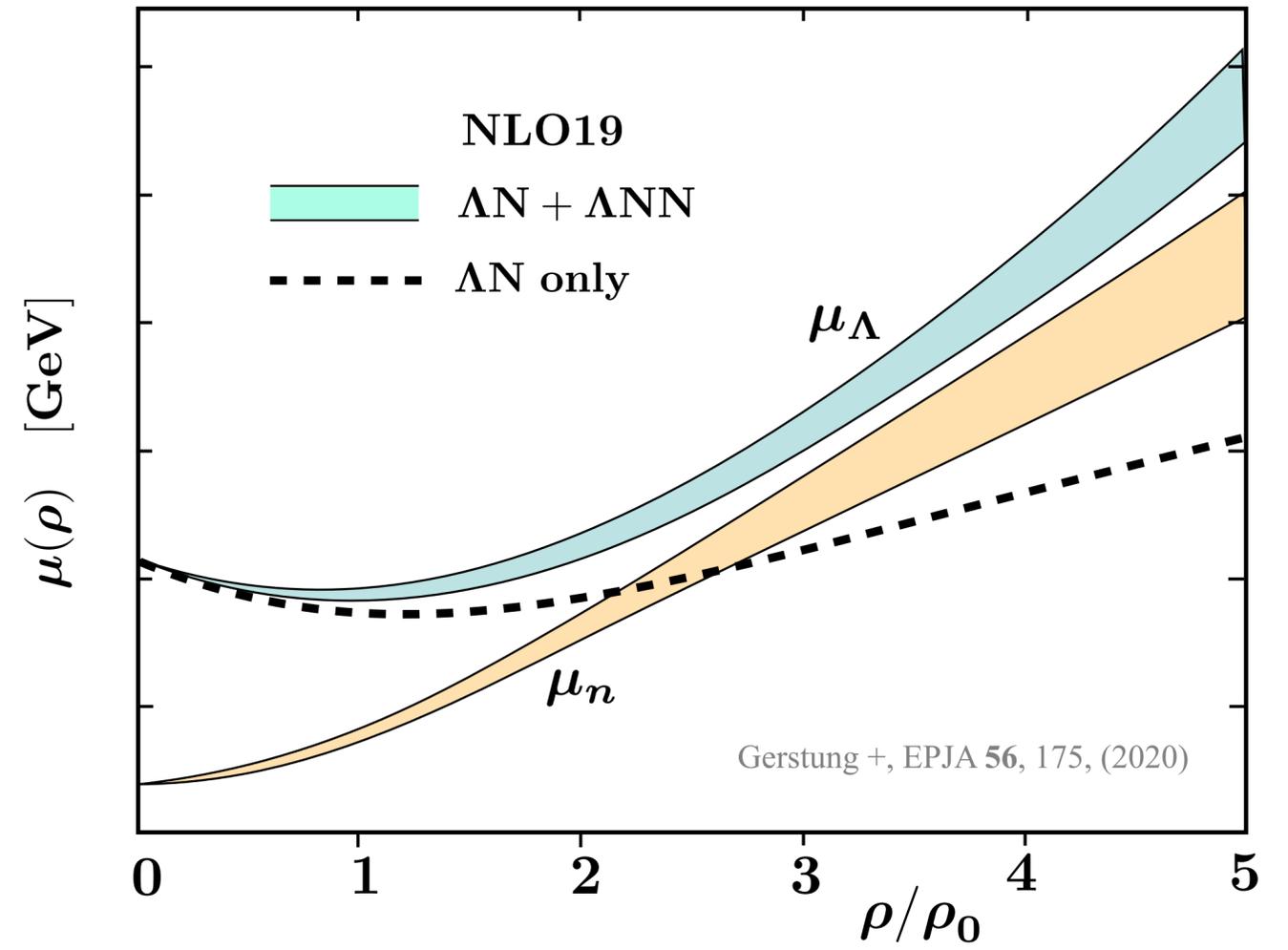


- Necessary for spectroscopy

Neutron star



Neutron matter chemical pot.

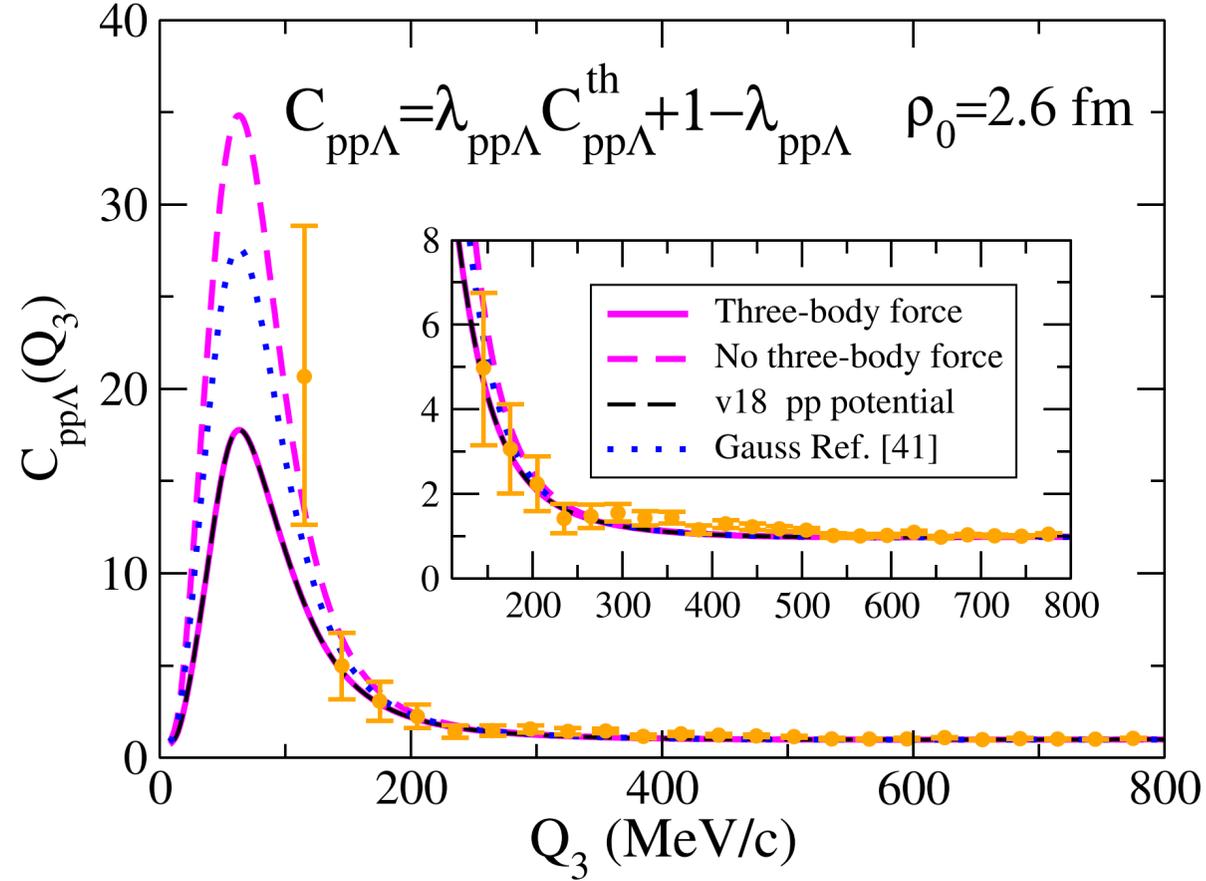


- ▶ Necessary for 2-solar mass
- ▶ ΛNN 3BF:
 - 2π exchange + phenomenological short-range term
- ▶ Related lattice study with pionless EFT

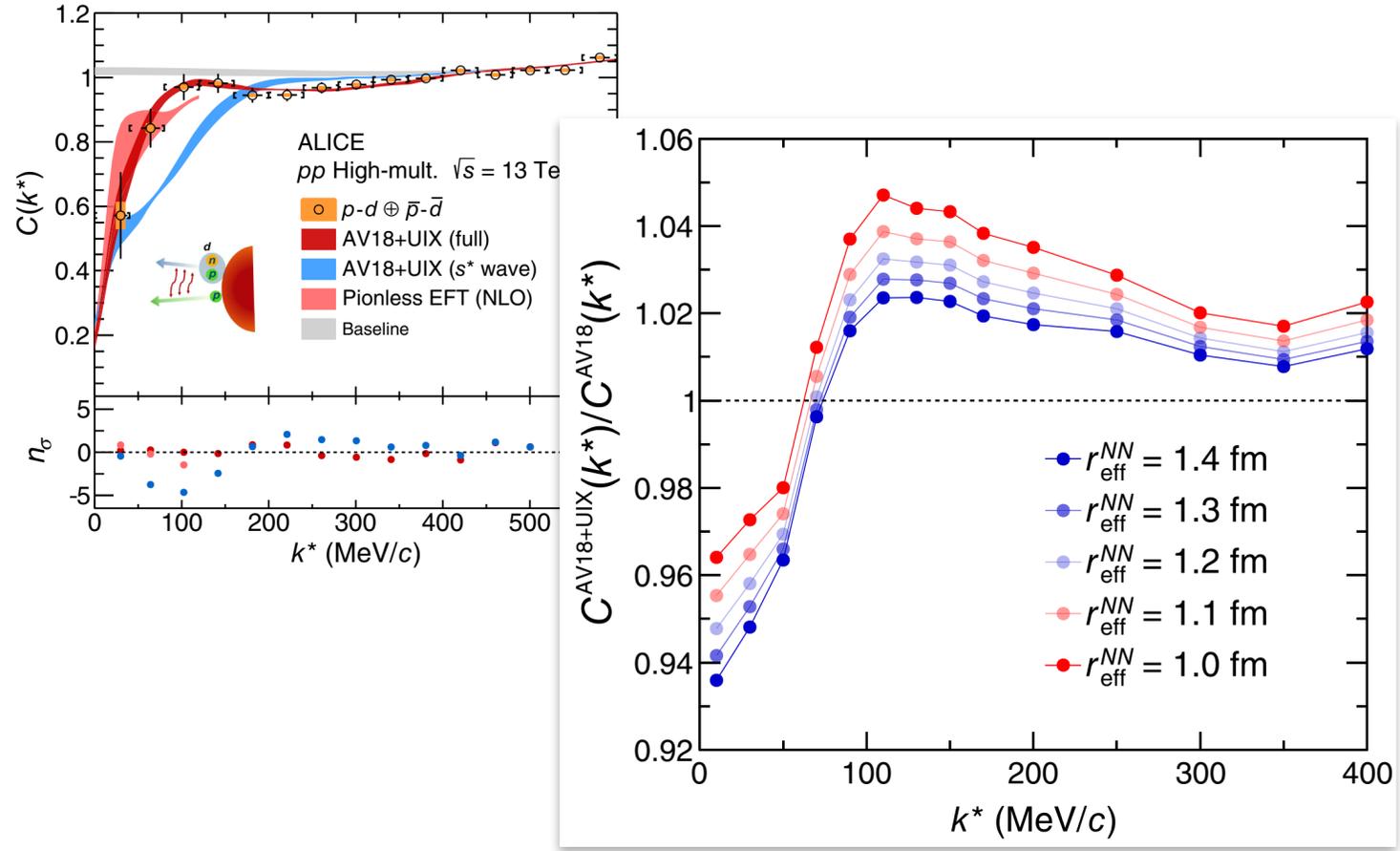
- ▶ Modify saturation point
- ▶ ΛNN 3BF from chiral EFT

Tong +, SB 70, 825 (2025)
 Tong +, AJ 982, 164 (2025)

Comparison with ALICE data



Garrido +, PRC 110, 054004 (2024)



Acharya +, PRX 14, 031051 (2024)

- Possibly significant ΛNN 3BF effect
- Phenomenological Gaussian 3BF

- Small 3NF effect

What about ΞNN 3BFs?

No studies on
3BFs w/ $S = -2$

Prediction by Gaussian-expansion method

Hiyama +, PRL **124**, 092501 (2020)

(T, J^π)	$NN\Xi$	
	$(\frac{1}{2}, \frac{1}{2}^+)$	$(\frac{1}{2}, \frac{3}{2}^+)$
ESC08c	...	7.20
HAL QCD

Prediction by Faddeev approach

Miyagawa & Kohno, FBS **62**, 65 (2021).

- ▶ Jülich-chiral-EFT 2BF and HAL-QCD 2BF
→ No bound states
- ▶ ESC08c
→ $E_{BE} = 3.05$ MeV ($T = 1/2, J^\pi = 2/3^+$)

Related studies

Garcilazo +, PRL **110**, 012503 (2013)
 Garcilazo +, JPG **41**, 095103 (2014)
 Garcilazo +, JPG **42**, 025103 (2015)
 Garcilazo +, PRC **93**, 034001 (2016)
 Filikhina +, MMG **5**, 1 (2017)
 Egorov, PAN **86**, 277 (2023)
 Garcilazo +, PRC **93**, 024001 (2016)
 Garcilazo & Valcarce, CPC **44**, 104104 (2020)
 Carr +, PRC **57**, 2858 (1998)
 Miyagawa +, NPA **614**, 535 (1997)
 Glöckle & Miyagawa, FBS **30**, 241 (2001)

Prediction by Gaussian-expansion method

Hiyama +, PRL 124, 092501 (2020)

	NNE	
(T, J^π)	$(\frac{1}{2}, \frac{1}{2}^+)$	$(\frac{1}{2}, \frac{3}{2}^+)$
ESC08c	...	7.20
HAL QCD

No ENN 3BFs included

Prediction by Faddeev approach Miyagawa & Kohno, FBS 62, 65 (2021).

- ▶ Jülich-chiral-EFT 2BF and HAL-QCD 2BF
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- ▶ ESC08c
→ $E_{BE} = 3.05 \text{ MeV}$ ($T = 1/2, J^\pi = 2/3^+$)

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PHYSICAL REVIEW C **93**, 014001 (2016)

Leading three-baryon forces from SU(3) chiral effective field theory

Stefan Petschauer,^{1,*} Norbert Kaiser,¹ Johann Haidenbauer,² Ulf-G. Meißner,^{2,3} and Wolfram Weise^{1,4}

¹*Physik Department, Technische Universität München, D-85747 Garching, Germany*

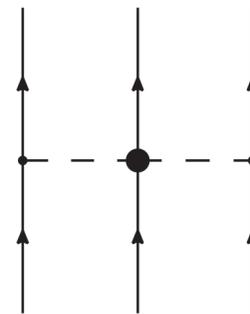
²*Institute for Advanced Simulation and Jülich Center for Hadron Physics, Institut für Kernphysik, Forschungszentrum Jülich, D-52425 Jülich, Germany*

³*Helmholtz-Institut für Strahlen- und Kernphysik and Bethe Center for Theoretical Physics, Universität Bonn, D-53115 Bonn, Germany*

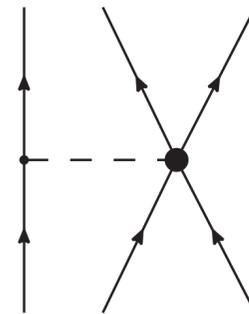
⁴*ECT*, Villa Tambosi, 38123 Villazzano (Trento), Italy*

(Received 6 November 2015; published 11 January 2016)

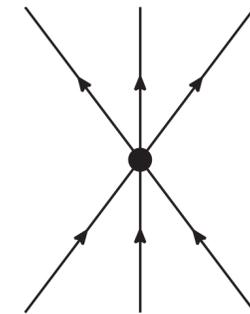
► 3BFs of any combinations of three octet baryons (N , Λ , Σ , Ξ)



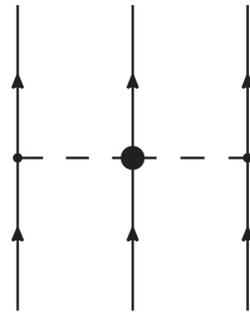
2-meson exchange



1-meson exchange

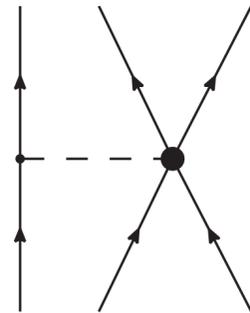


Contacts



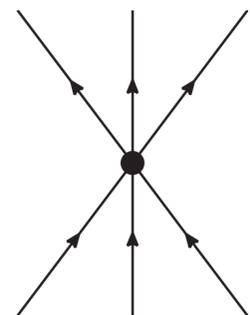
2π exchange

$$V_{\text{TPE}}^{NNN} = \frac{g_A^2}{8f_\pi^2} \mathcal{A} \sum_{i \neq j \neq k} \frac{\vec{\sigma}_i \cdot \vec{q}_i \vec{\sigma}_j \cdot \vec{q}_j}{(\vec{q}_i^2 + m_\pi^2)(\vec{q}_j^2 + m_\pi^2)} \times \left[\frac{\delta^{\alpha\beta}}{f_\pi^2} (-4c_1 m_\pi^2 + 2c_3 \vec{q}_i \cdot \vec{q}_j) + \sum_\gamma \frac{c_4}{f_\pi^2} \epsilon^{\alpha\beta\gamma} \tau_k^\gamma \vec{\sigma}_k \cdot (\vec{q}_i \times \vec{q}_j) \right] \tau_i^\alpha \tau_j^\beta$$



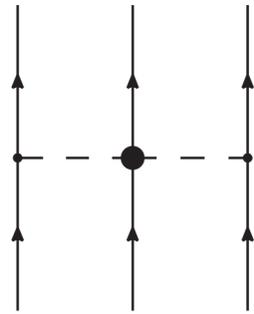
1π exchange

$$V_{\text{OPE}}^{NNN} = -\frac{g_A}{8f_\pi^2} d' \mathcal{A} \sum_{i \neq j \neq k} \frac{\vec{\sigma}_j \cdot \vec{q}_j}{\vec{q}_j^2 + m_\pi^2} \vec{\tau}_i \cdot \vec{\tau}_j \vec{\sigma}_i \cdot \vec{q}_j$$



Contacts

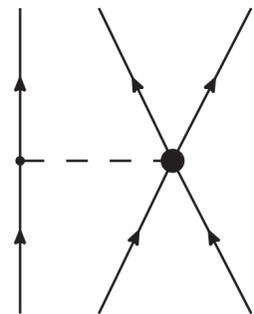
$$V_{\text{ct}}^{NNN} = \frac{1}{2} E \mathcal{A} \sum_{j \neq k} \vec{\tau}_j \cdot \vec{\tau}_k$$



2π exchange

$$V_{\text{TPE}}^{\Lambda NN} = \frac{g_A^2}{3f_0^4} \frac{\vec{\sigma}_3 \cdot \vec{q}_{63} \vec{\sigma}_2 \cdot \vec{q}_{52}}{(\vec{q}_{63}^2 + m_\pi^2)(\vec{q}_{52}^2 + m_\pi^2)} \vec{\tau}_2 \cdot \vec{\tau}_3 \left[-(3b_0 + b_D)m_\pi^2 + (2b_2 + 3b_4) \vec{q}_{63} \cdot \vec{q}_{52} \right]$$

$$- P_{23}^{(\sigma)} P_{23}^{(\tau)} \frac{g_A^2}{3f_0^4} \frac{\vec{\sigma}_3 \cdot \vec{q}_{53} \vec{\sigma}_2 \cdot \vec{q}_{62}}{(\vec{q}_{53}^2 + m_\pi^2)(\vec{q}_{62}^2 + m_\pi^2)} \vec{\tau}_2 \cdot \vec{\tau}_3 \left[-(3b_0 + b_D)m_\pi^2 + (2b_2 + 3b_4) \vec{q}_{53} \cdot \vec{q}_{62} \right]$$



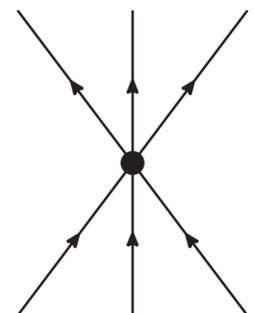
1π exchange

$$V_{\text{OPE}}^{\Lambda NN} = -\frac{g_A}{2f_0^2} \left\{ \frac{\vec{\sigma}_2 \cdot \vec{q}_{52}}{\vec{q}_{52}^2 + m_\pi^2} \vec{\tau}_2 \cdot \vec{\tau}_3 [(D'_1 \vec{\sigma}_1 + D'_2 \vec{\sigma}_3) \cdot \vec{q}_{52}] \right.$$

$$+ \frac{\vec{\sigma}_3 \cdot \vec{q}_{63}}{\vec{q}_{63}^2 + m_\pi^2} \vec{\tau}_2 \cdot \vec{\tau}_3 [(D'_1 \vec{\sigma}_1 + D'_2 \vec{\sigma}_2) \cdot \vec{q}_{63}]$$

$$+ P_{23}^{(\sigma)} P_{23}^{(\tau)} P_{13}^{(\sigma)} \frac{\vec{\sigma}_2 \cdot \vec{q}_{62}}{\vec{q}_{62}^2 + m_\pi^2} \vec{\tau}_2 \cdot \vec{\tau}_3 \left[-\frac{D'_1 + D'_2}{2} (\vec{\sigma}_1 + \vec{\sigma}_3) \cdot \vec{q}_{62} + \frac{D'_1 - D'_2}{2} i(\vec{\sigma}_3 \times \vec{\sigma}_1) \cdot \vec{q}_{62} \right]$$

$$\left. + P_{23}^{(\sigma)} P_{23}^{(\tau)} P_{12}^{(\sigma)} \frac{\vec{\sigma}_3 \cdot \vec{q}_{53}}{\vec{q}_{53}^2 + m_\pi^2} \vec{\tau}_2 \cdot \vec{\tau}_3 \left[-\frac{D'_1 + D'_2}{2} (\vec{\sigma}_1 + \vec{\sigma}_2) \cdot \vec{q}_{53} - \frac{D'_1 - D'_2}{2} i(\vec{\sigma}_1 \times \vec{\sigma}_2) \cdot \vec{q}_{53} \right] \right\}$$



Contacts

$$V_{\text{ct}}^{\Lambda NN} = C'_1 (1 - \vec{\sigma}_2 \cdot \vec{\sigma}_3)(3 + \vec{\tau}_2 \cdot \vec{\tau}_3)$$

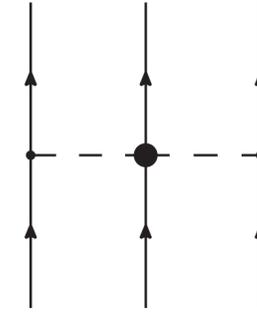
$$+ C'_2 \vec{\sigma}_1 \cdot (\vec{\sigma}_2 + \vec{\sigma}_3)(1 - \vec{\tau}_2 \cdot \vec{\tau}_3)$$

$$+ C'_3 (3 + \vec{\sigma}_2 \cdot \vec{\sigma}_3)(1 - \vec{\tau}_2 \cdot \vec{\tau}_3),$$

2π -exchange term

Uratsu +, PRC 113, 015204 (2026)

$$V_{\text{TPE}}^{\Xi NN} = \mathcal{A}_{23} (Y_{123}^{456} + Y_{231}^{564} + Y_{312}^{645})$$



$$Y_{123}^{456} = \frac{g_A g_B}{12f_\pi^4} \frac{(\boldsymbol{\sigma}_1 \cdot \mathbf{q}_{41})(\boldsymbol{\sigma}_3 \cdot \mathbf{q}_{63})}{(q_{41}^2 + m_\pi^2)(q_{63}^2 + m_\pi^2)} \left[\boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_3 \left(\underline{4c_1 m_\pi^2} - \underline{2c_3 \mathbf{q}_{41} \cdot \mathbf{q}_{63}} \right) + \underline{c_4} \{ \boldsymbol{\tau}_3 \cdot (\boldsymbol{\tau}_1 \times \boldsymbol{\tau}_2) \} \{ \boldsymbol{\sigma}_2 \cdot (\mathbf{q}_{41} \times \mathbf{q}_{63}) \} \right]$$

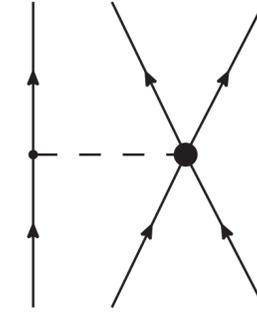
$$Y_{231}^{564} = \frac{g_A g_B}{12f_\pi^4} \frac{(\boldsymbol{\sigma}_2 \cdot \mathbf{q}_{52})(\boldsymbol{\sigma}_1 \cdot \mathbf{q}_{41})}{(q_{52}^2 + m_\pi^2)(q_{41}^2 + m_\pi^2)} \left[\boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_1 \left(\underline{4c_1 m_\pi^2} - \underline{2c_3 \mathbf{q}_{52} \cdot \mathbf{q}_{41}} \right) + \underline{c_4} \{ \boldsymbol{\tau}_3 \cdot (\boldsymbol{\tau}_1 \times \boldsymbol{\tau}_2) \} \{ \boldsymbol{\sigma}_3 \cdot (\mathbf{q}_{52} \times \mathbf{q}_{41}) \} \right]$$

$$Y_{312}^{645} = \frac{g_A^2}{12f_\pi^4} \frac{(\boldsymbol{\sigma}_3 \cdot \mathbf{q}_{63})(\boldsymbol{\sigma}_2 \cdot \mathbf{q}_{52})}{(q_{63}^2 + m_\pi^2)(q_{52}^2 + m_\pi^2)} \left[\boldsymbol{\tau}_3 \cdot \boldsymbol{\tau}_2 \left(\underline{-12u_1 m_\pi^2} + \underline{6u_3 \mathbf{q}_{63} \cdot \mathbf{q}_{52}} \right) - \underline{u_4} \{ \boldsymbol{\tau}_3 \cdot (\boldsymbol{\tau}_1 \times \boldsymbol{\tau}_2) \} \{ \boldsymbol{\sigma}_1 \cdot (\mathbf{q}_{63} \times \mathbf{q}_{52}) \} \right]$$

6 LECs

1 π -exchange term

Uratsu +, PRC 113, 015204 (2026)



$$V_{\text{OPE}}^{\Xi_{NN}} = X_{123}^{456} + X_{231}^{564} + X_{312}^{645} + \mathcal{P}_{23}\mathcal{P}_{12}X_{312}^{564} + \mathcal{P}_{23}\mathcal{P}_{13}X_{231}^{645}$$

$$X_{123}^{456} = \frac{g_B d}{2f_\pi^2} \frac{\boldsymbol{\sigma}_1 \cdot \mathbf{q}_{41}}{q_{41}^2 + m_\pi^2} [(\boldsymbol{\tau}_2 - \boldsymbol{\tau}_3) \cdot \boldsymbol{\tau}_1 (\boldsymbol{\sigma}_2 - \boldsymbol{\sigma}_3) \cdot \mathbf{q}_{41} + (\boldsymbol{\tau}_1 \times \boldsymbol{\tau}_2) \cdot \boldsymbol{\tau}_3 (\boldsymbol{\sigma}_2 \times \boldsymbol{\sigma}_3) \cdot \mathbf{q}_{41}]$$

$$X_{231}^{564} = \frac{g_A}{2f_\pi^2} \frac{\boldsymbol{\sigma}_2 \cdot \mathbf{q}_{52}}{q_{52}^2 + m_\pi^2} [(e_1 \boldsymbol{\sigma}_3 + e_2 \boldsymbol{\sigma}_1) \cdot \mathbf{q}_{52} \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 + (e_3 \boldsymbol{\sigma}_3 + e_4 \boldsymbol{\sigma}_1) \cdot \mathbf{q}_{52} \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_2 - e_5 (\boldsymbol{\tau}_2 \times \boldsymbol{\tau}_3) \cdot \boldsymbol{\tau}_1 (\boldsymbol{\sigma}_3 \times \boldsymbol{\sigma}_1) \cdot \mathbf{q}_{52}]$$

$$X_{312}^{645} = \frac{g_A}{2f_\pi^2} \frac{\boldsymbol{\sigma}_3 \cdot \mathbf{q}_{63}}{q_{63}^2 + m_\pi^2} [(e_4 \boldsymbol{\sigma}_1 + e_3 \boldsymbol{\sigma}_2) \cdot \mathbf{q}_{63} \boldsymbol{\tau}_3 \cdot \boldsymbol{\tau}_1 + (e_2 \boldsymbol{\sigma}_1 + e_1 \boldsymbol{\sigma}_2) \cdot \mathbf{q}_{63} \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 - e_5 (\boldsymbol{\tau}_3 \times \boldsymbol{\tau}_1) \cdot \boldsymbol{\tau}_2 (\boldsymbol{\sigma}_1 \times \boldsymbol{\sigma}_2) \cdot \mathbf{q}_{63}]$$

$$X_{312}^{564} = \frac{g_A}{2f_\pi^2} \frac{\boldsymbol{\sigma}_3 \cdot \mathbf{q}_{63}}{q_{63}^2 + m_\pi^2} [\{f_1 \boldsymbol{\sigma}_1 + f_2 \boldsymbol{\sigma}_2 + f_3 i(\boldsymbol{\sigma}_1 \times \boldsymbol{\sigma}_2)\} \cdot \mathbf{q}_{63} \boldsymbol{\tau}_3 \cdot \boldsymbol{\tau}_1 + \{f_2 \boldsymbol{\sigma}_1 + f_1 \boldsymbol{\sigma}_2 + f_3 i(\boldsymbol{\sigma}_1 \times \boldsymbol{\sigma}_2)\} \cdot \mathbf{q}_{63} \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3$$

$$+ \{f_4(\boldsymbol{\sigma}_1 + \boldsymbol{\sigma}_2) + i f_5(\boldsymbol{\sigma}_1 \times \boldsymbol{\sigma}_2)\} \cdot \mathbf{q}_{63} i(\boldsymbol{\tau}_3 \times \boldsymbol{\tau}_1) \cdot \boldsymbol{\tau}_2]$$

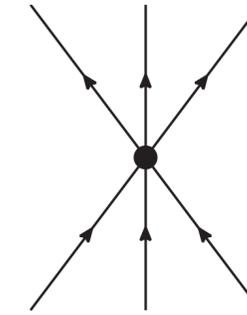
$$X_{231}^{645} = \frac{g_A}{2f_\pi^2} \frac{\boldsymbol{\sigma}_2 \cdot \mathbf{q}_{52}}{q_{52}^2 + m_\pi^2} [\{f_1 \boldsymbol{\sigma}_3 + f_2 \boldsymbol{\sigma}_1 - f_3 i(\boldsymbol{\sigma}_3 \times \boldsymbol{\sigma}_1)\} \cdot \mathbf{q}_{52} \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 + \{f_2 \boldsymbol{\sigma}_3 + f_1 \boldsymbol{\sigma}_1 - f_3 i(\boldsymbol{\sigma}_3 \times \boldsymbol{\sigma}_1)\} \cdot \mathbf{q}_{52} \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_2$$

$$- \{f_4(\boldsymbol{\sigma}_3 + \boldsymbol{\sigma}_1) - i f_5(\boldsymbol{\sigma}_3 \times \boldsymbol{\sigma}_1)\} \cdot \mathbf{q}_{52} i(\boldsymbol{\tau}_2 \times \boldsymbol{\tau}_3) \cdot \boldsymbol{\tau}_1]$$

11 LECs

Contact term

Uratsu +, PRC 113, 015204 (2026)



$$\begin{aligned}
 V_{\text{ct}}^{\Xi NN} = & \underline{E_1} + \underline{E_2}(\boldsymbol{\sigma}_2 + \boldsymbol{\sigma}_3) \cdot \boldsymbol{\sigma}_1 + \underline{E_3}\boldsymbol{\sigma}_2 \cdot \boldsymbol{\sigma}_3 \\
 & + [\underline{F_1} - \underline{F_2}(\boldsymbol{\sigma}_2 - \boldsymbol{\sigma}_3) \cdot \boldsymbol{\sigma}_1 - \underline{F_1}\boldsymbol{\sigma}_2 \cdot \boldsymbol{\sigma}_3] \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_2 \\
 & + [\underline{F_1} - \underline{F_2}(\boldsymbol{\sigma}_2 - \boldsymbol{\sigma}_3) \cdot \boldsymbol{\sigma}_1 - \underline{F_1}\boldsymbol{\sigma}_2 \cdot \boldsymbol{\sigma}_3] \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_3 \\
 & + \left[\underline{G_1} - \underline{E_2}(\boldsymbol{\sigma}_2 + \boldsymbol{\sigma}_3) \cdot \boldsymbol{\sigma}_1 - \frac{1}{3}\underline{E_1}\boldsymbol{\sigma}_2 \cdot \boldsymbol{\sigma}_3 \right] \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \\
 & + \underline{F_2}(\boldsymbol{\sigma}_1 \times \boldsymbol{\sigma}_2) \cdot \boldsymbol{\sigma}_3 (\boldsymbol{\tau}_1 \times \boldsymbol{\tau}_2) \cdot \boldsymbol{\tau}_3
 \end{aligned}$$

Gen Uratsu (M2)



6 LECs

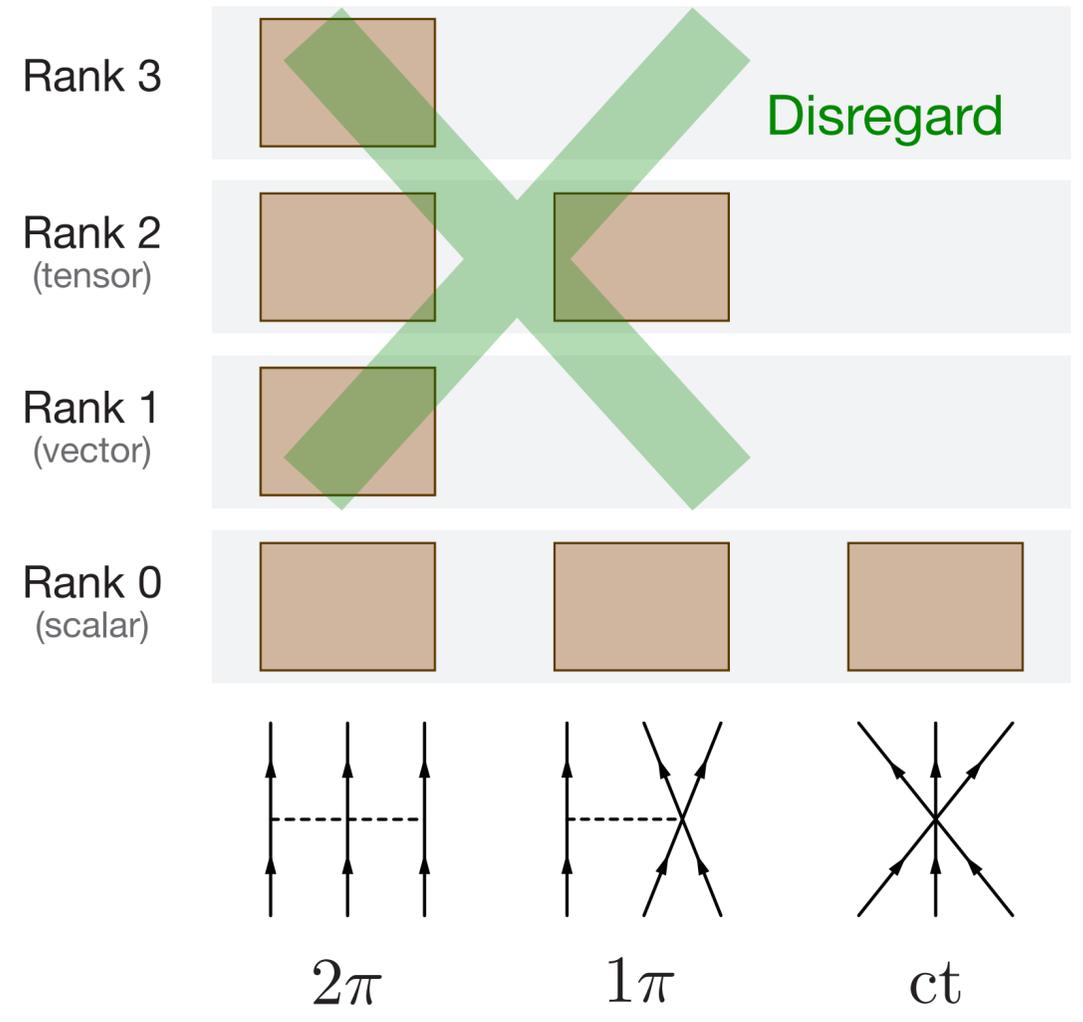
We roughly estimate
 Ξ_{NN} 3BFs in $d-\Xi^-$ scattering

Hard to constrain all LECs
& all complicated terms

1. Central components only

Uratsu +, PRC 113, 015204 (2026)

Irreducible tensor decomposition



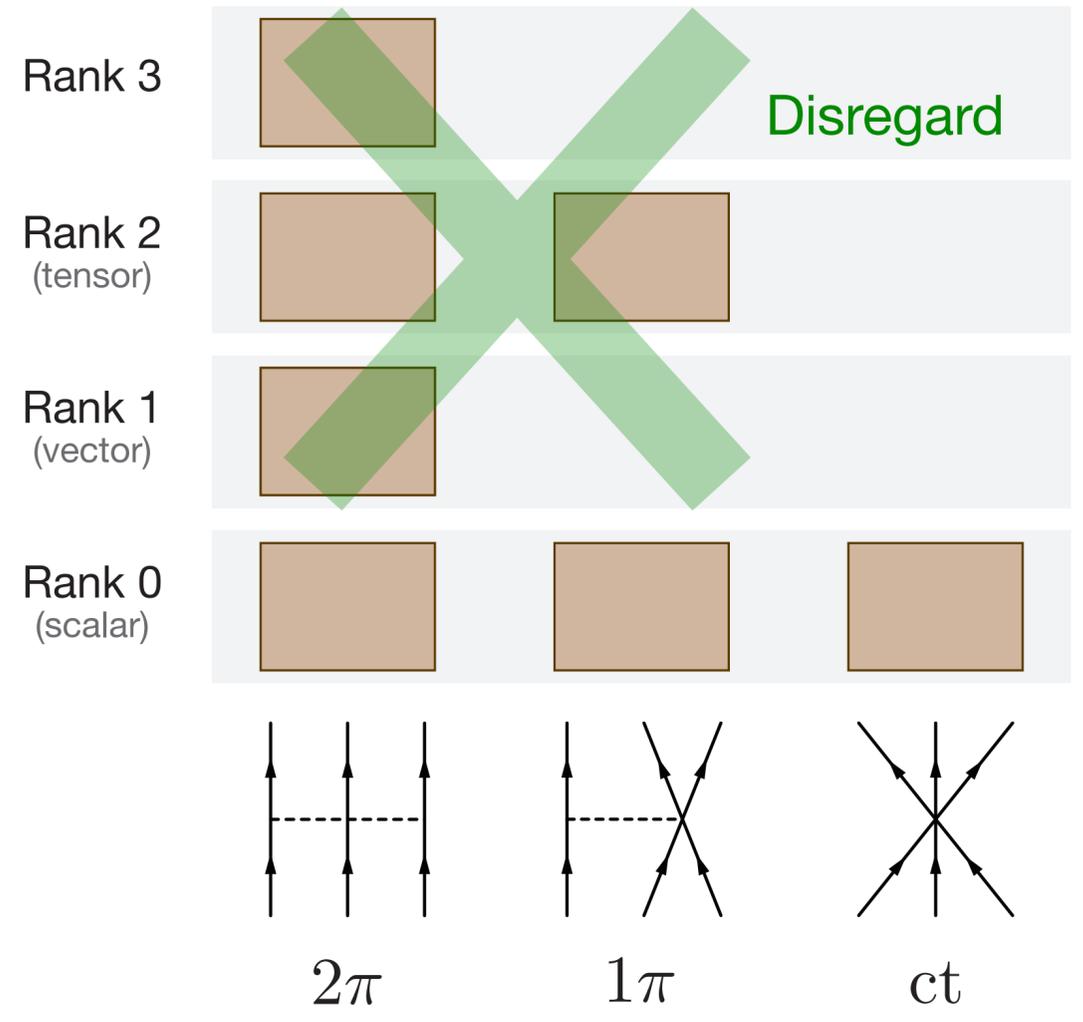
1. Central components only

2. Fourier transform

Uratsu +, PRC 113, 015204 (2026)

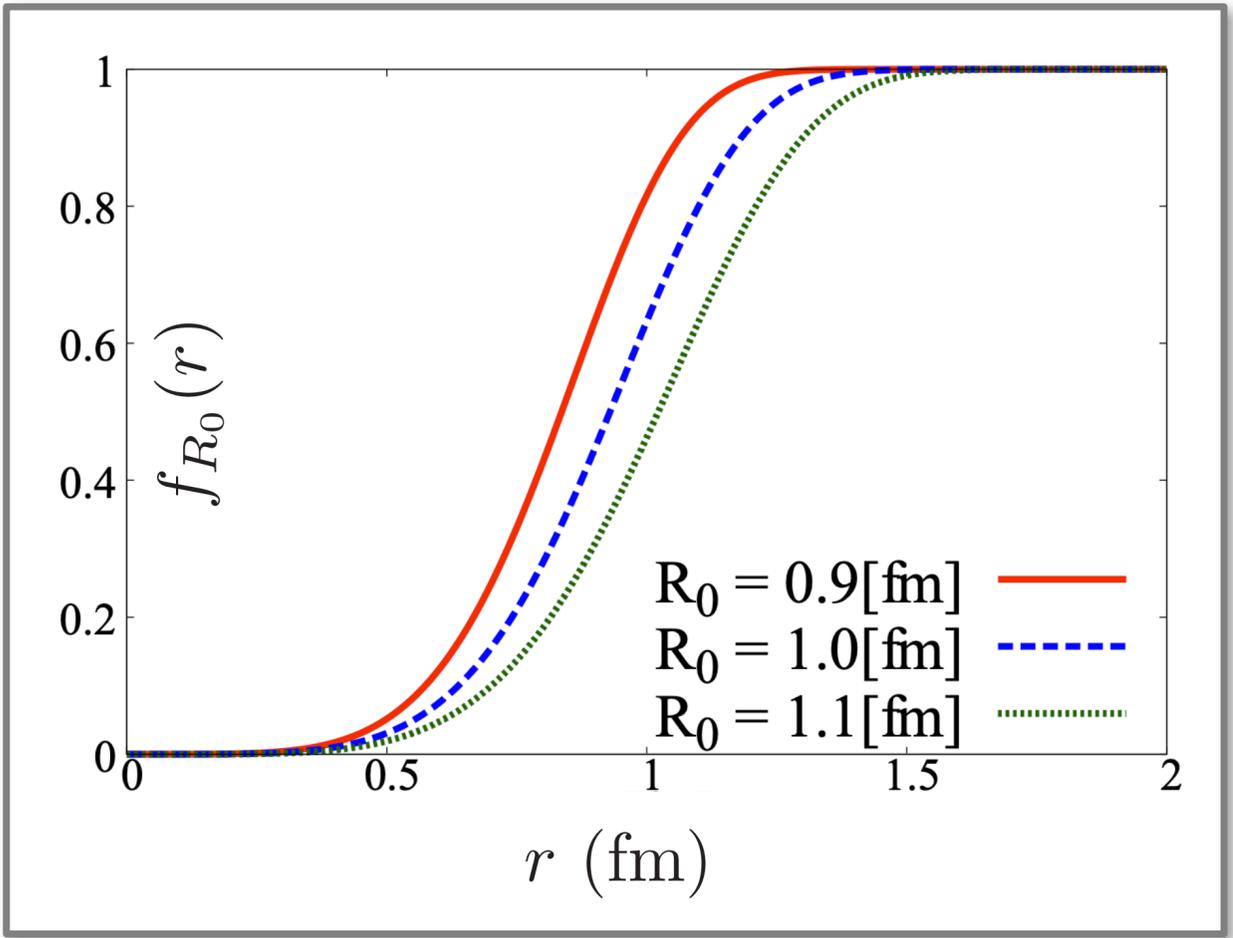
Irreducible tensor decomposition

Central potentials in coordinate space



1. Central components only

Irreducible tensor decomposition



2. Fourier transform

Uratsu +, PRC 113, 015204 (2026)

Central potentials in coordinate space

3. Regularization

Gezerlis +, PRC 90, 054323 (2014)

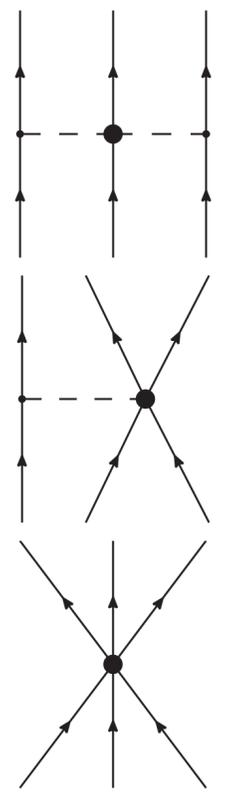
► Yukawa functions from π exchange

$$Y(m_\pi r) \rightarrow Y(m_\pi r) f_{R_0}(r)$$

$$f_{R_0}(r) = 1 - \exp\left[-\left(\frac{r}{R_0}\right)^5\right]$$

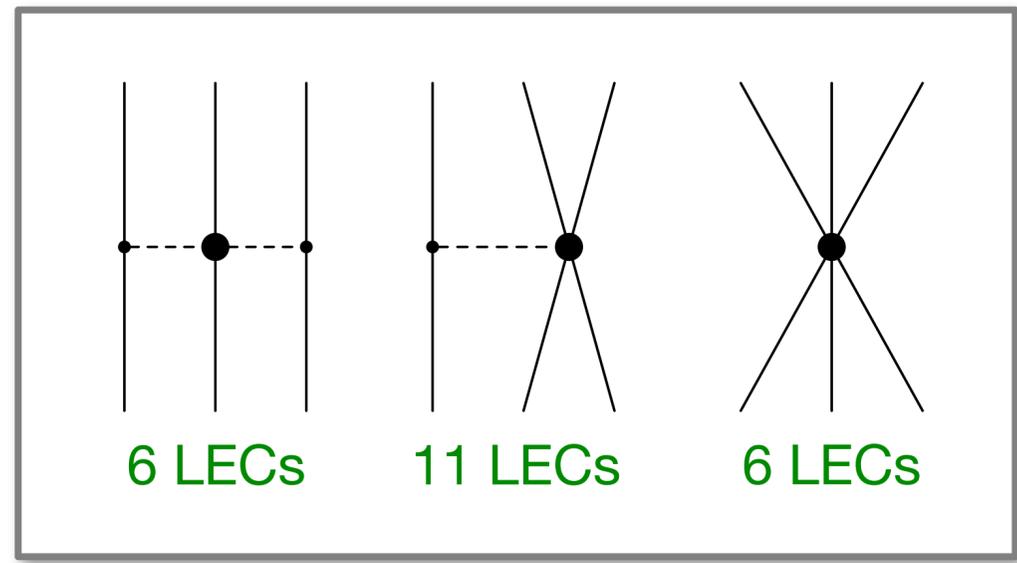
► Delta functions from contacts

$$\delta(\mathbf{r}) \rightarrow \frac{5}{4\pi\Gamma(3/5)R_0^3} \exp\left[-\left(\frac{r}{R_0}\right)^5\right]$$



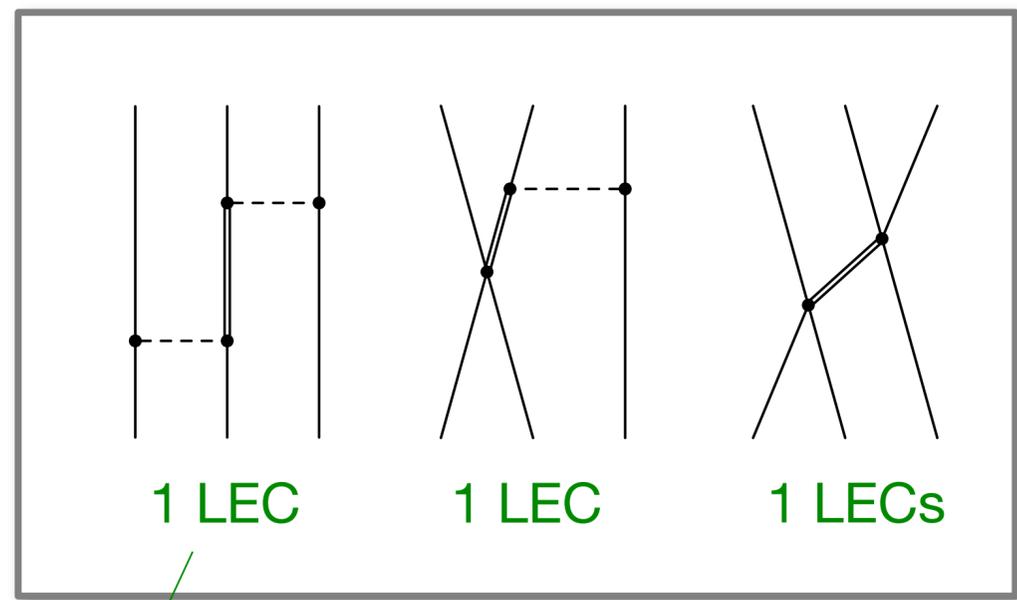
4. Decuplet saturation approx.

Petschauer +, NPA 957 347 (2017)



6 LECs 11 LECs 6 LECs

≈



1 LEC 1 LEC 1 LECs

/ Large N_c value

Only 3- & 4-point vertices

$\Delta(1232)$ & $\Xi(1530)$ included

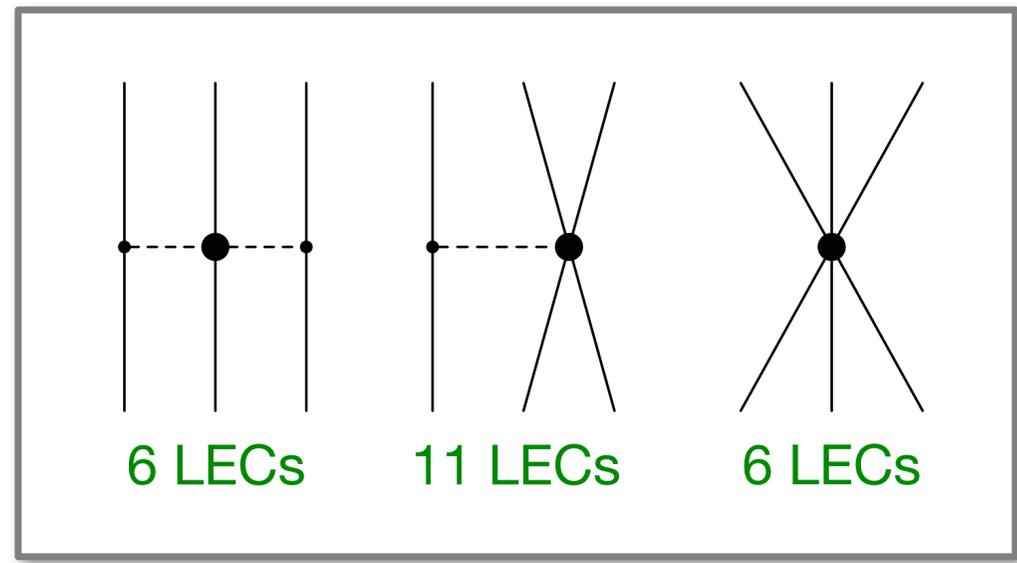
Decuplet-octet mass splitting
~ 200 MeV

$$C = 3g_A/4$$

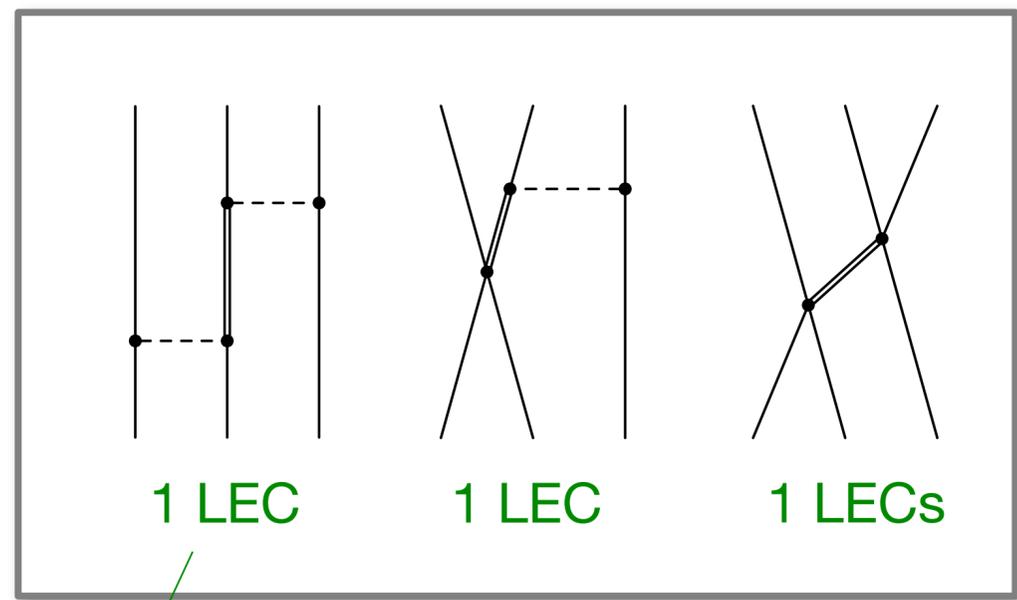
Kaiser +, NPA 637, 395 (1998)
Vonk & Meißner, EPJA 61, 135 (2025)

4. Decuplet saturation approx.

Petschauer +, NPA 957 347 (2017)



\rightsquigarrow



Large N_c value

$$C = 3g_A/4$$

Kaiser +, NPA 637, 395 (1998)
Vonk & Meißner, EPJA 61, 135 (2025)

5. Folding potential

Uratsu +, PRC 113, 015204 (2026)

$$U_{3BF}^{(\sigma)}(R) = \frac{1}{(4\pi)^2} \iint dr d\hat{R} \frac{\varphi^2(r)}{r^2} W^{(\sigma)}(\mathbf{r}, \mathbf{R})$$

$$W^{(\sigma)}(\mathbf{r}, \mathbf{R}) = \frac{1}{(2\pi)^6} \iiint d\mathbf{q}_1 d\mathbf{q}_2 d\mathbf{q}_3 e^{i(\mathbf{q}_1 \cdot \mathbf{r}_1 + \mathbf{q}_2 \cdot \mathbf{r}_2 + \mathbf{q}_3 \cdot \mathbf{r}_3)}$$

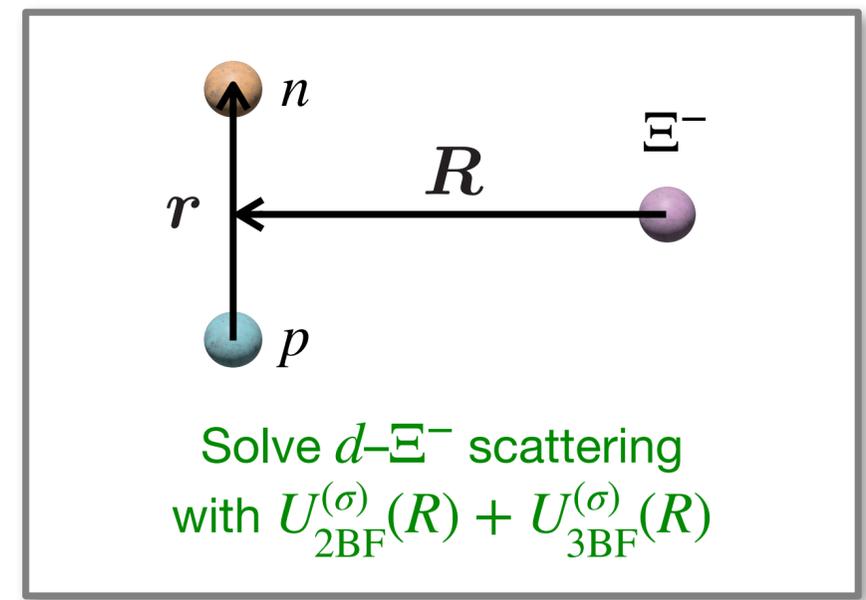
$$\times \delta(\mathbf{q}_1 + \mathbf{q}_2 + \mathbf{q}_3) \left\langle V_{(0)}^{\Xi NN}(\mathbf{q}_1, \mathbf{q}_2, \mathbf{q}_3) \right\rangle_{\text{spin-isospin}}$$

Central potential
Spin-isospin matrix elements

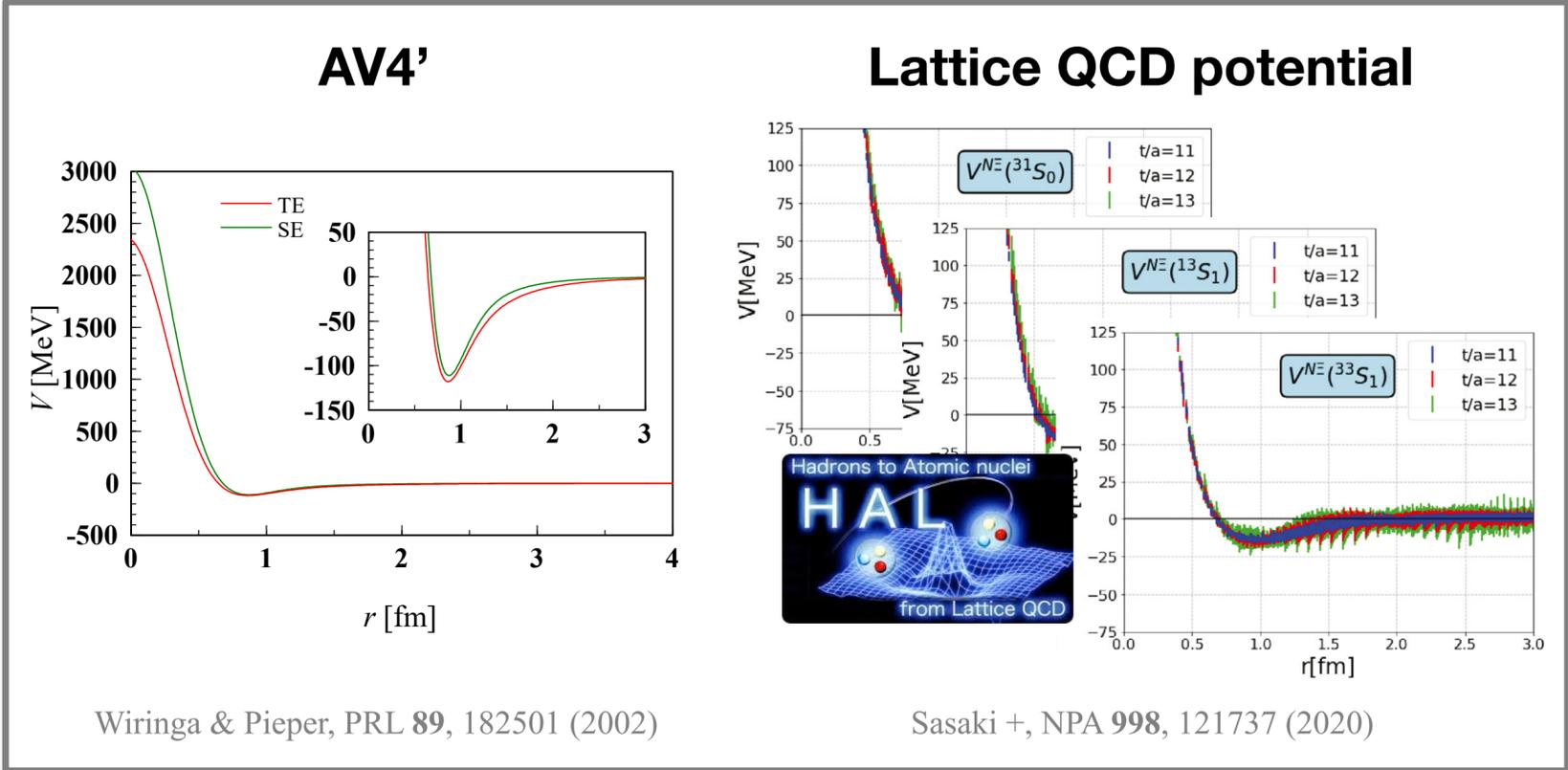
Only 3- & 4-point vertices

$\Delta(1232)$ & $\Xi(1530)$ included

Decuplet-octet mass splitting ~ 200 MeV



2BFs



Correlation functions

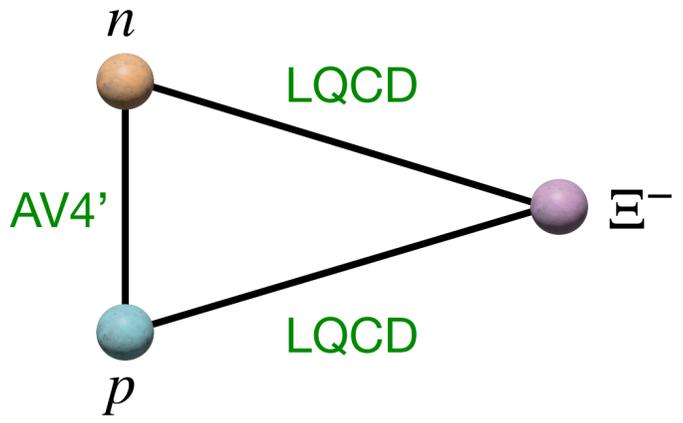
☼ Koonin-Pratt formula Koonin, PRB **70**, 43 (1977)
Pratt, PRD **33**, 1314 (1986)

$$C_{d\Xi^-}(q) = 4\pi \int dR R^2 \mathcal{S}(R) \sum_{L=1} \hat{L}^2 \left[\frac{F_L(qR)}{qR} \right]^2 + \frac{2\pi}{3} \int dR R^2 \mathcal{S}(R) \sum_{\sigma=\frac{1}{2}, \frac{3}{2}} \hat{\sigma}^2 \left| \frac{\chi_{L=0}^{(\sigma)}(q, R)}{qR} \right|^2$$

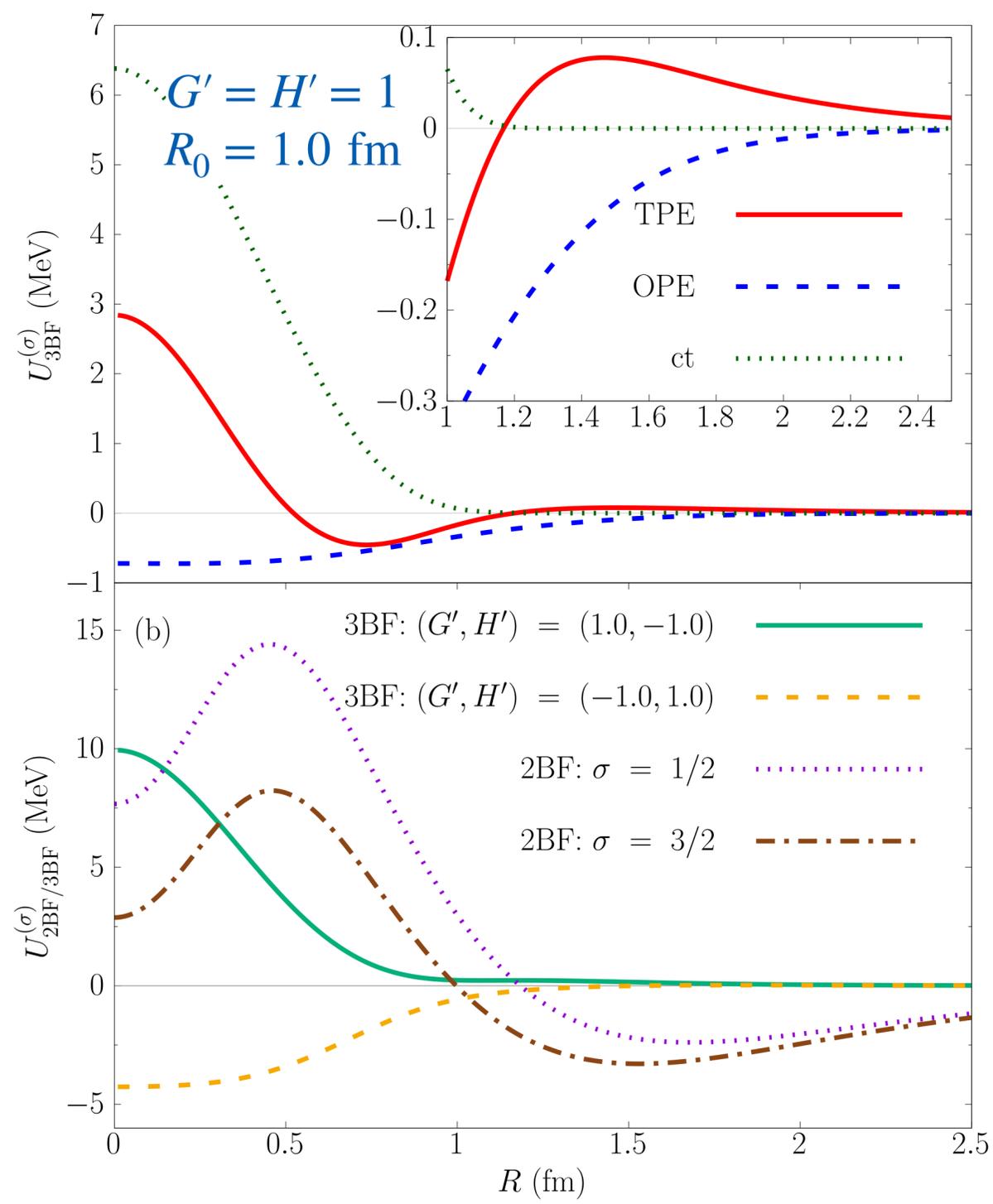
☼ 2-body source func. (Gaussian)

Limitations

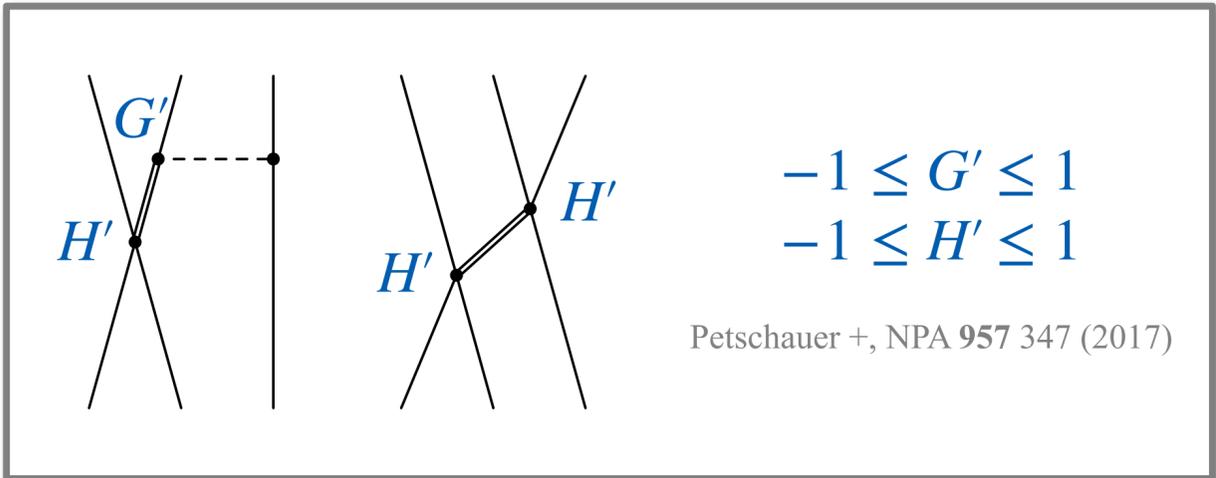
- ☼ S-wave only (all subsystems)
- ☼ No deuteron breakup
Confirmed to be small: Ogata +, PRC **103**, 065205 (2021)
- ☼ No rearrangement channels
- ☼ No $\Xi N - \Lambda \Lambda$ coupling
Expected to be small: Kamiya +, PRC **105**, 014915 (2022)



Uratsu +, PRC 113, 015204 (2026)

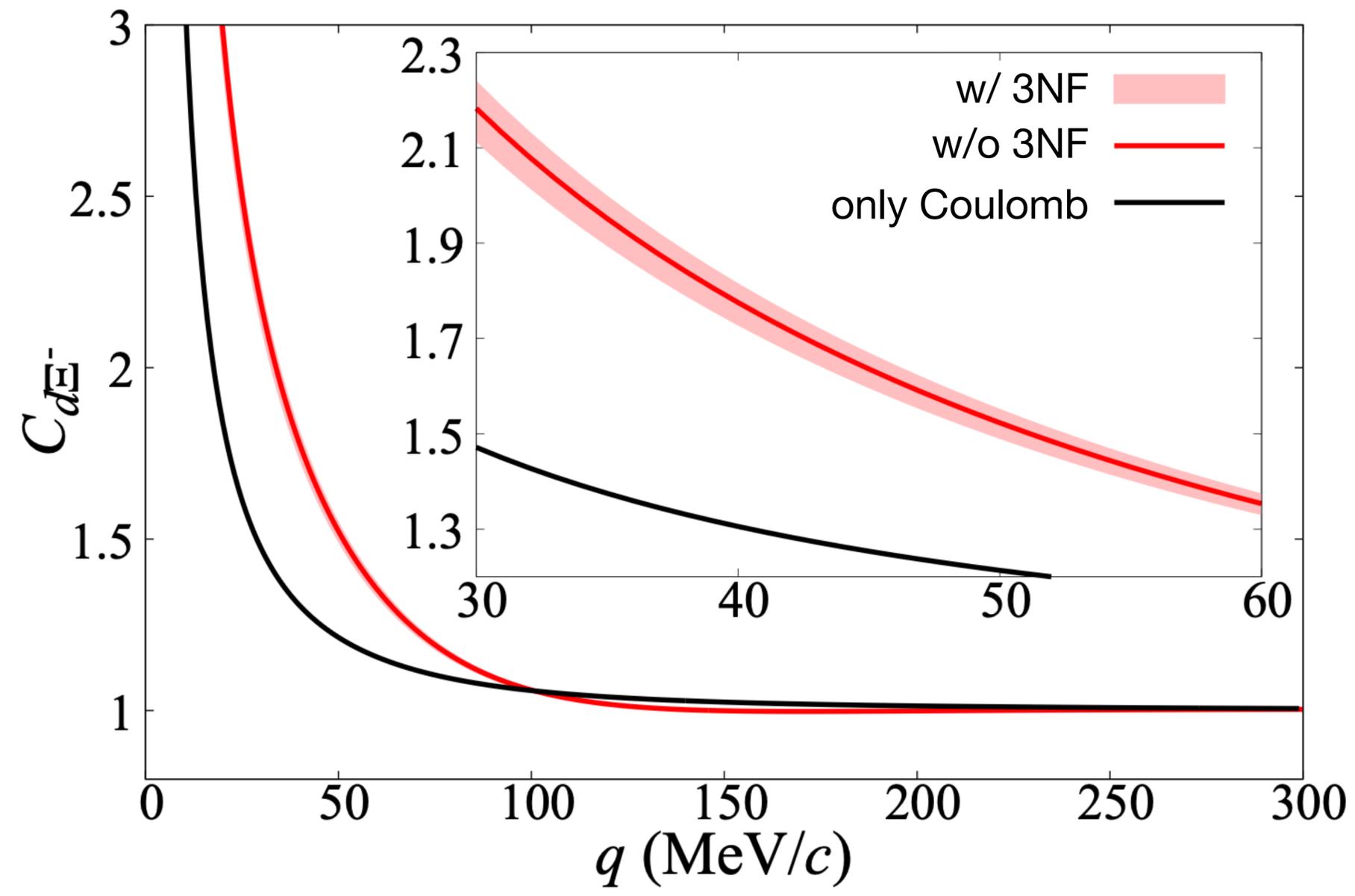


Rough estimate of LECs



► Weaker and shorter w.r.t. 2BF

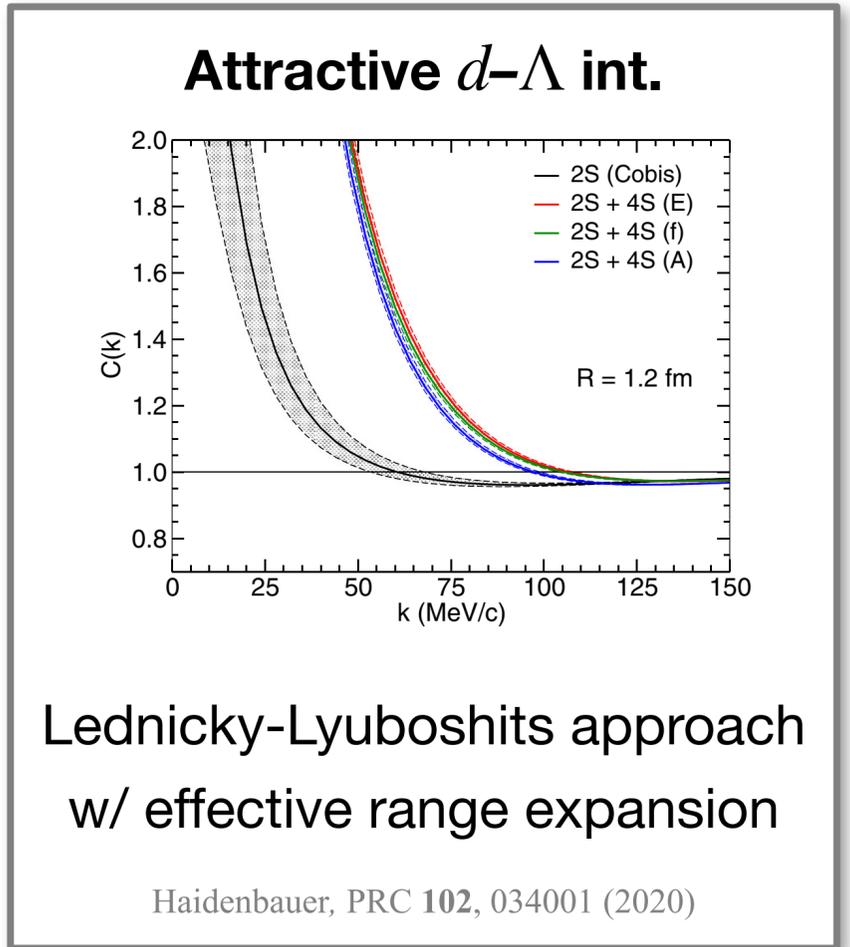
$d + \Xi^-$

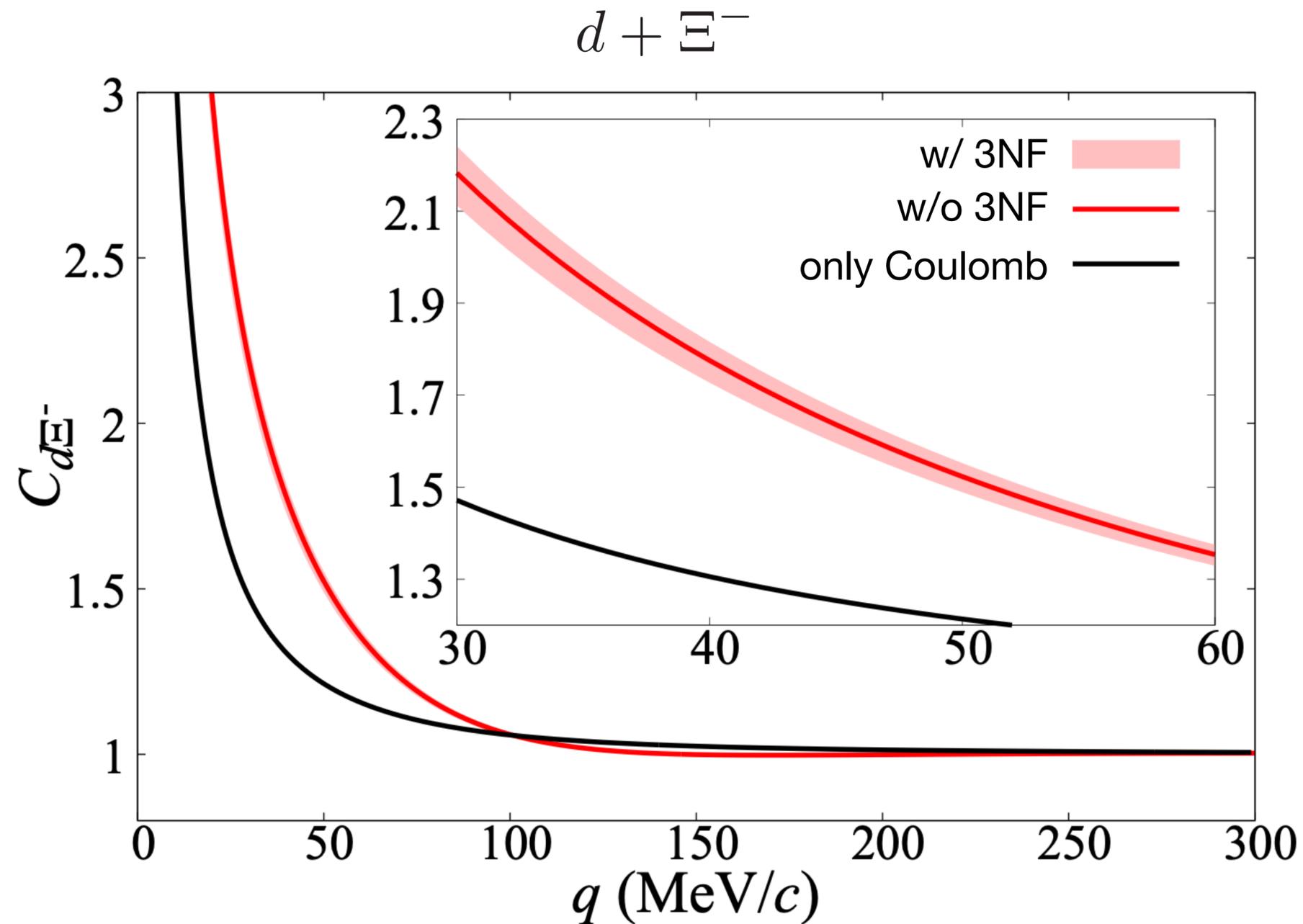


Source size: 1.2 fm

► Attractive $d-\Xi^-$ interaction by 2BF

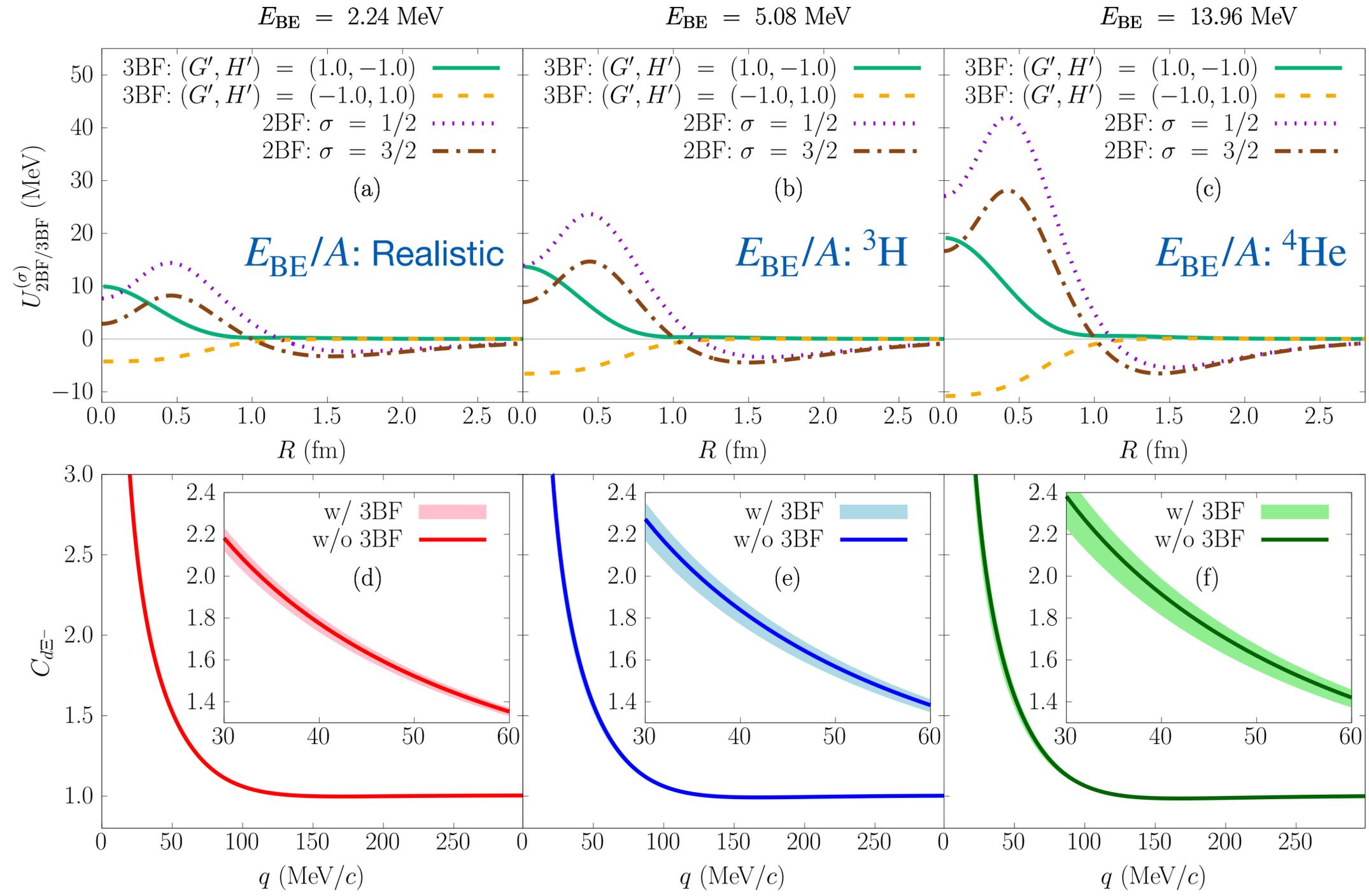
Consistent





Source size: 1.2 fm

- ▶ Attractive $d-\Xi^-$ interaction by 2BF
- ▶ 3BF effect: $\lesssim 4\%$
- ▶ Reason for small effect:
CF is sensitive to the potential
at $1 \lesssim R \lesssim 2$ fm
- ▶ Cutoff & source size variation:
The same situation

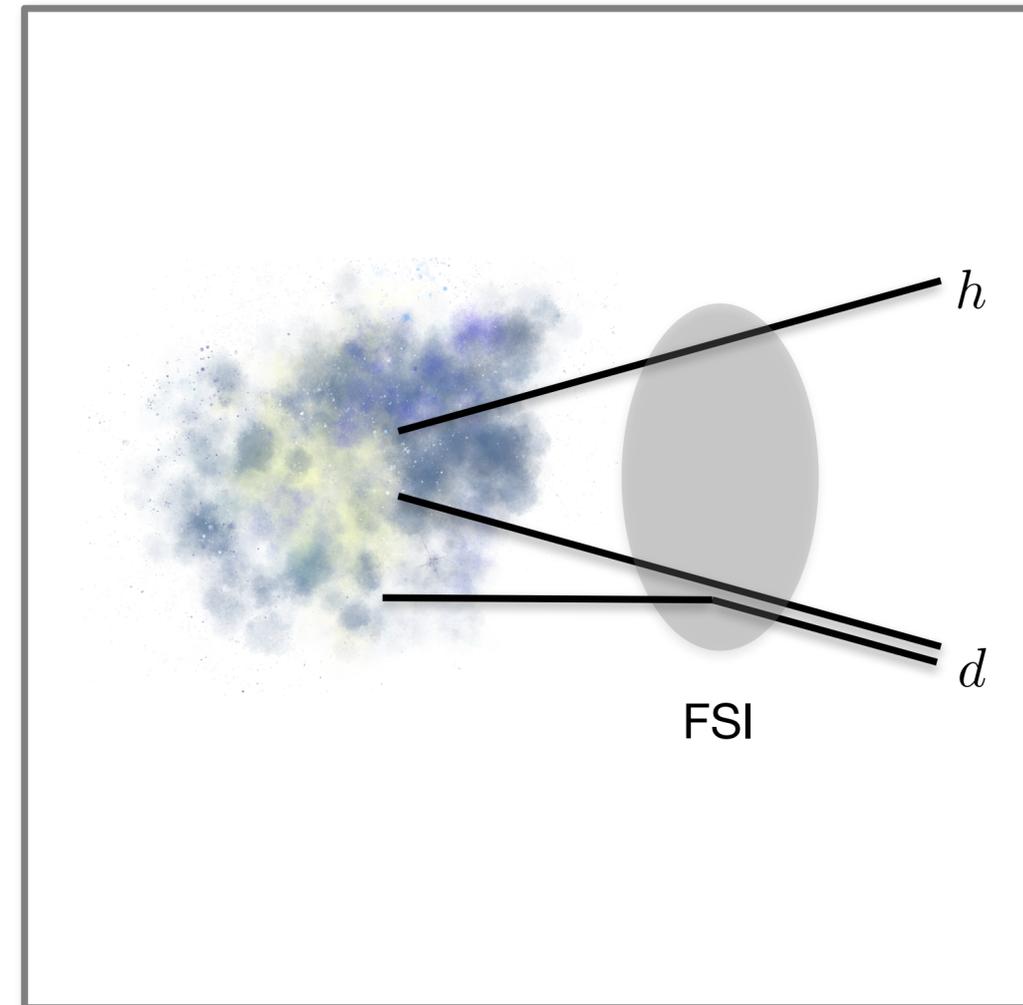
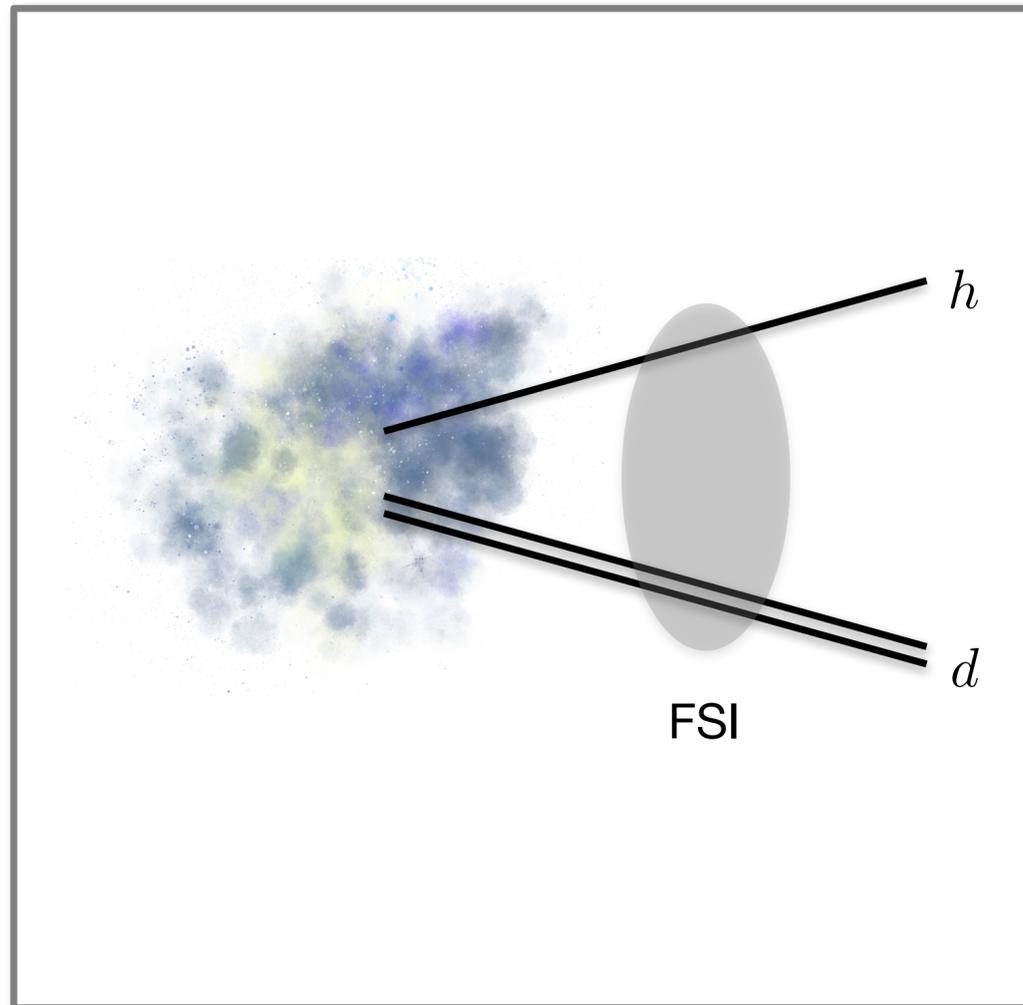


▶ Even deep binding:
3BF effect $\lesssim 8\%$

▶ Loosely bound nature of d
cannot explain small 3BF effect

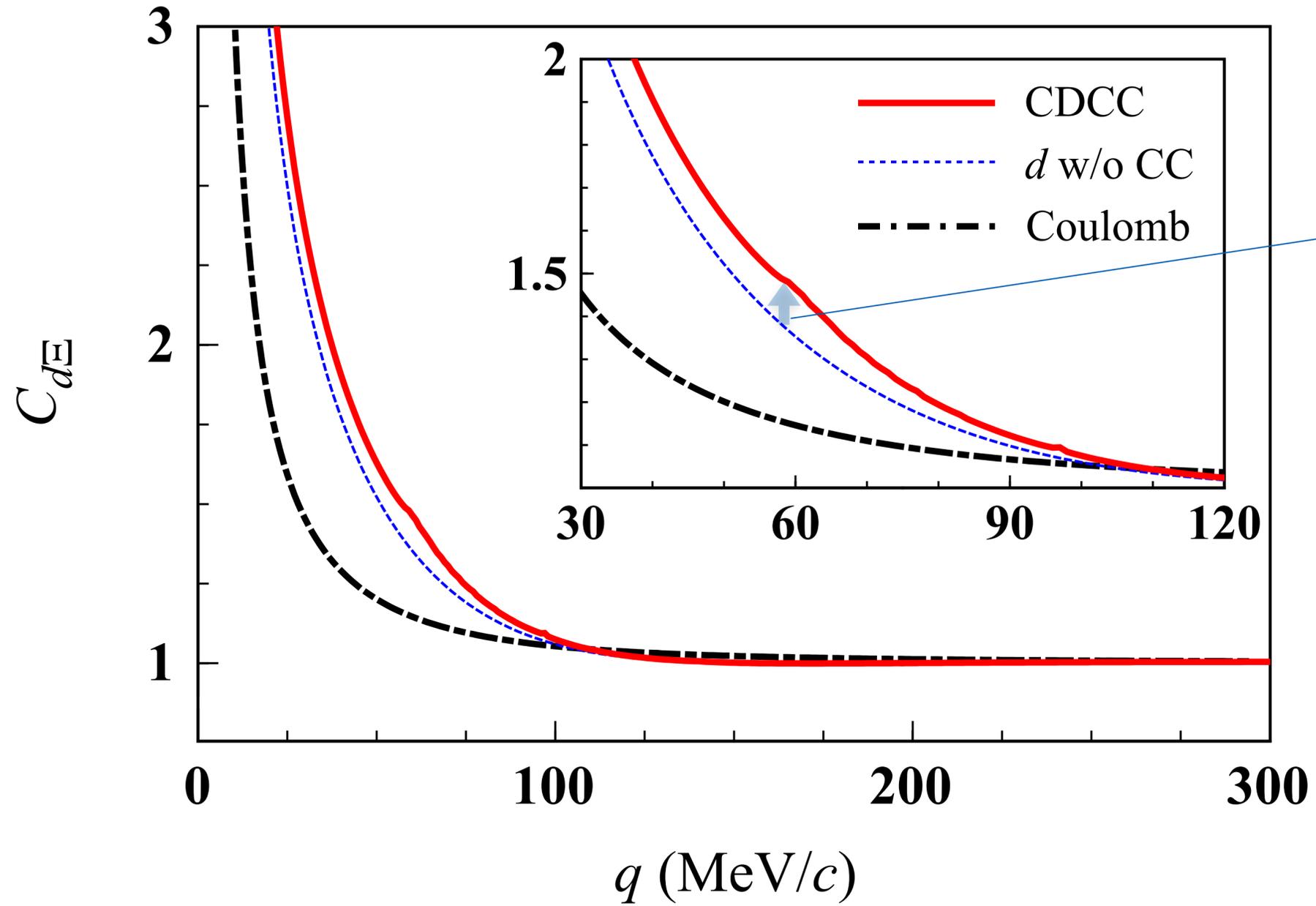
Direct production or formation by final-state interaction

Cf. Mrówczyński & Słóń, APPB 51, 1739 (2020)



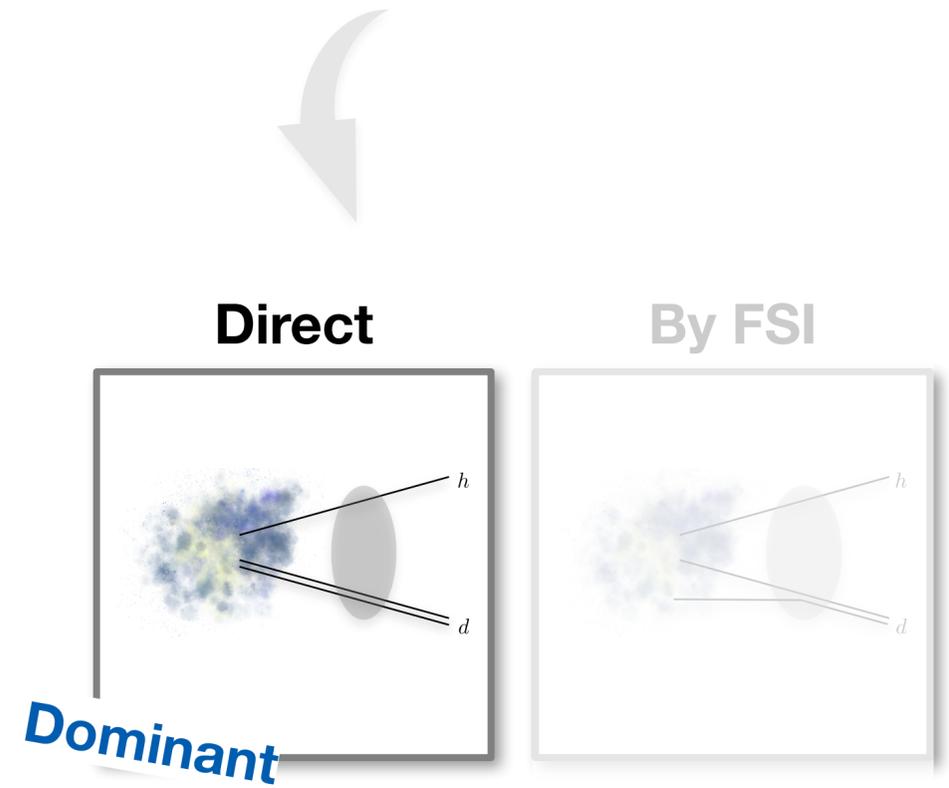
Direct production or formation by final-state interaction

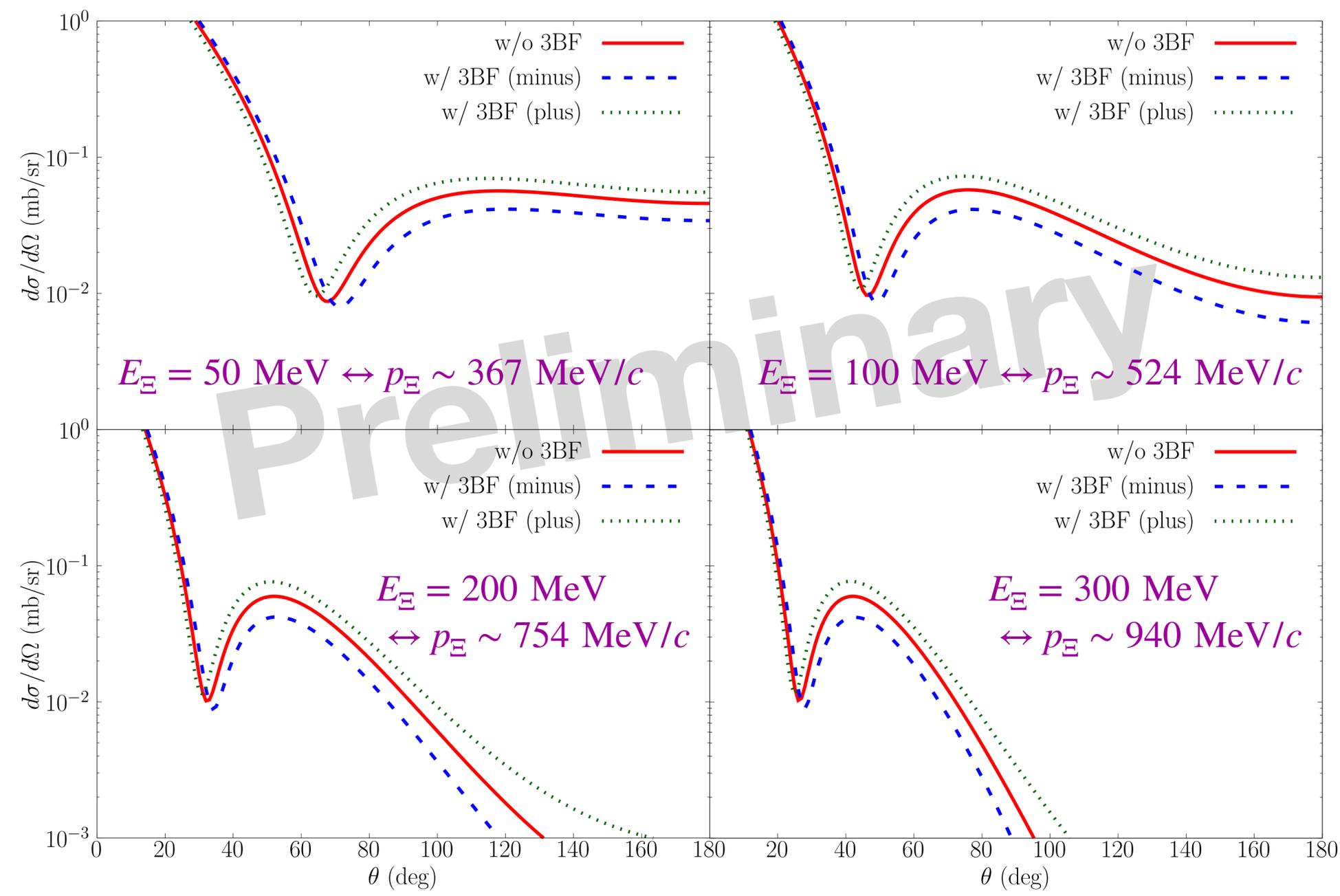
Cf. Mrówczyński & Słóń, APPB 51, 1739 (2020)



► Simulation w/ coupled channels method

Slight enhancement (6–8%)

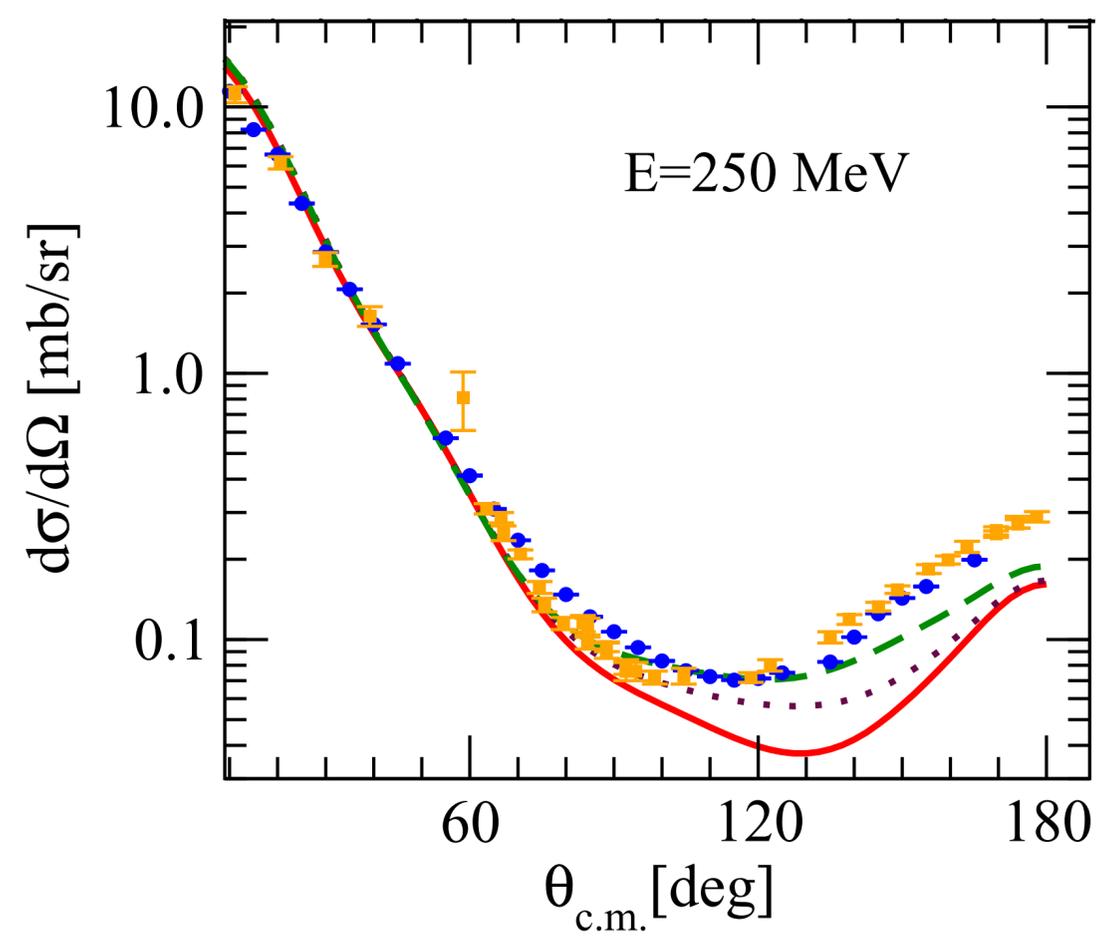




- ▶ Central 2BF + 3BF only
- ▶ 3BF effect: $\sim 20\text{--}40\%$ in magnitude
- ▶ Shift of dip position
- ▶ Typical experiments:
 $450 \lesssim p \lesssim 850 \text{ MeV}/c$

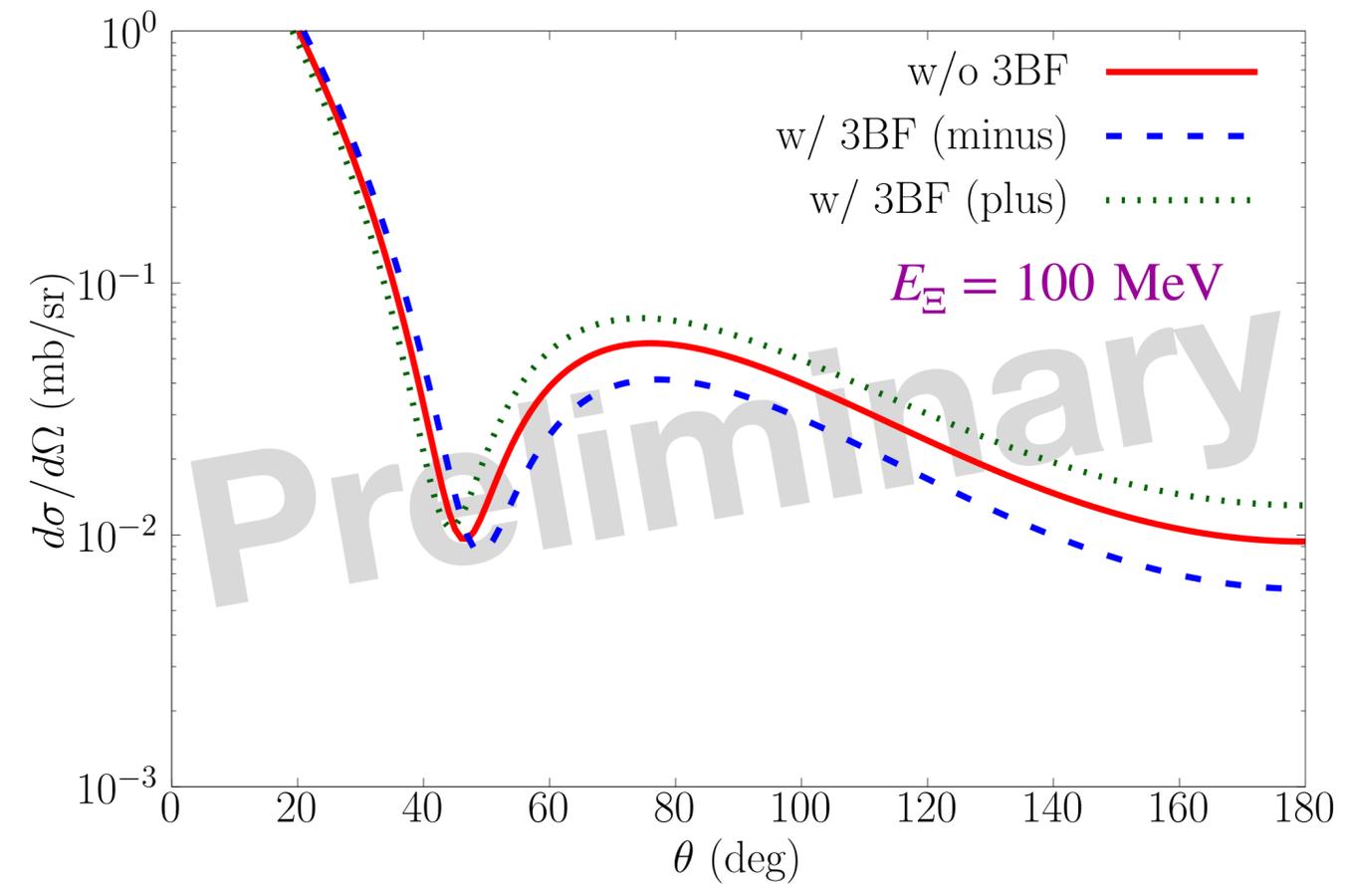
Miwa +, PRC **104**, 045204 (2021)
Miwa +, PRL **128**, 072501 (2022)
Nanamura +, PTEP **2022**, 093D01 (2022)

$d + p$ scattering



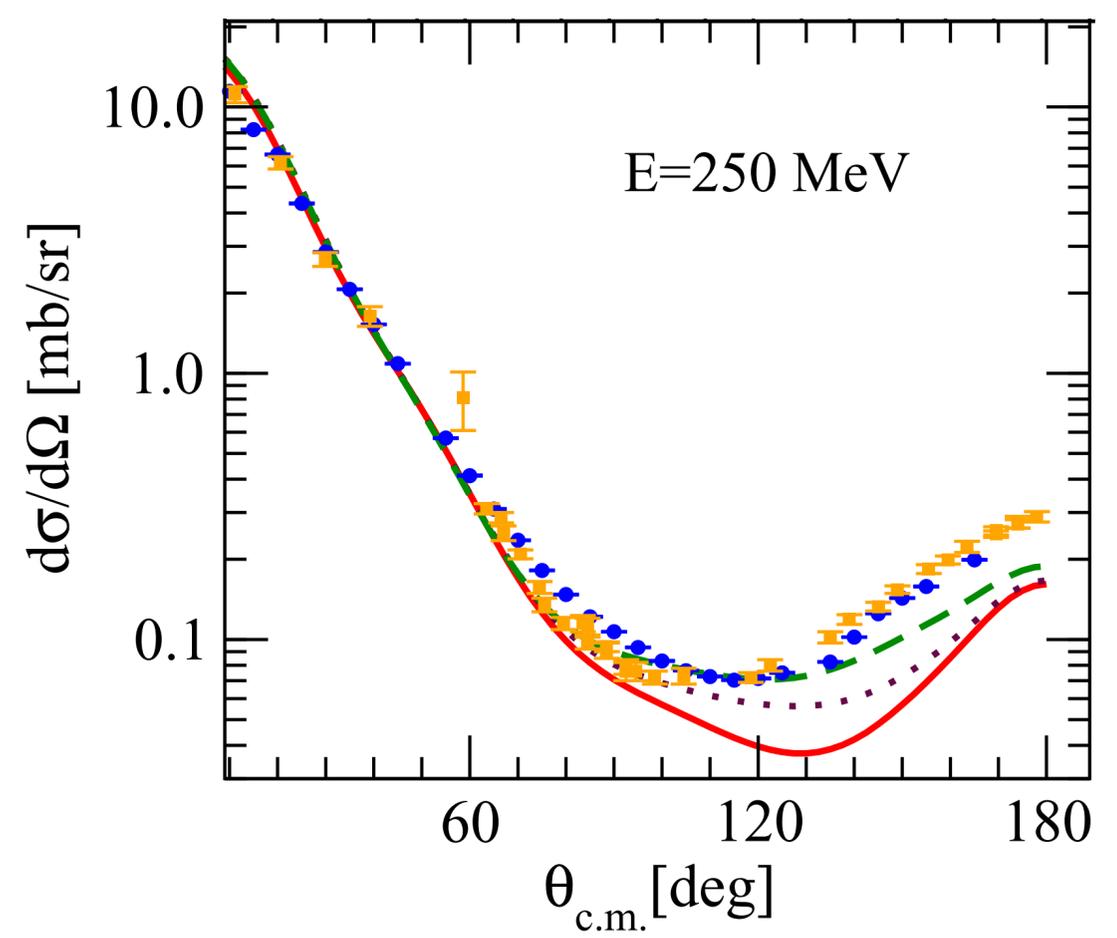
Witała +, PRC 105, 054004 (2022)

$d + \Xi^-$ scattering



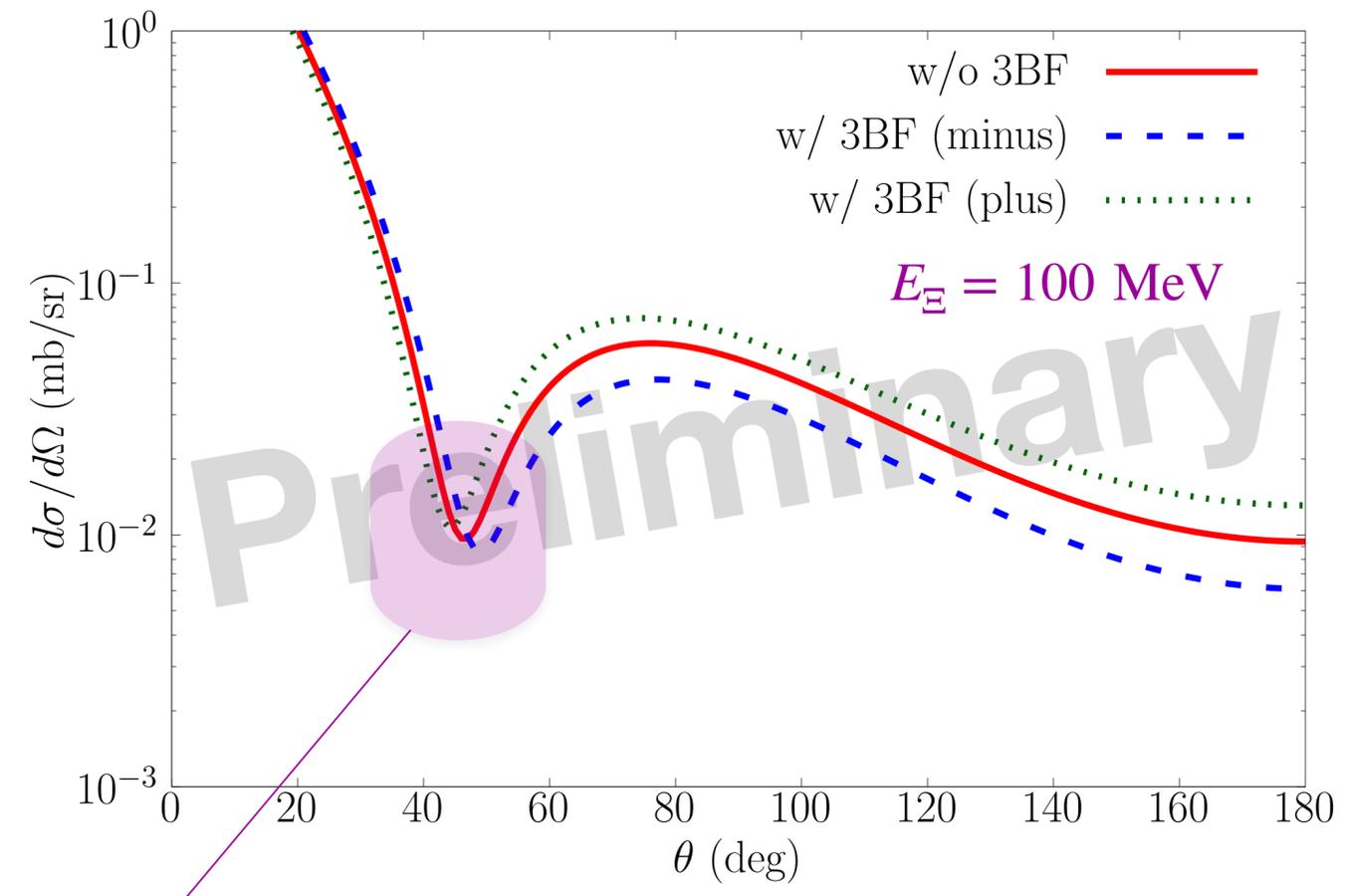
Preliminary

$d + p$ scattering



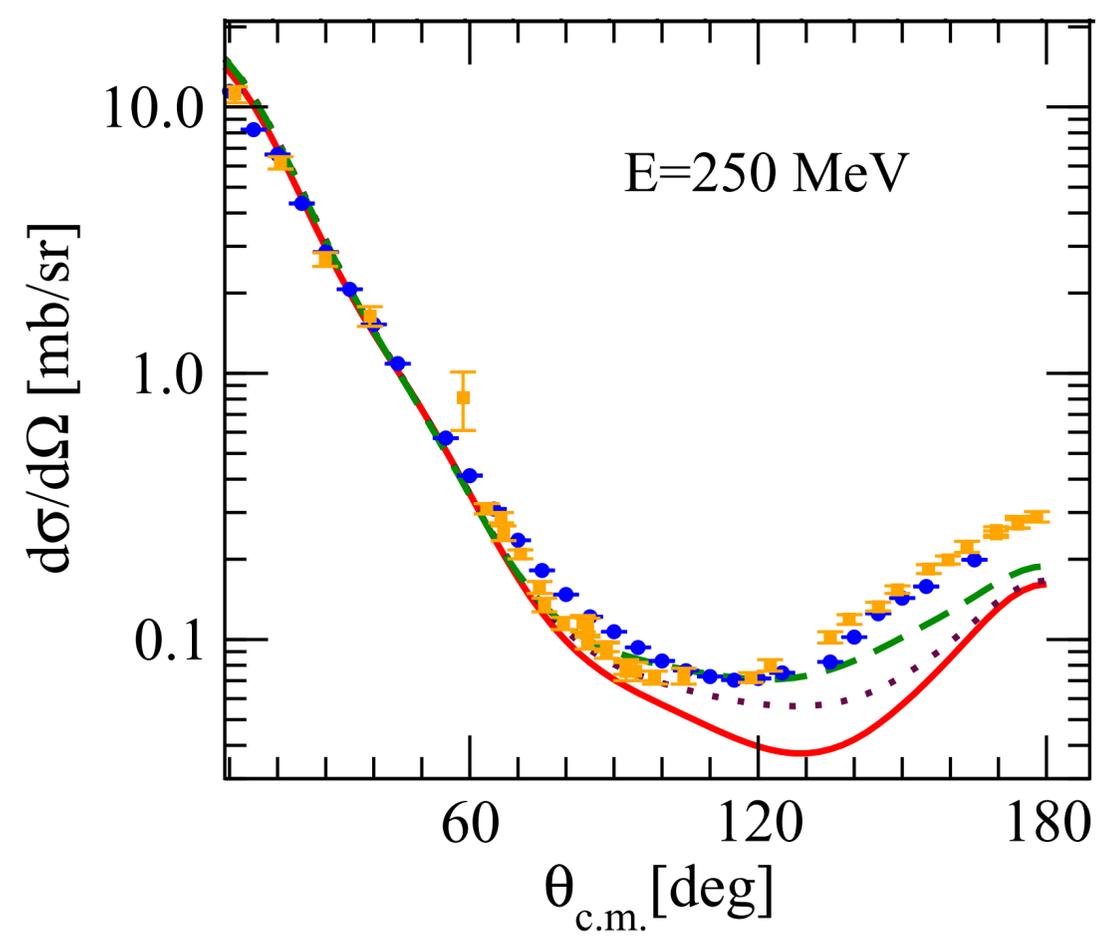
Witała +, PRC 105, 054004 (2022)

$d + \Xi^-$ scattering



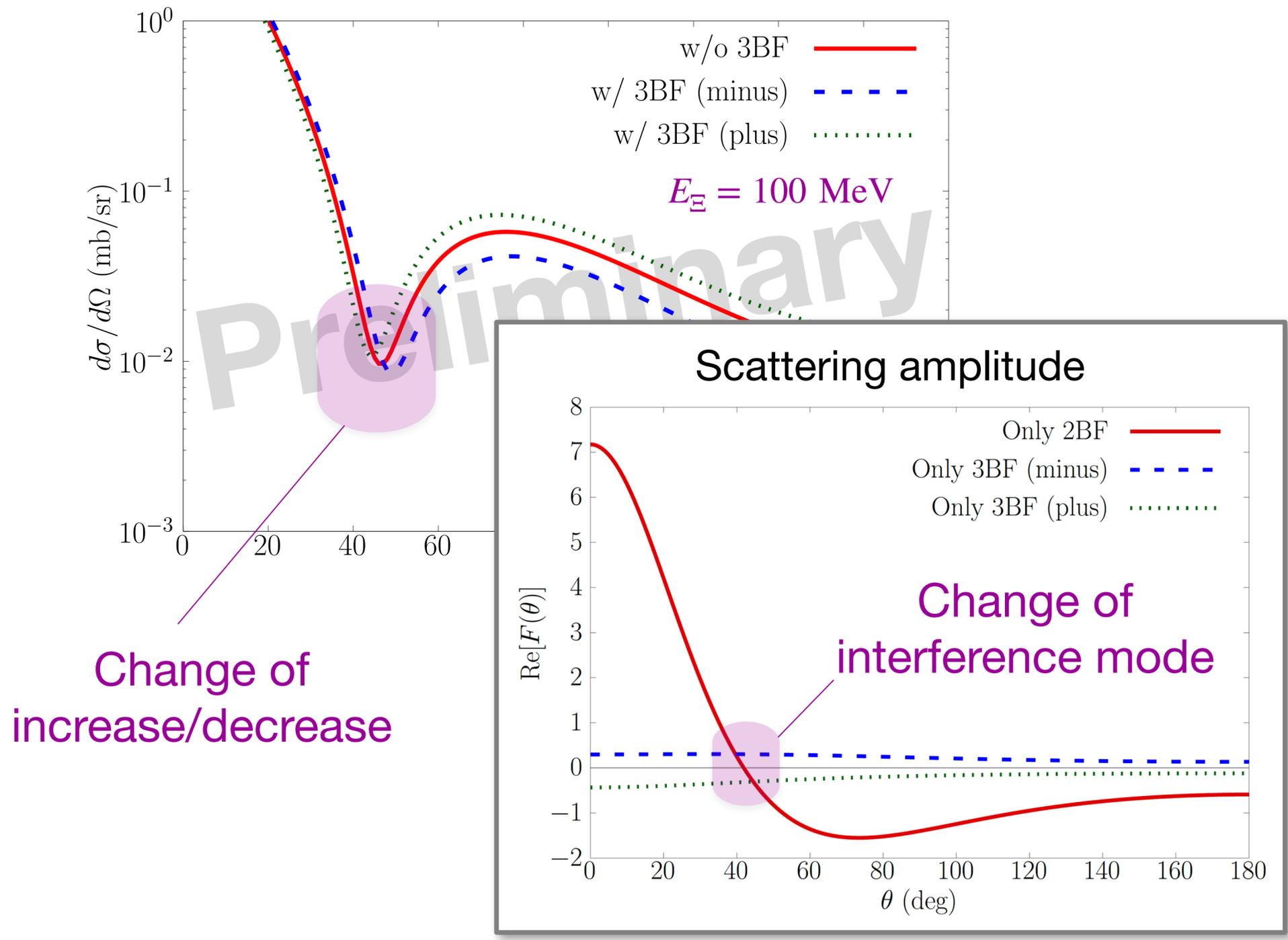
Change of increase/decrease

$d + p$ scattering



Witała +, PRC 105, 054004 (2022)

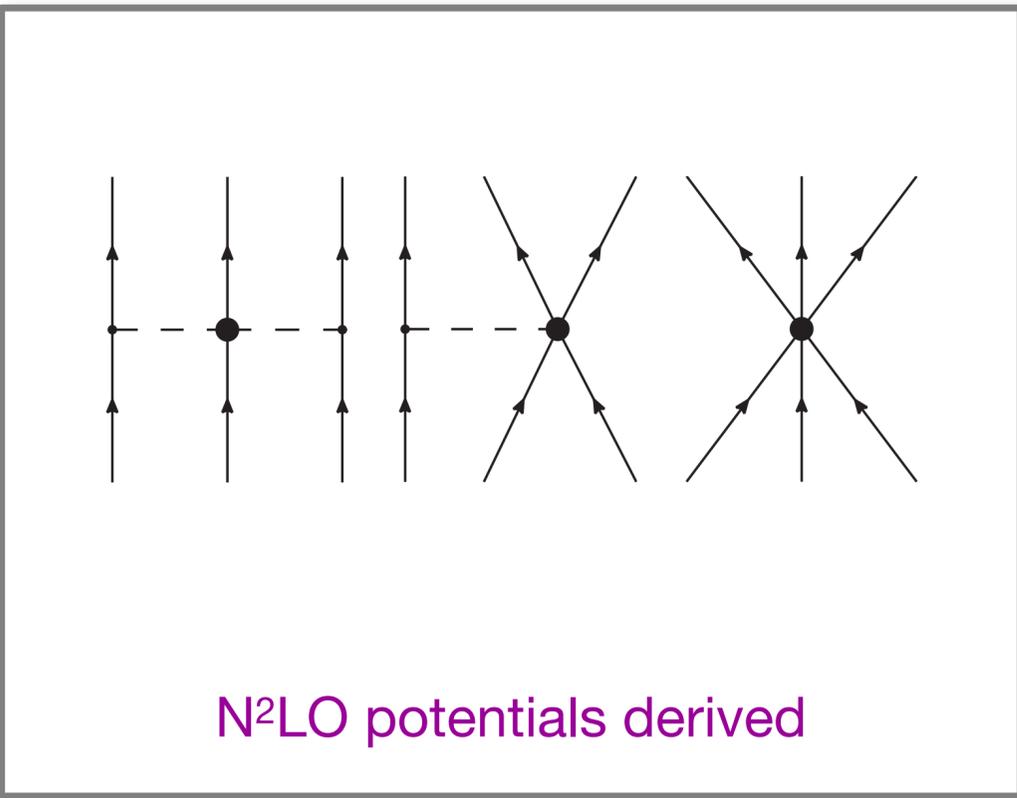
$d + \Xi^-$ scattering





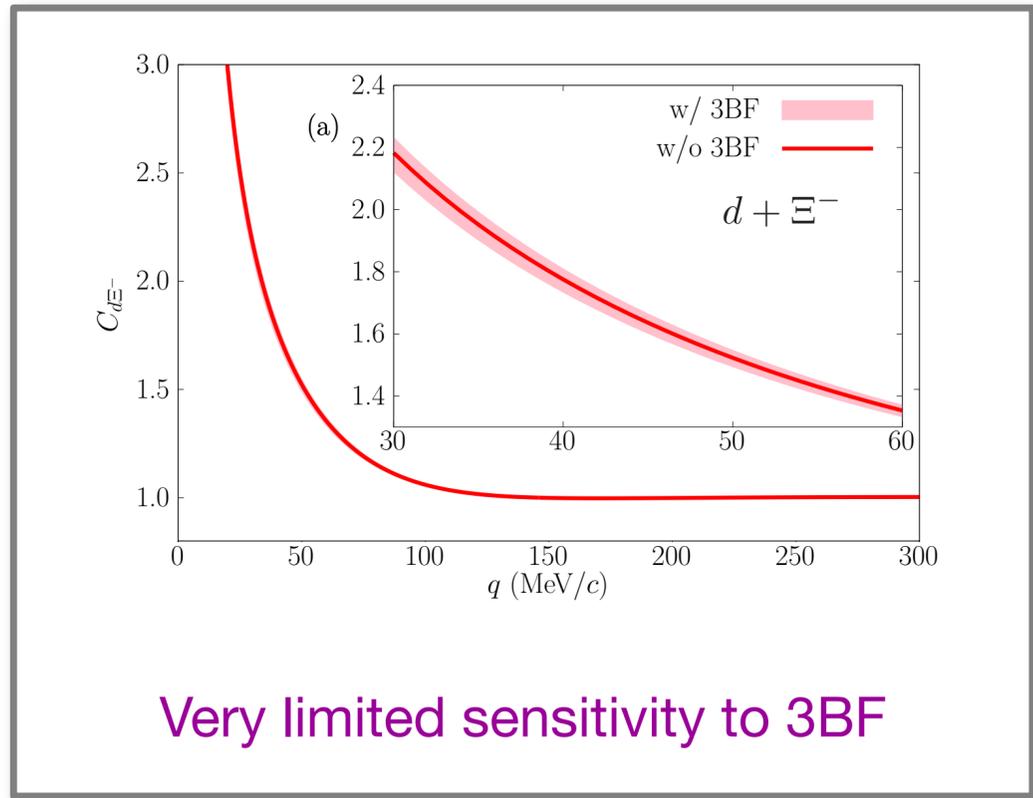
Uratsu +, PRC 113, 015204 (2026)

ΞNN 3BF from SU(3) chiral EFT



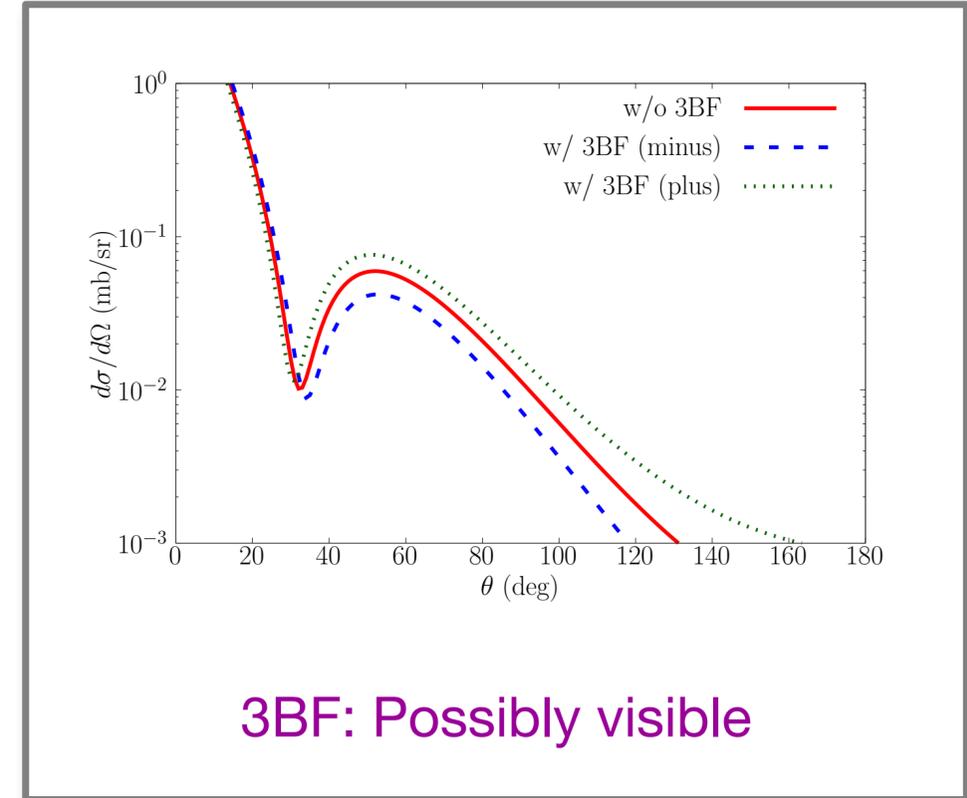
N²LO potentials derived

Femtoscscopy



Very limited sensitivity to 3BF

Elastic cross sections



3BF: Possibly visible