

Phase structure and dynamics of QCD at high densities

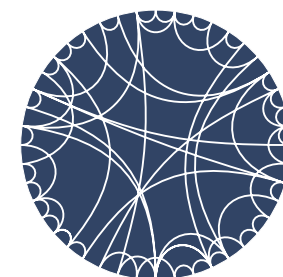
Jan M. Pawłowski

Universität Heidelberg & ExtreMe Matter Institute

Buenas Ideas on the QCD Phase Diagram, May 27th 2026



fqcd-collaboration.github.io



STRUCTURES
CLUSTER OF
EXCELLENCE

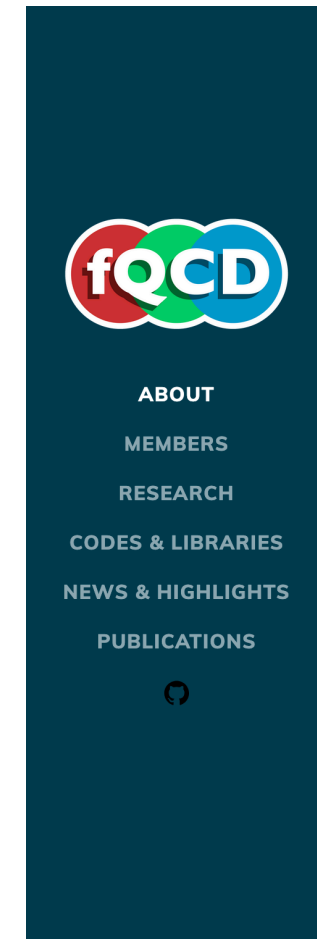


UNIVERSITÄT
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SEIT 1386



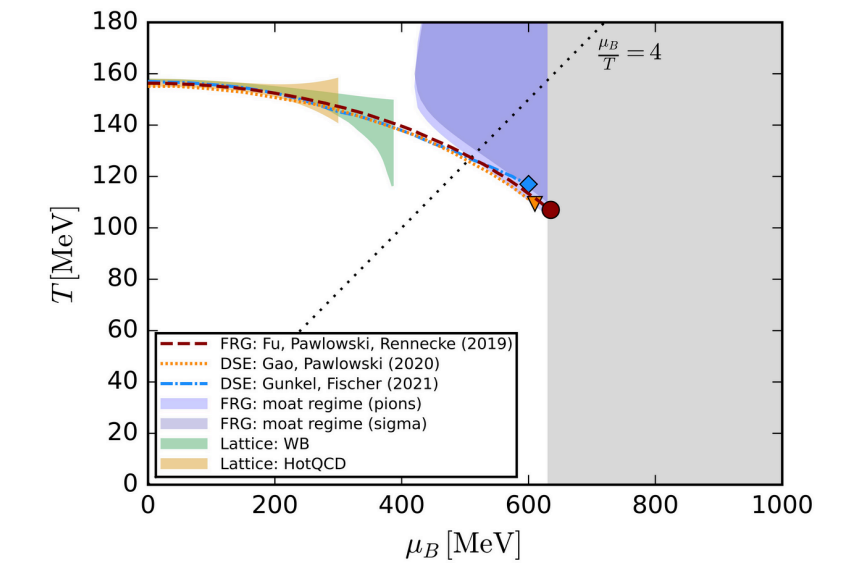


fQCD collaboration



fQCD COLLABORATION

We study the phase structure, thermodynamics and transport properties of strongly interacting matter. In order to access the notoriously difficult regimes of QCD, finite density and real time, we develop first-principles functional approaches with a focus on the functional renormalisation group and Dyson-Schwinger equations.



[github](#)

Dalian, Beijing, Darmstadt, Heidelberg, Gießen

Braun, Chen, Fu, Gao, Huang, Ihssen, Kockler, Lu, Pawłowski, Rennecke, Sattler, Stoll, Tan, Wang, Wen, Wessely, Yin, Zheng, Zorbach

Functional renormalisation group

$$\partial_t \Gamma_k[\phi] = \frac{1}{2} \left(\text{glue quantum fluctuations} - \text{quark quantum fluctuations} \right) + \frac{1}{2} \left(\text{hadronic quantum fluctuations} \right)$$

The diagram shows the FRG equation for the effective action Γ_k . It consists of three terms: a glue loop (orange wavy line), a quark loop (black solid line), and a hadronic loop (blue double line). Each loop has a diamond-shaped regulator operator \square on top.

Dyson-Schwinger equations

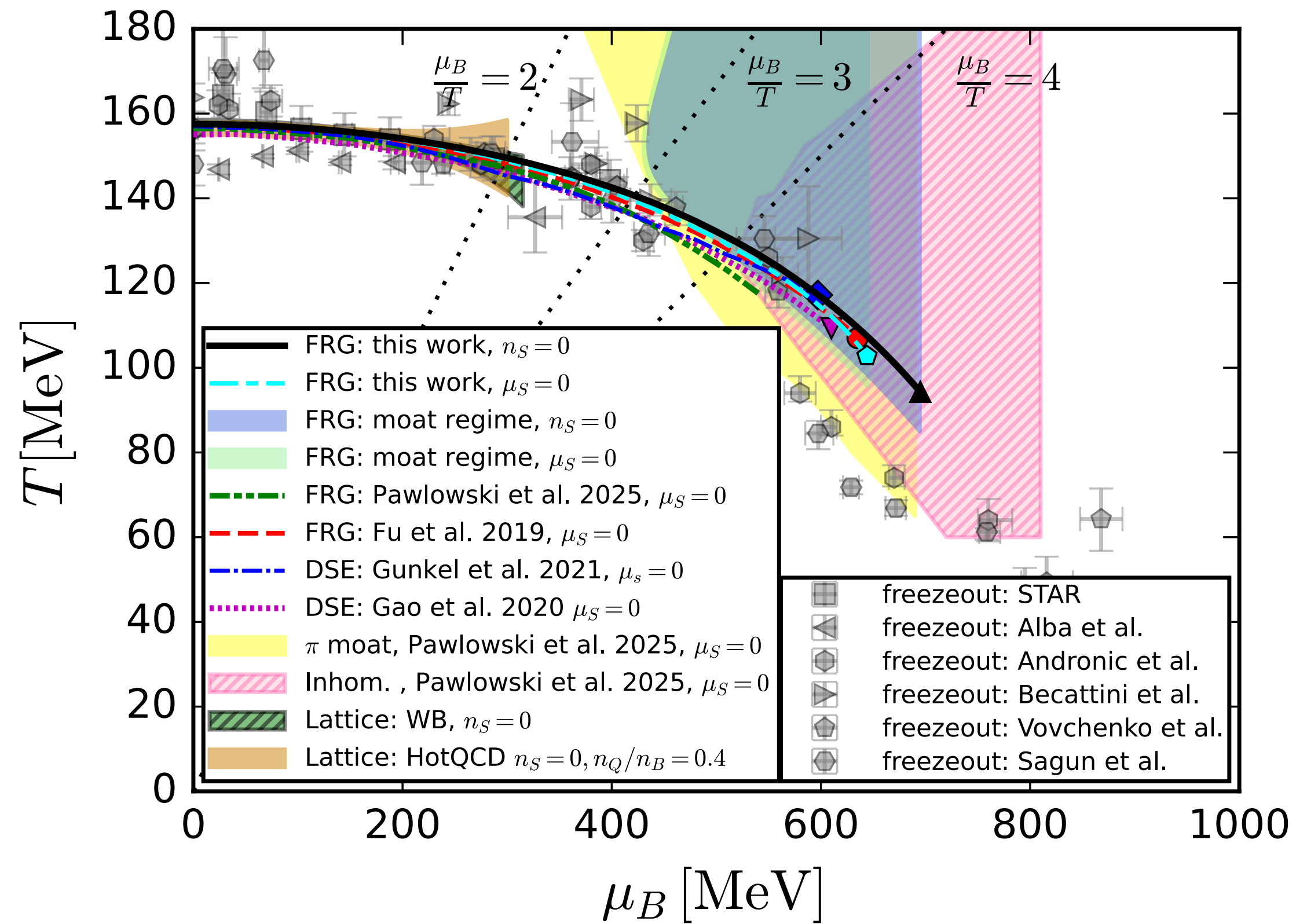
$$\frac{\delta(\Gamma - S)}{\delta A_0} = \frac{1}{2} \left(\text{glue loop} - \text{quark loop} \right) - \frac{1}{6} \left(\text{glue self-energy} + \text{quark self-energy} \right)$$

The diagram shows the Dyson-Schwinger equation for the gluon self-energy. It includes a gluon loop (orange wavy line), a quark loop (black solid line), and a ghost loop (dashed line). The right-hand side also includes diagrams for the self-energy corrections to the gluon and quark lines.

Phase structure and dynamics of QCD at high densities

- **Critical end point and new phases: where do we stand?**
- **Strong correlations above the chiral crossover**
- **Ripples of the critical and point and new phases**
- **QCD moat and inhomogeneous phases**

Critical end point and new phases: where do we stand?

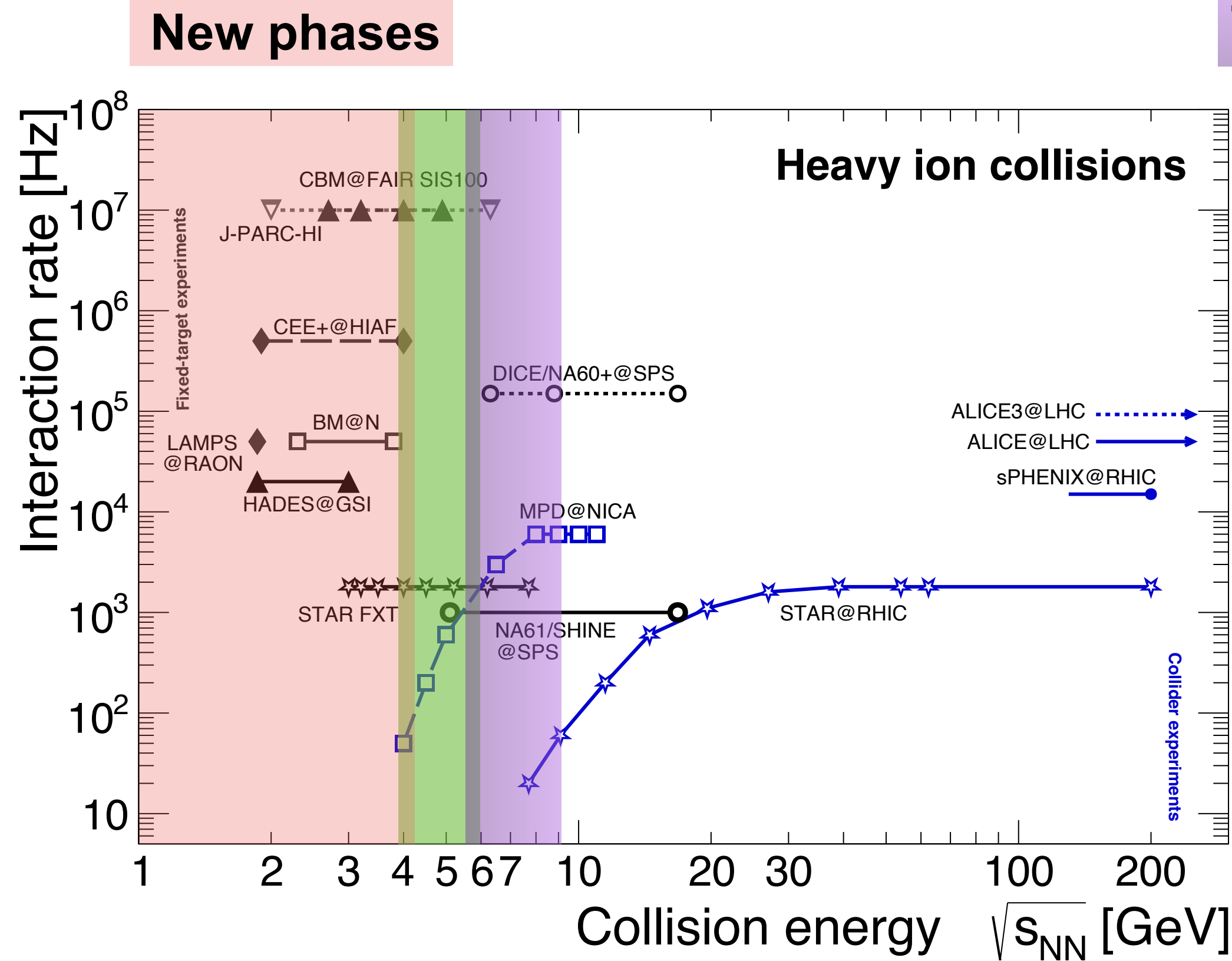


Experimental & Theoretical Landscape

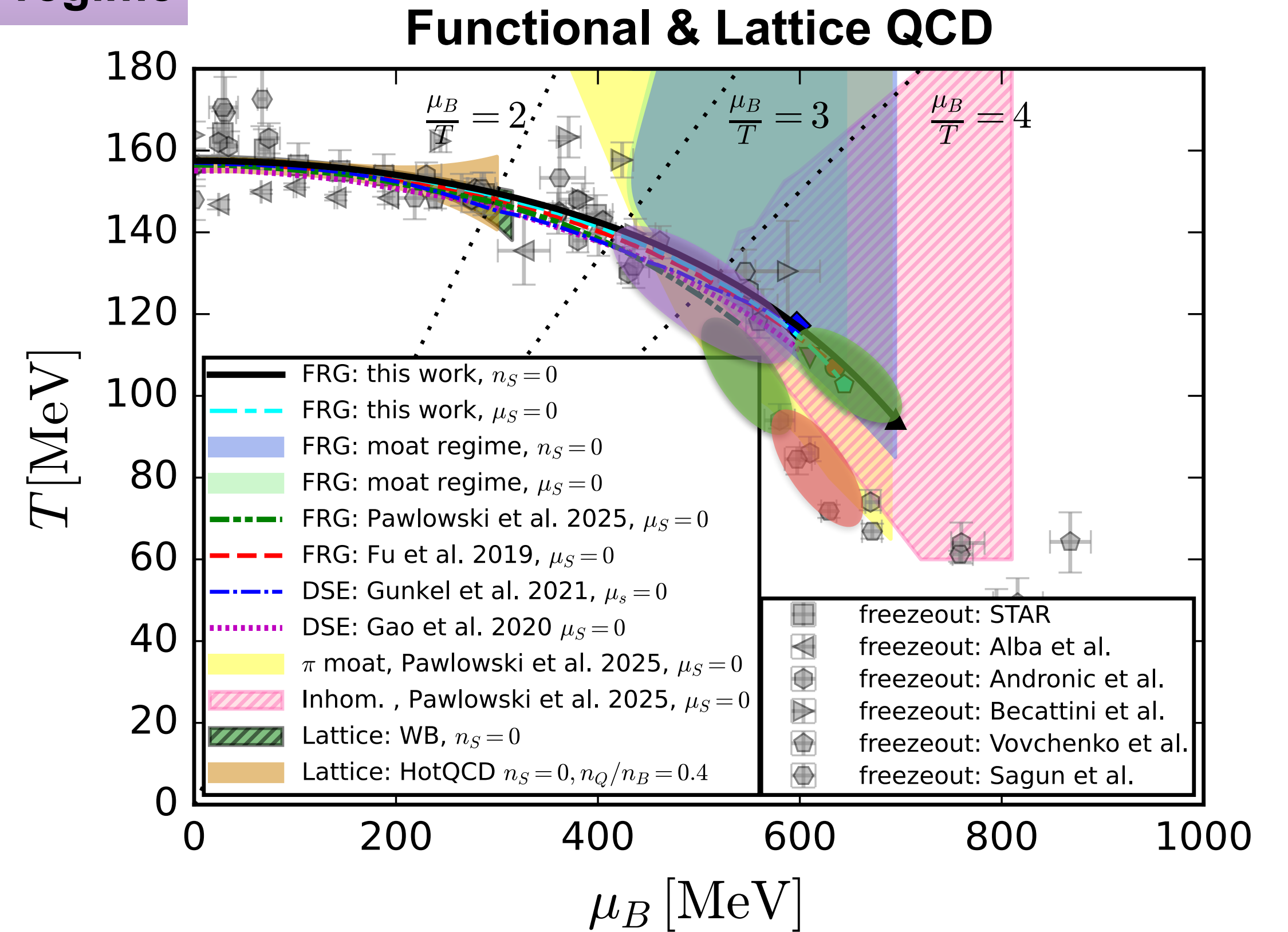
Experimental landscape

Theoretical landscape

Onset of new phases on the chiral transition line (CEP)



Transition regime



Peak of kurtosis on the freeze-out line

Critical end point and new phases: where do we stand?

Quantitative functional QCD

$$\frac{\mu_B}{T} \lesssim 4.5$$

Functional QCD: CEP estimate

$$\mu_u = \mu_d = \mu_s$$

fQCD Fu, JMP, Rennecke, PRD 101 (2020) 054032 (fRG)

fQCD Gao, JMP, PLB 820 (2021) 136584 (DSE)

$$\mu_u = \mu_d \quad \mu_s = 0$$

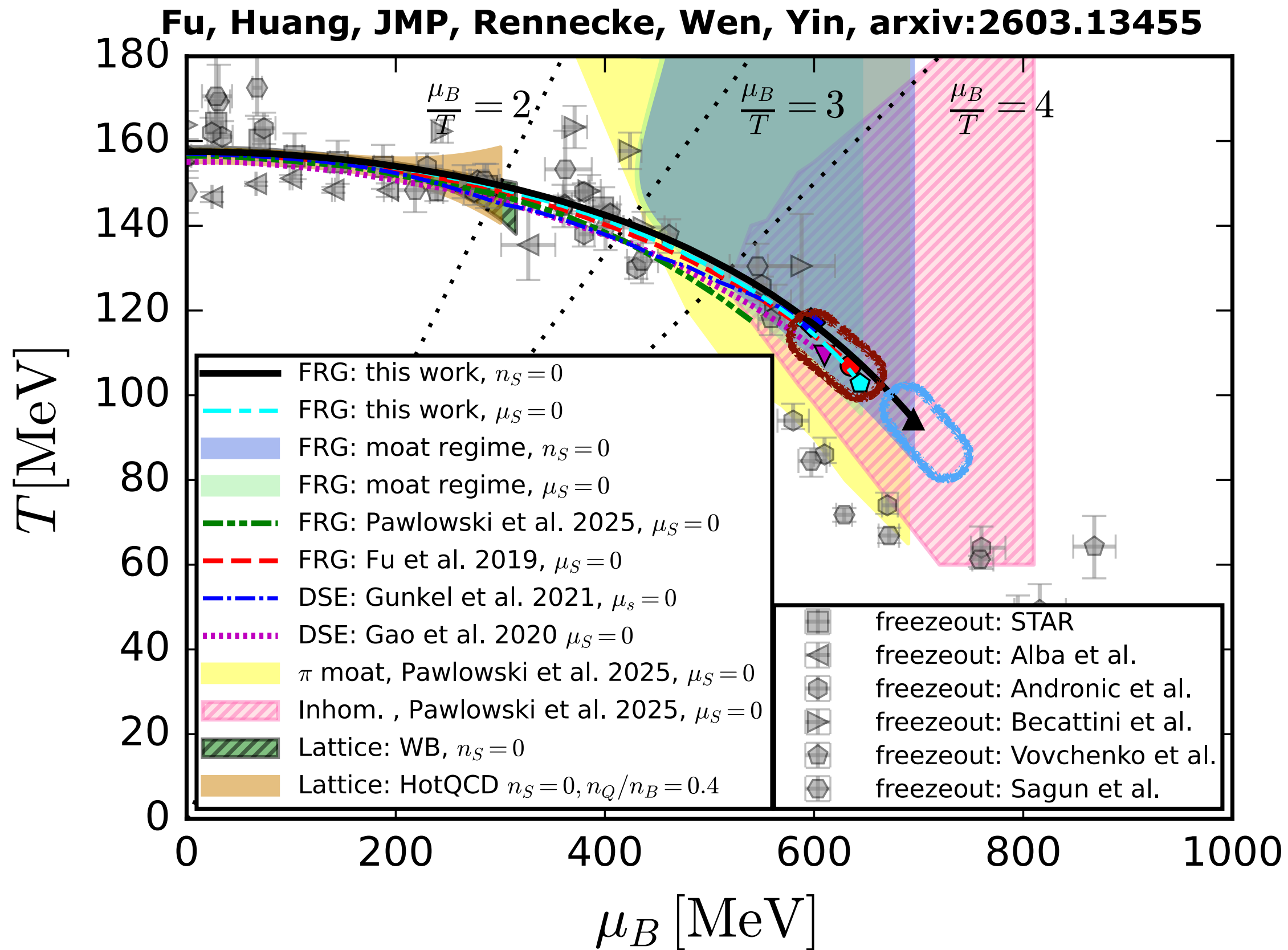
Gunkel, Fischer, PRD 104 (2021) 054022 (DSE)

$$(\mu_B, T)_{\text{CEP}} \sim (105 - 115, 600 - 650) \text{ MeV}$$

Strangeness neutrality

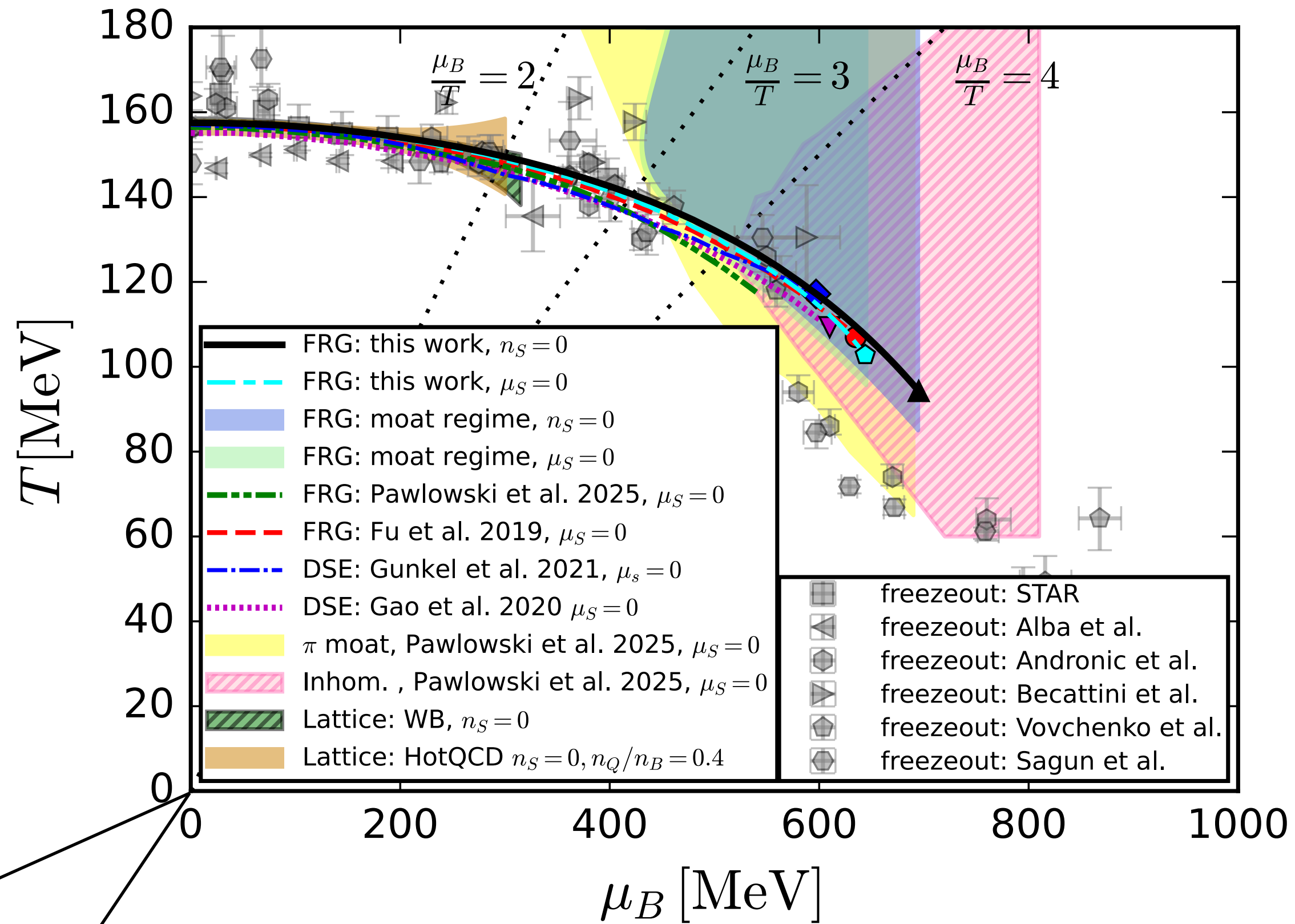
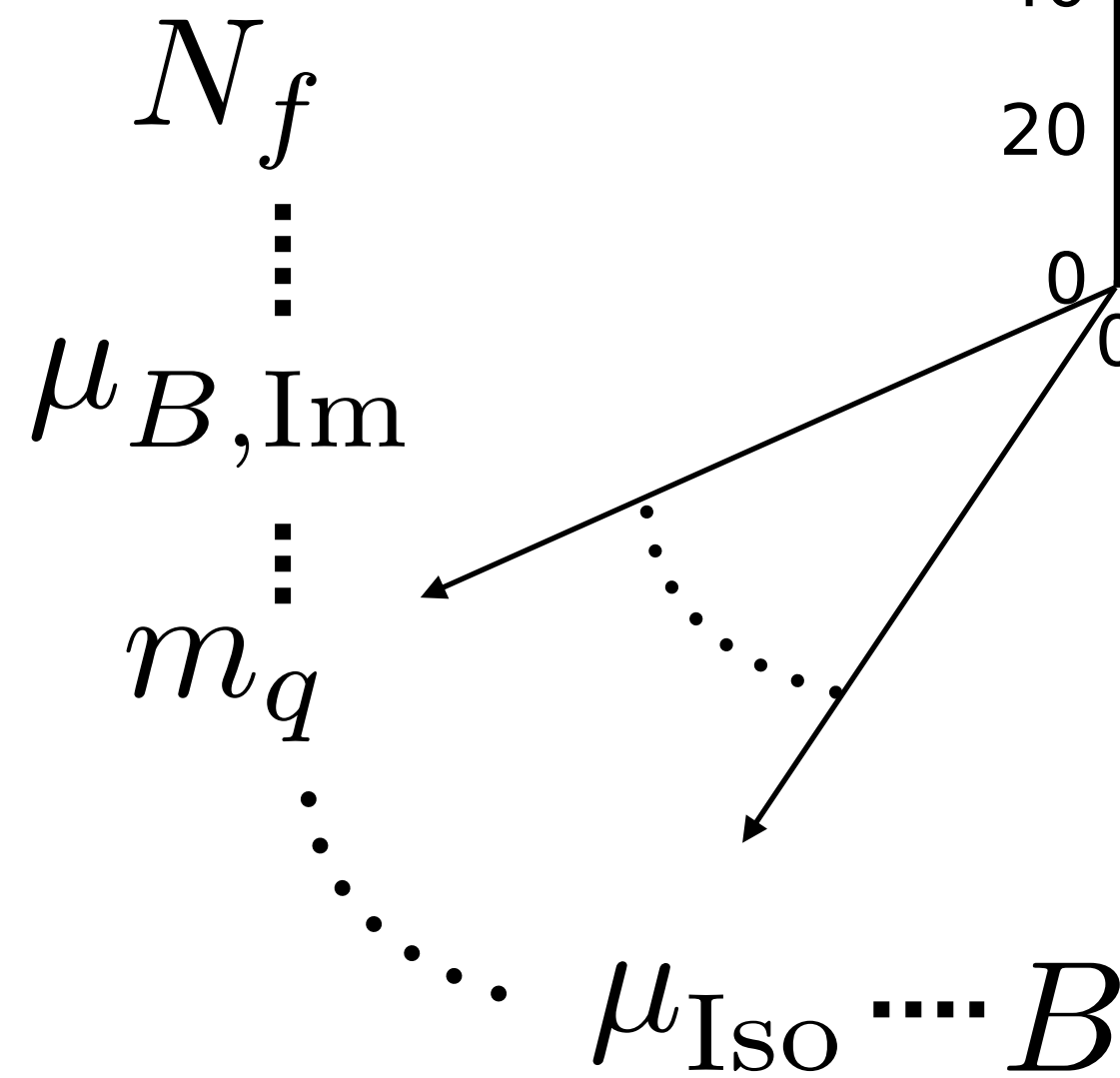
$$(\mu_B, T)_{\text{CEP}} = (92, 696) \text{ MeV}$$

$$\frac{\kappa_{n_s=0}}{\kappa_{\mu_i=\mu_q}} = 0.897$$



Critical end point and new phases: where do we stand?

See talks of
Christian, Álvaro



Collect all possible information/structure
for
physics understanding & extrapolations

$$\mu_u = \mu_d = \mu_s$$

$$\mu_u = \mu_d \quad \mu_s = 0$$

$$(\mu_B, T)_{\text{CEP}} \sim (105 - 115, 600 - 650) \text{ MeV}$$

Strangeness neutrality

$$(\mu_B, T)_{\text{CEP}} = (92, 696) \text{ MeV}$$

Lattice

HotQCD:

Bazavov, Ding, Hegde, Kaczmarek, Karsch, Karthik, Laermann, Lahiri, Larsen, Li, Mukherjee, Ohno, Petreczky, Sandmeyer, Schmidt, Sharma, Steinbrecher, PLB 795 (2019)

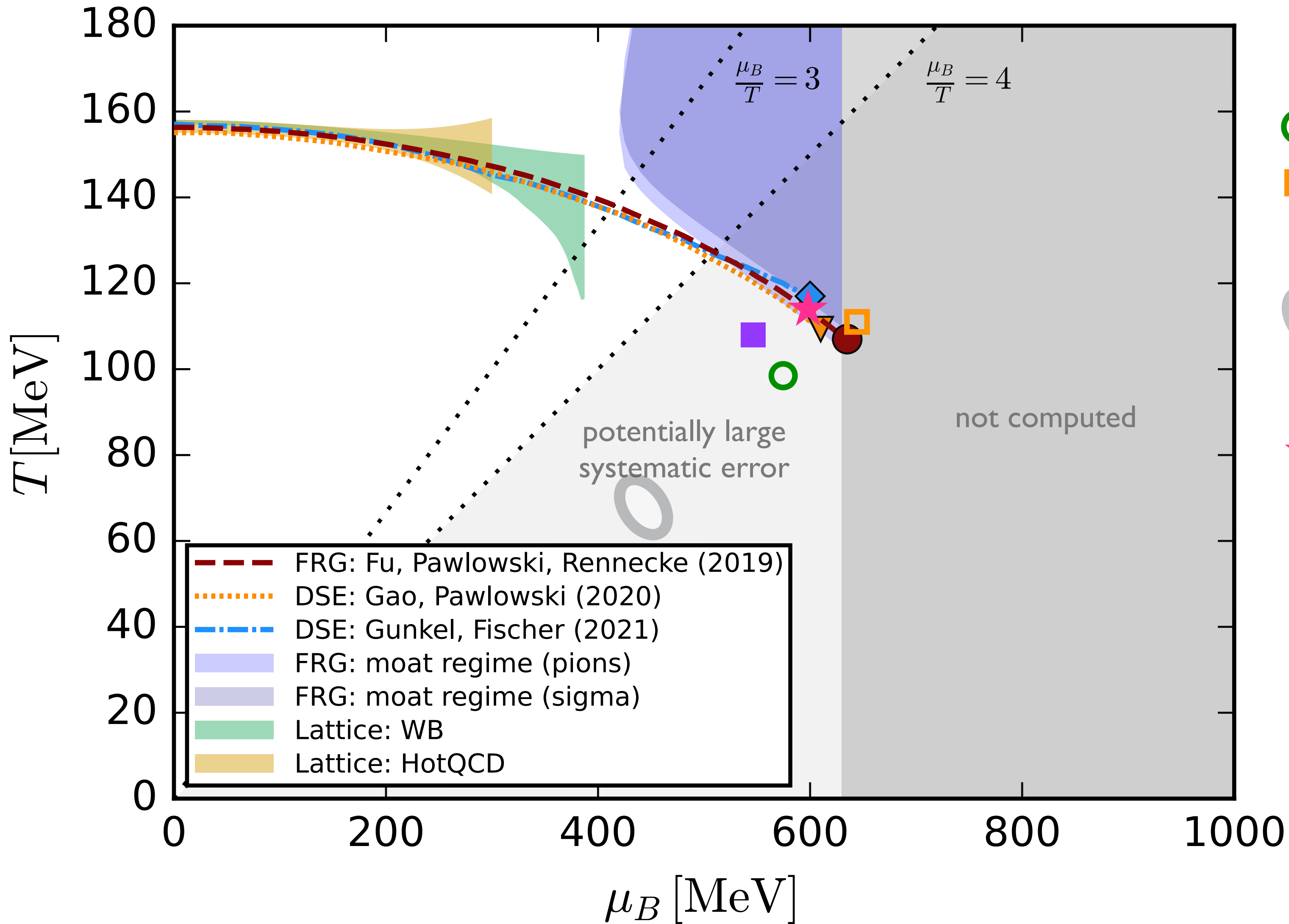
WB:

Borsányi, Fodor, Guenther, Kara, Katz, Parotto, Pasztor, Ratti, Szabo, PRL 125 (2020) 052001

QCD PHASE DIAGRAM & THE CEP

Modified from Fabian Rennecke's plenary talk @ QM 2025

FRG & DSE results corroborated by subsequent "extrapolations" of lattice data



using Yang-Lee edge singularities:

- conformal Padé [Basar, 2312.06952]
- multi-point Padé [Clarke et al., 2405.10196]
 $N_\tau = 6, 8$ results + continuum estimate [Schmidt, 2504.00629]
- very recent lattice extrapolation ($16^3 \times 8$) [Adam et al, 2507.13254]

using thermodynamics:

- ★ constant entropy density [Shah et al. 2410.16206]
- See talk of Volodymyr [Shah et al. 2601.08823]

model-based extrapolation (tiny selection):

- holography [Hippert et al., 2309.00579]
(agrees with [Cai et al., 2201.02004])

CEP location well constrained by now. And it's in **FAIR** range!

$$\sqrt{s_{NN}} \approx 3.6 - 4.1 \text{ GeV}$$



Extrapolations & von Neumann's Elephant

Extrapolations are ill-conditioned problems

Those are my interpretations,
and if you don't like them....
well, I have others

'... and now for something
completely different...'



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Extrapolations are ill-conditioned problems

'There are two ways of doing calculations in theoretical physics.

One way is to have a clear physical picture of the process that you are calculating.

The other way is to have a precise and self-consistent mathematical formalism.

...You have neither'

Fermi to Dyson

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*'With four parameters I can fit an elephant,
and with five I can make him wiggle his trunk'*

Von Neumann



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*With four parameter models we can fit many data
but we cannot extrapolate without external information*

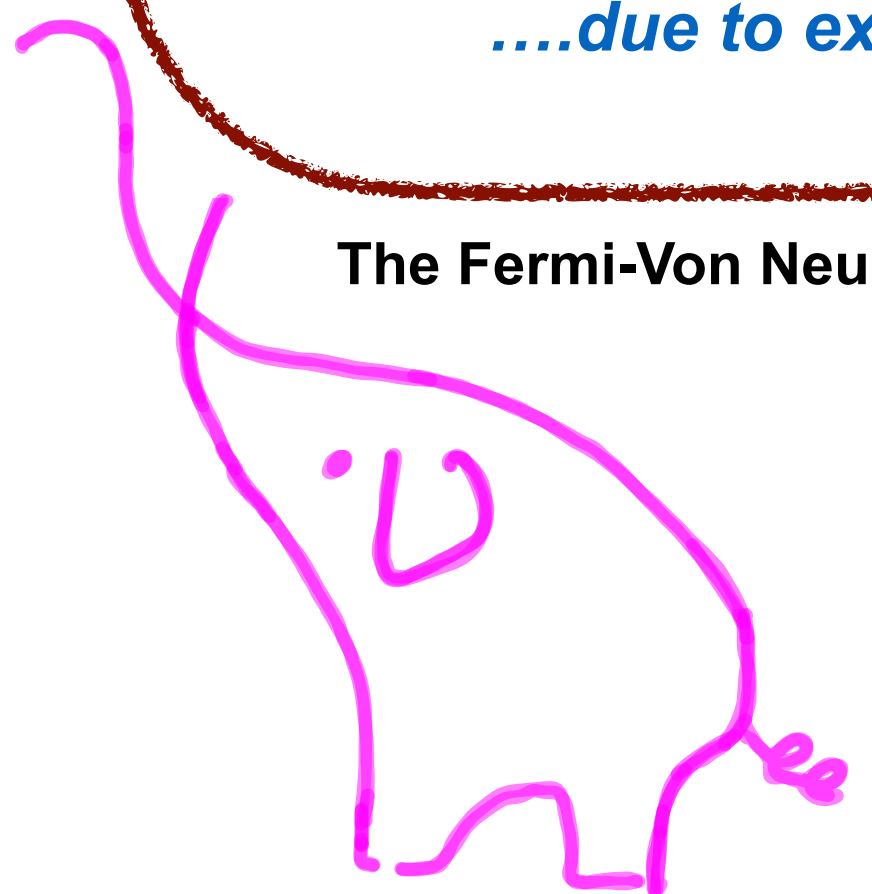
**In particular, extrapolations cannot predict the existence
and location of the CEP without external information**

*The other way is to have a precise and self-consistent
effective theory whose systematic error is under control
....due to external QCD information*

The Fermi-Von Neumann QCD phase structure elephant

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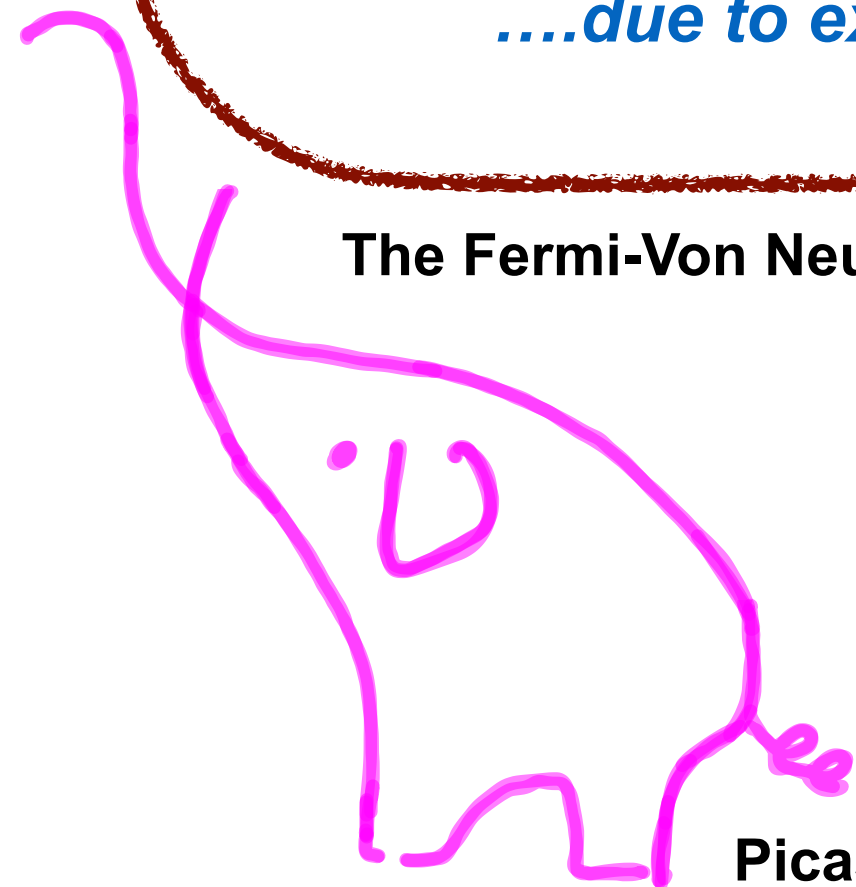
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Picasso-assisted Pawlowski elephant



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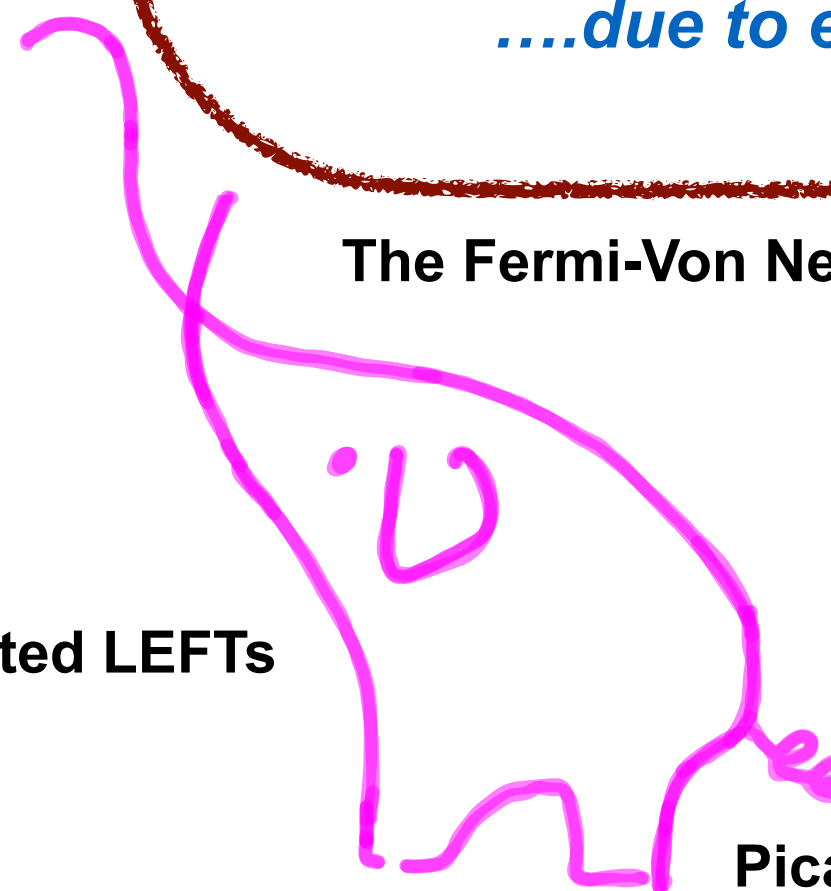
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The Fermi-Von Neumann QCD phase structure elephant

Proxy for QCD-assisted LEFTs



Picasso-assisted Pawlowski elephant



Direct computations and the minimal point of view

Those are my interpretations,
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- Self-consistent truncations to functional relations define analytic functions in μ_B , eg:

$$\partial_t \langle q(x) \bar{q}(y) \rangle_{\mu_B} = \text{Loop} \left[\langle q(x) \bar{q}(y) \rangle_{\mu_B}, \langle q(x) A_\mu(y) \bar{q}(z) \rangle_{\mu_B}, \dots ; \mu_B \right]$$

Unique: QCD-based analytic continuations
that satisfy the lattice benchmarks
at small chemical potential.



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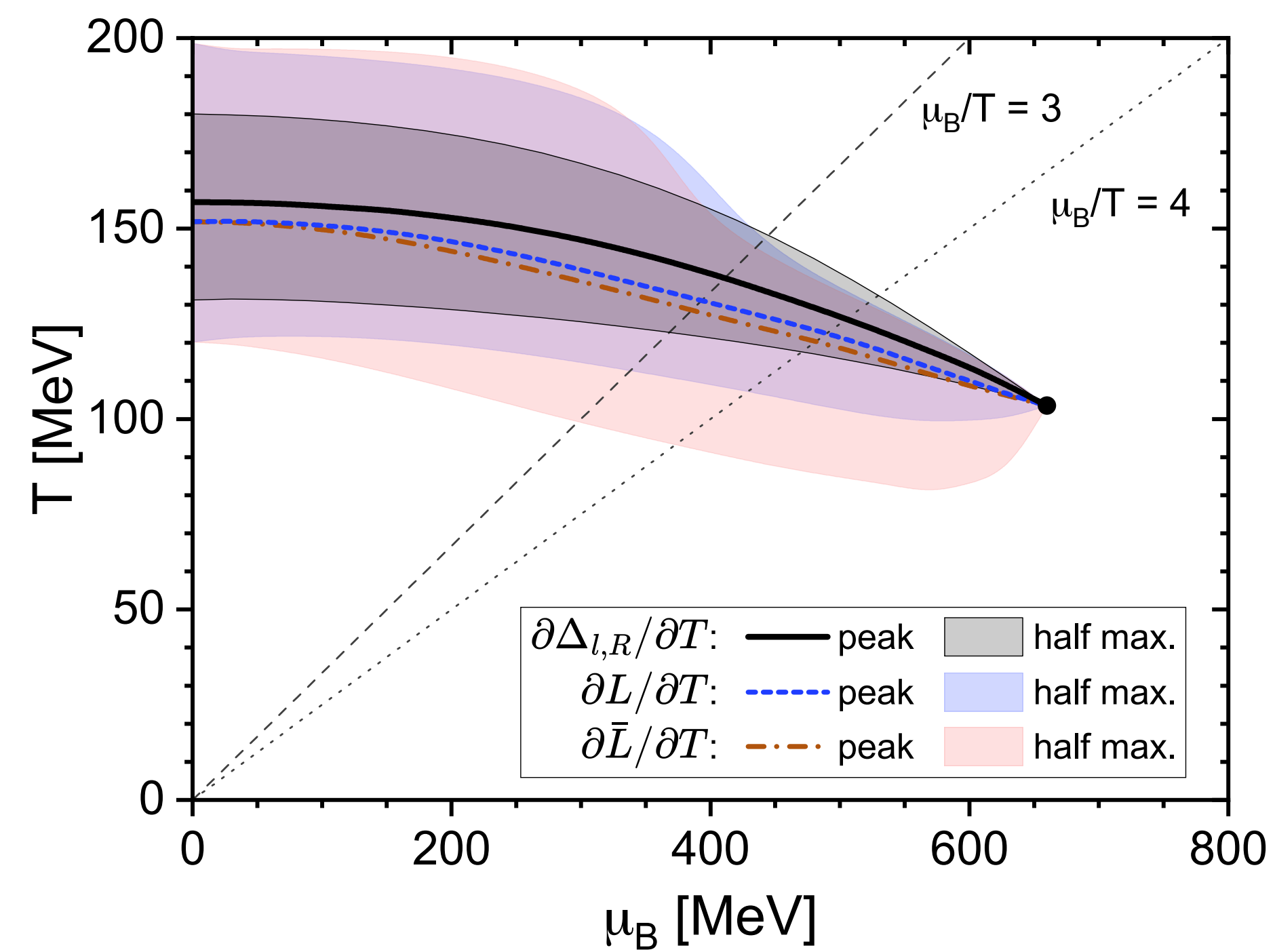
Unique: QCD-based analytic continuations
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- ? Corroborated?

By definition, LEFTs (including extrapolations) cannot assess
the existence or absence of emergent phenomena!

scales, scales, scales

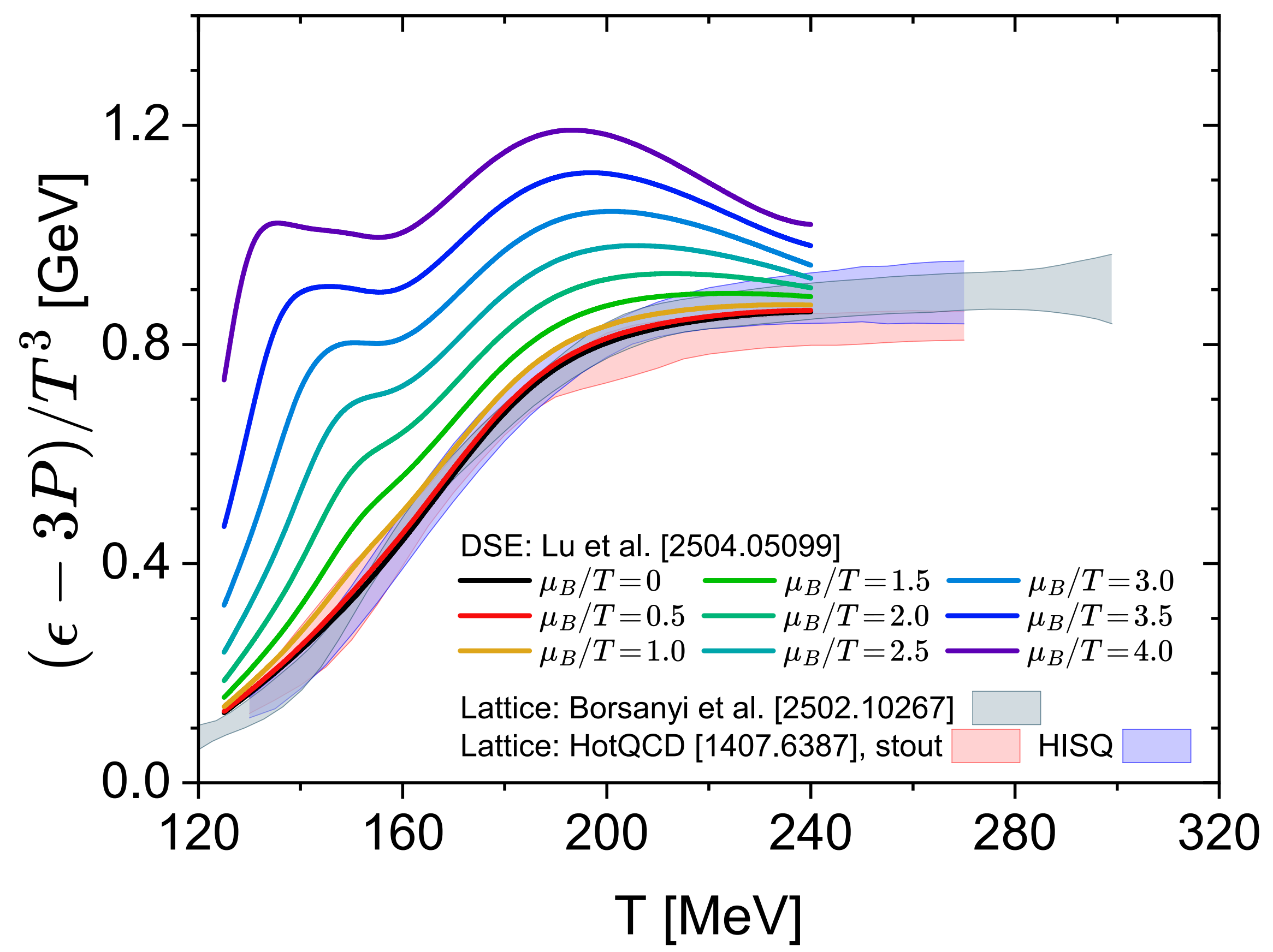
Strong correlations above the chiral crossover



scales, scales, scales

Strongly correlated physics

Strongly correlated phase for temperatures $T_\chi \lesssim T \lesssim 2T_\chi$



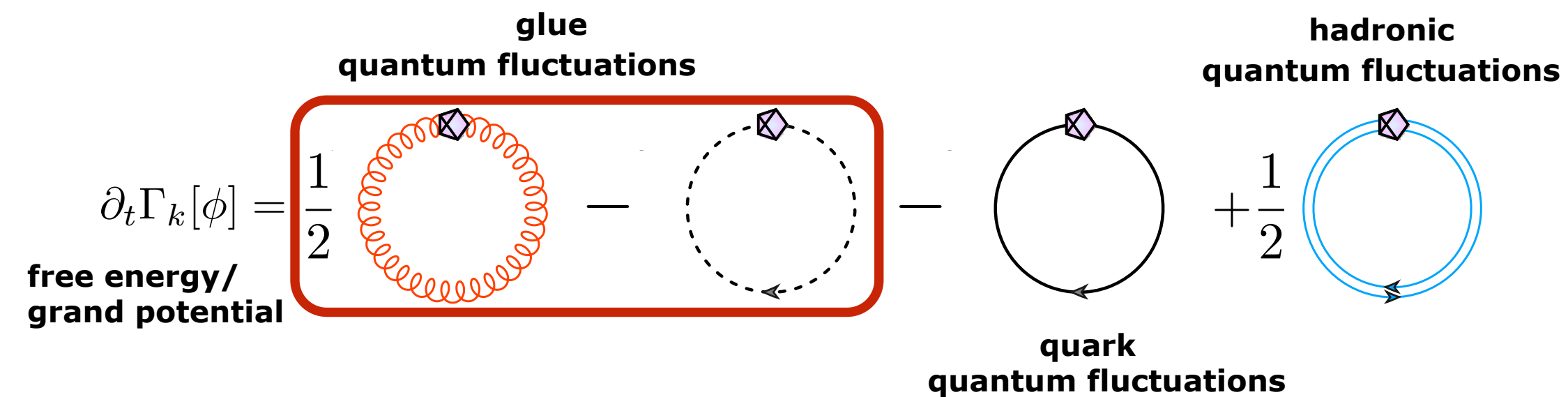
scales, scales, scales

Functional confinement & the dynamical gluonic background

FRG: Braun, Gies, JMP, PLB 684 (2010) 262

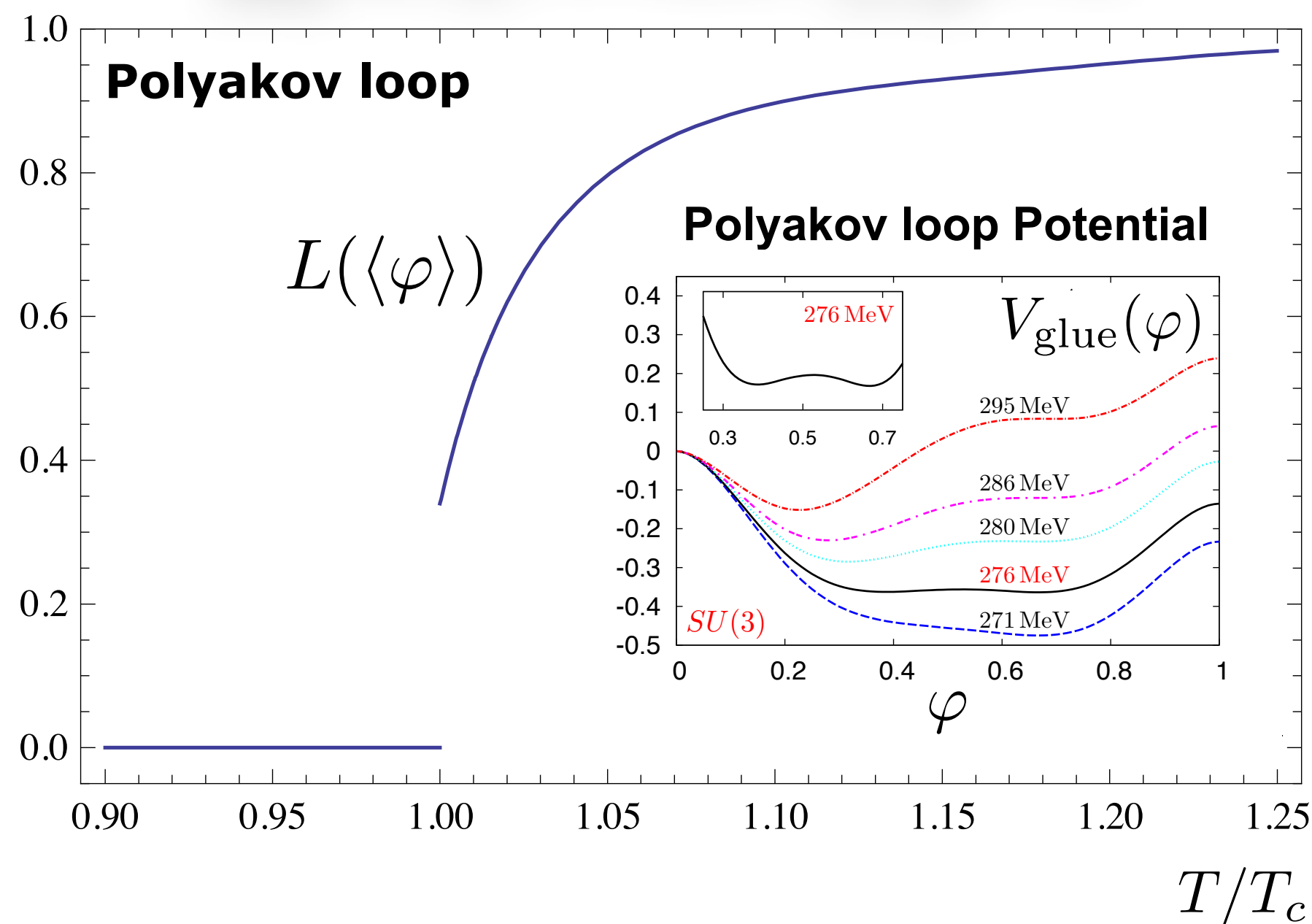
FRG, DSE, 2PI: Fister, JMP, PRD 88 (2013) 045010

$$L(A_0) = \frac{1}{N_c} \text{tr} \mathcal{P} e^{i g_s \int_0^\beta dt A_0(x)}$$



Polyakov loop Potential: $V_{\text{glue}}(\varphi)$

$$\mathcal{P} e^{i g_s \int_0^\beta dt A_0(x)} = e^{2\pi i \varphi}$$



$$T_c/\sqrt{\sigma} = 0.658 \pm 0.023$$

$$\text{lattice : } T_c/\sqrt{\sigma} = 0.646$$

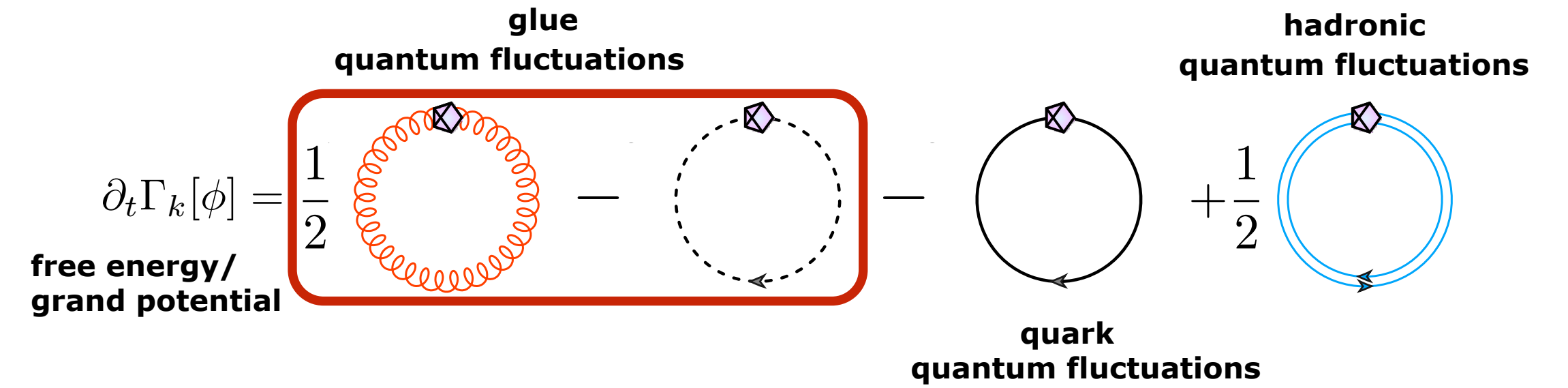
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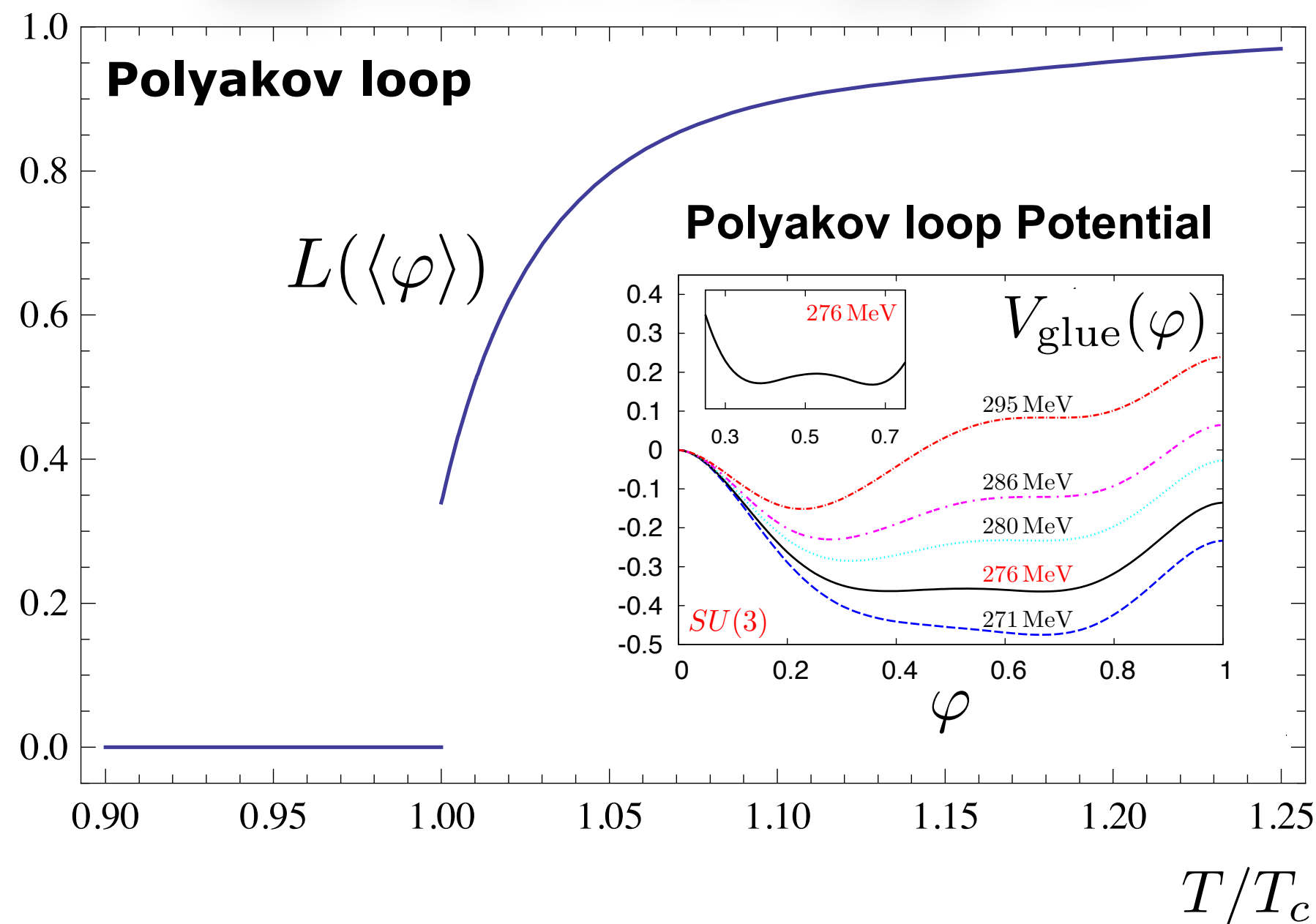
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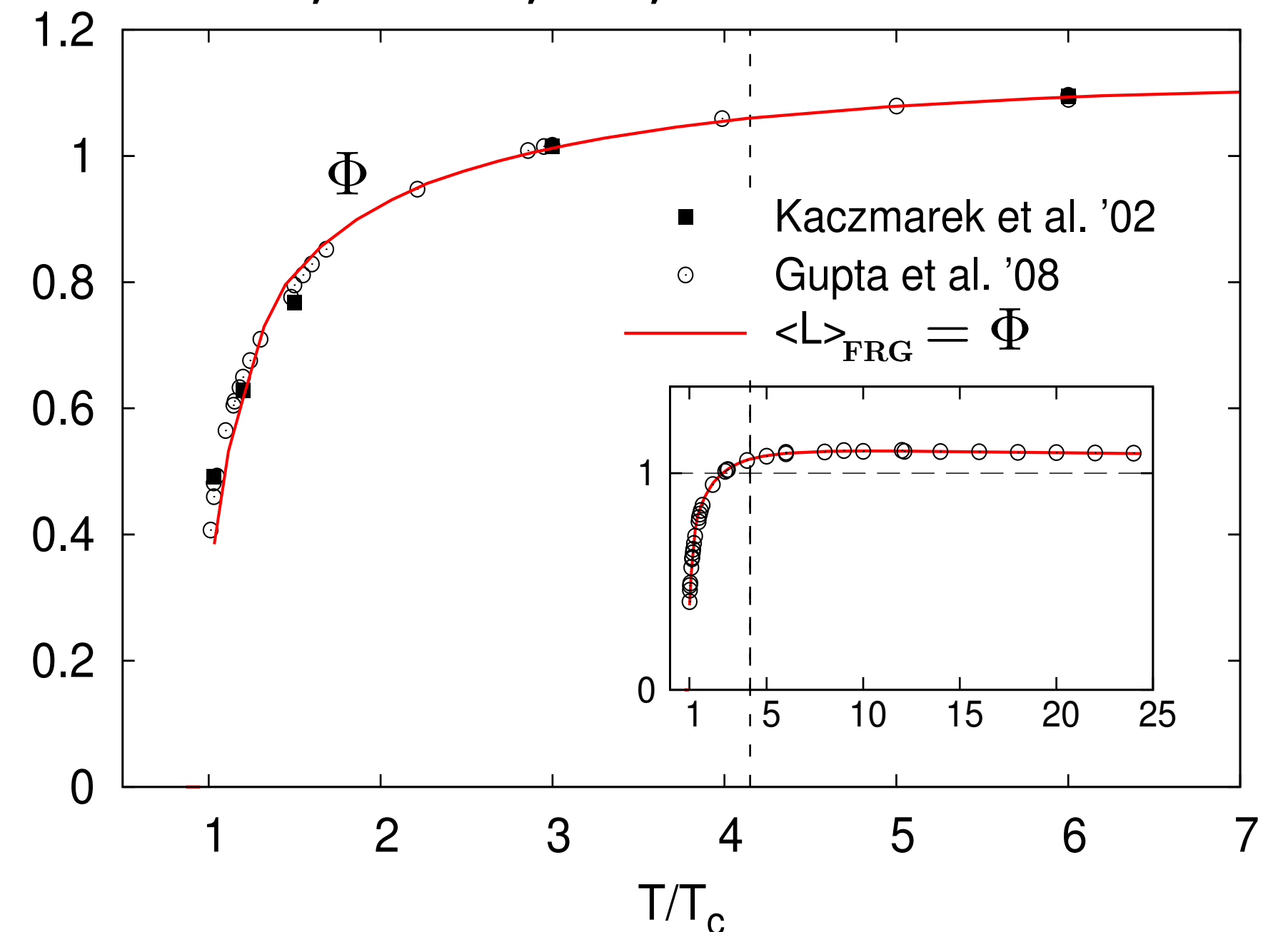


Polyakov loop Potential: $V_{\text{glue}}(\varphi)$

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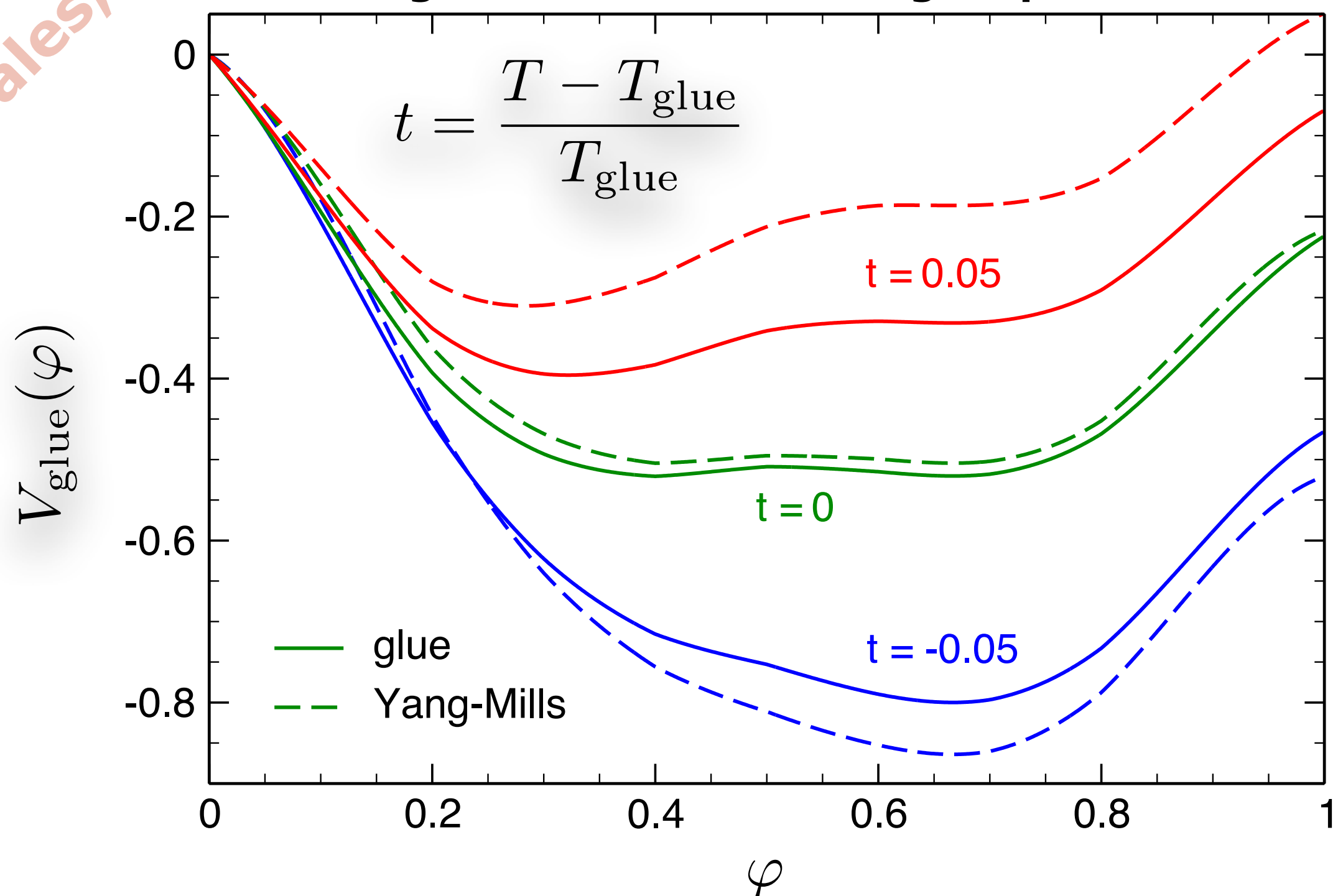
Herbst, Luecker, JMP, arXiv:1510.03830



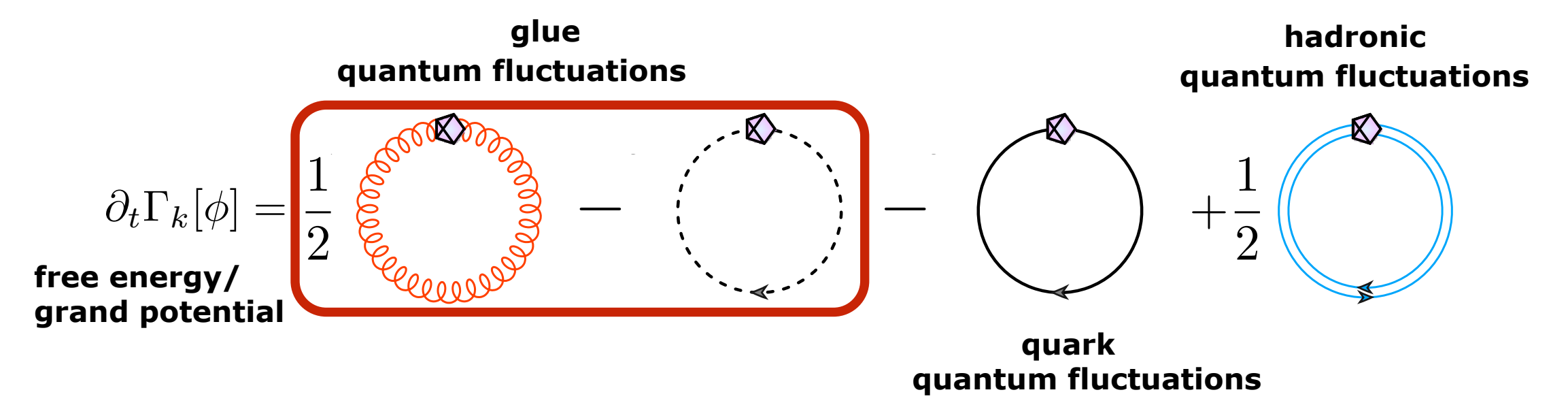
Functional confinement & the dynamical gluonic background

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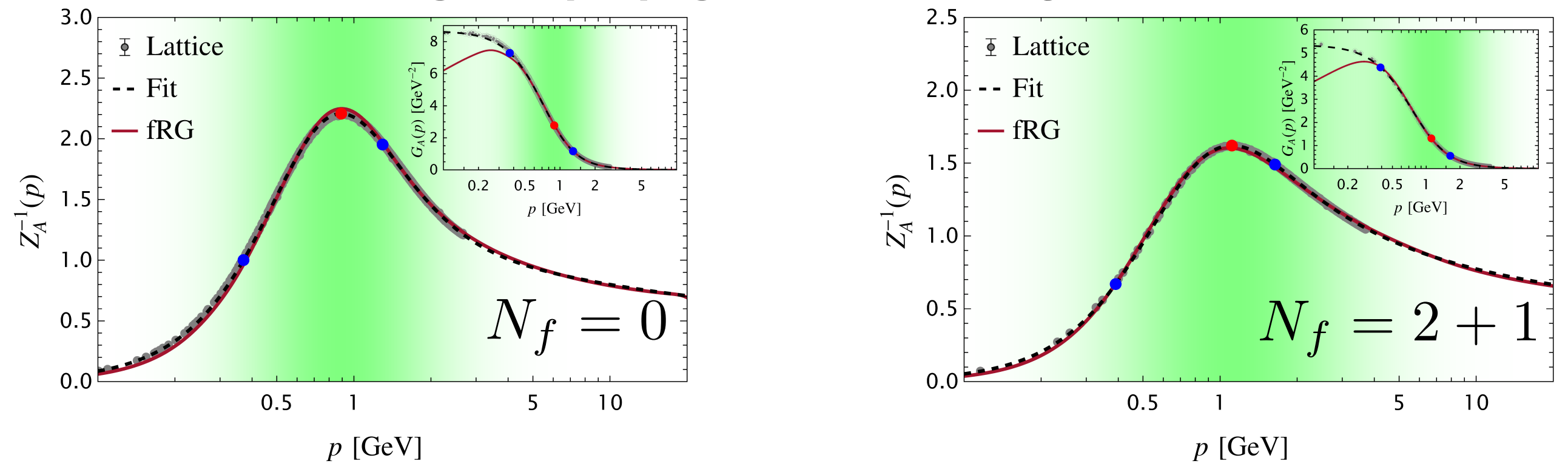
Yang-Mills vs two-flavour glue potential



Haas, Stiele, Braun, JMP, Schaffner-Bielich, PRD 87 (2013) 076004



gluon propagators in YM & QCD

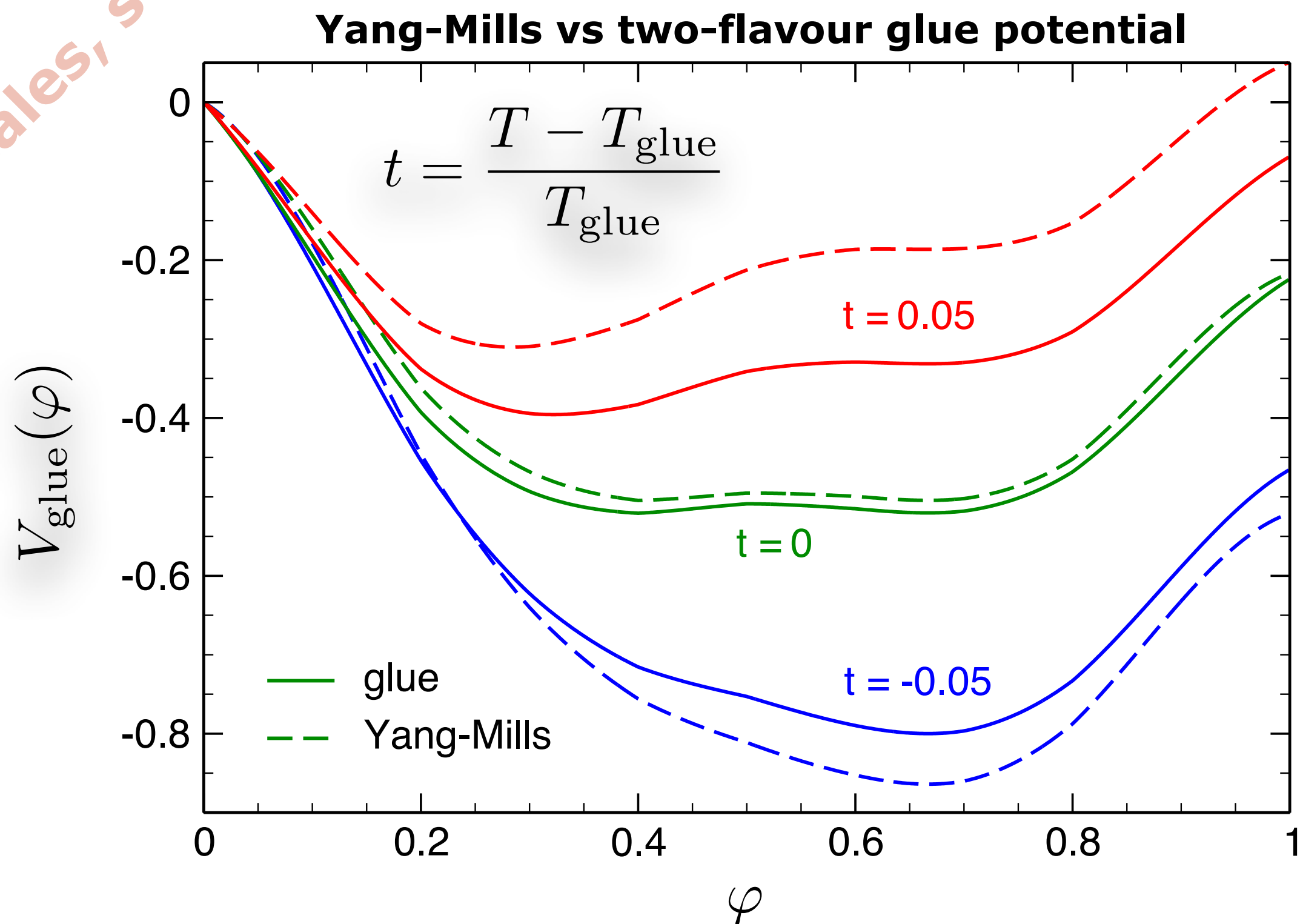


Ferreira, Papavassiliou, JMP, EPJC 85 (2025) 11, 1339

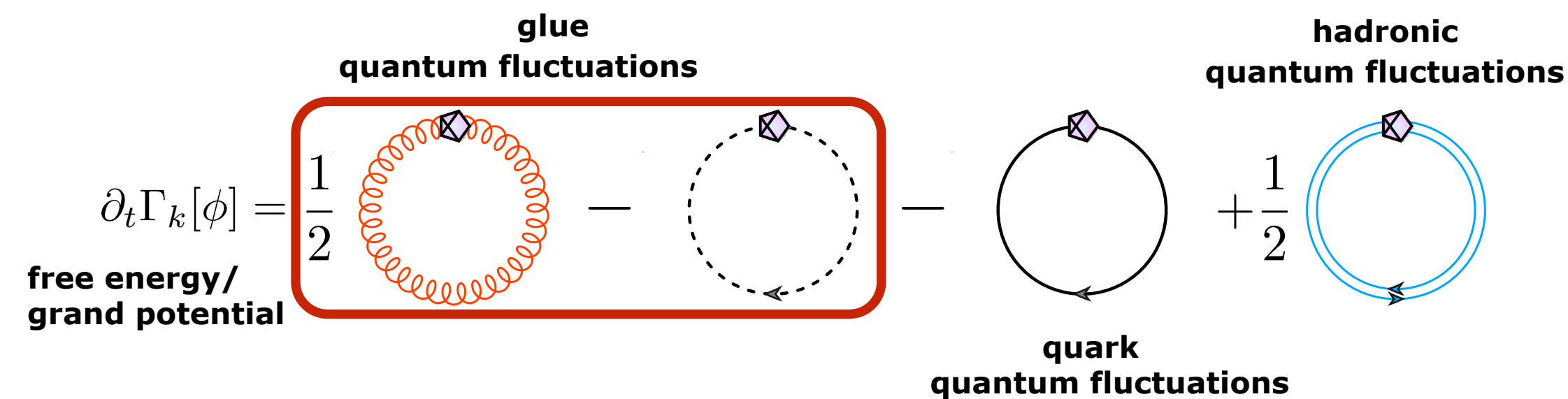
$$T_{\text{glue}}^{(\text{QCD})} \approx 200 \text{ MeV}$$

Functional confinement & the dynamical gluonic background

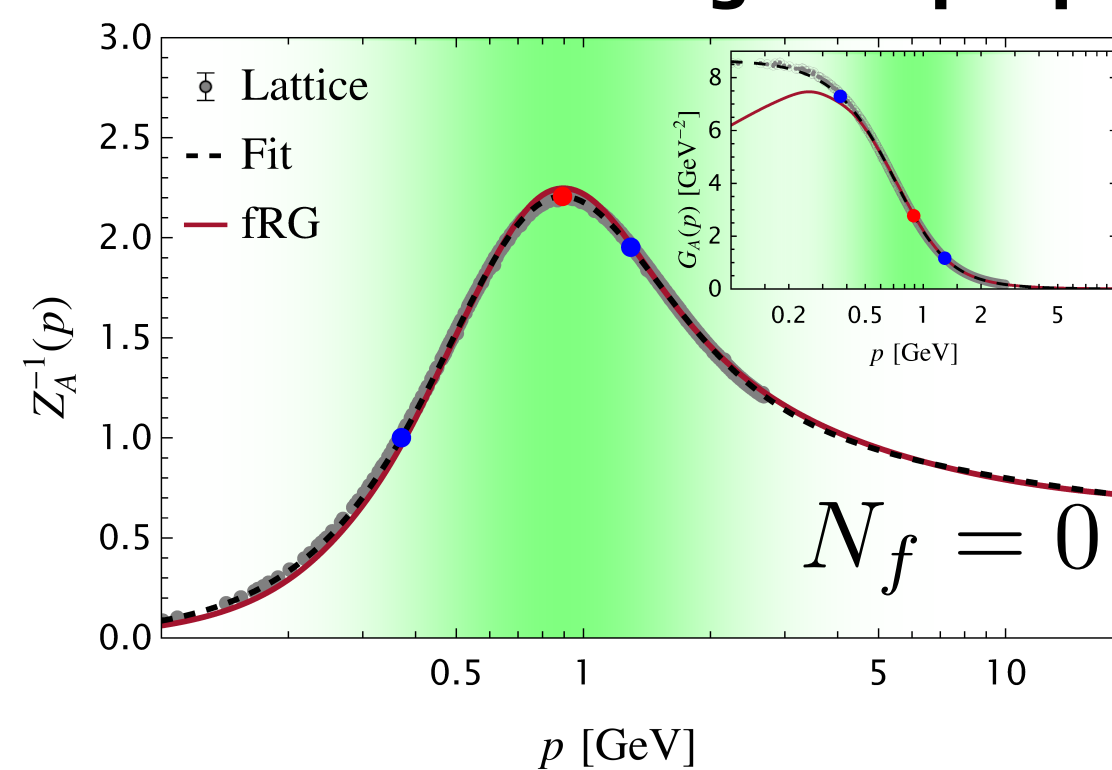
scales, scales, scales



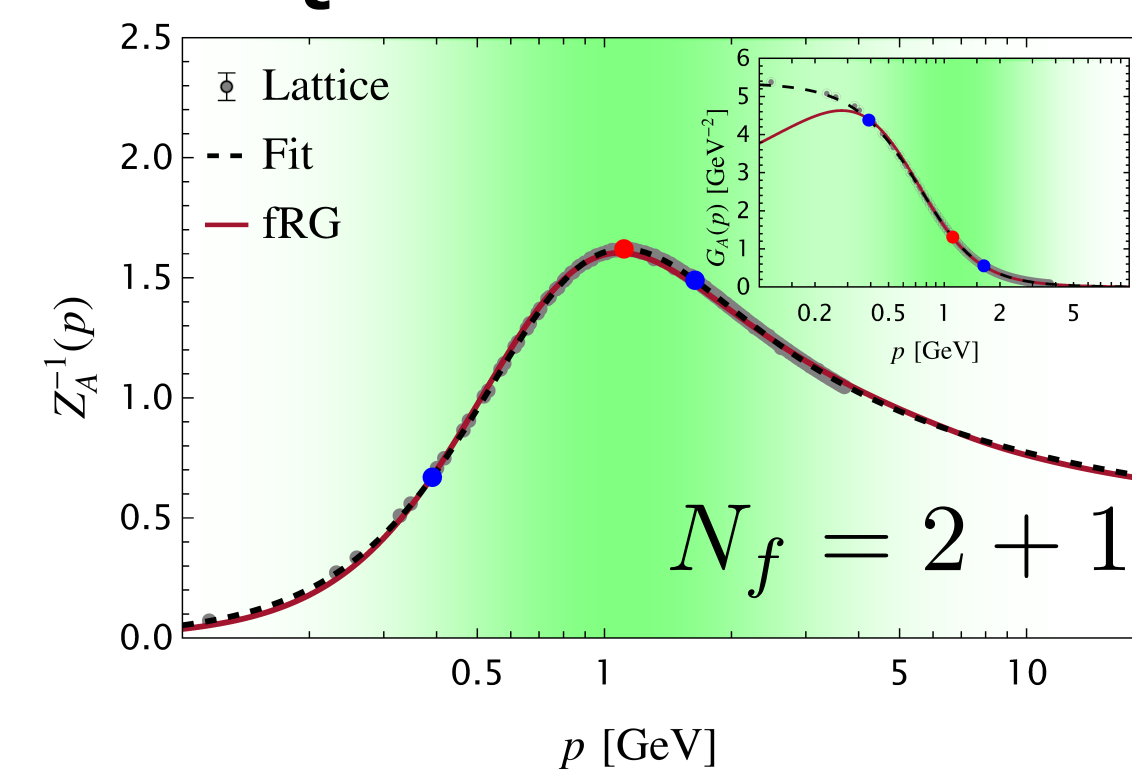
Haas, Stiele, Braun, JMP, Schaffner-Bielich, PRD 87 (2013) 076004



gluon propagators in YM & QCD



Ferreira, Papavassiliou, JMP, EPJC 85 (2025) 11, 1339



Direct applications to the QCD phase structure

Braun, Haas, Marhauser, JMP, PRL 106 (2011) 022002

Fischer, Fister, Lücker, JMP, PLB 732 (2014) 273

Fischer, Lücker, Welzbacher, PRD 90 (2014) 034022

Fischer, Lücker, JMP, PRD 91 (2015) 014024

Lu, Gao, Liu, JMP, 113 (2026) 054019

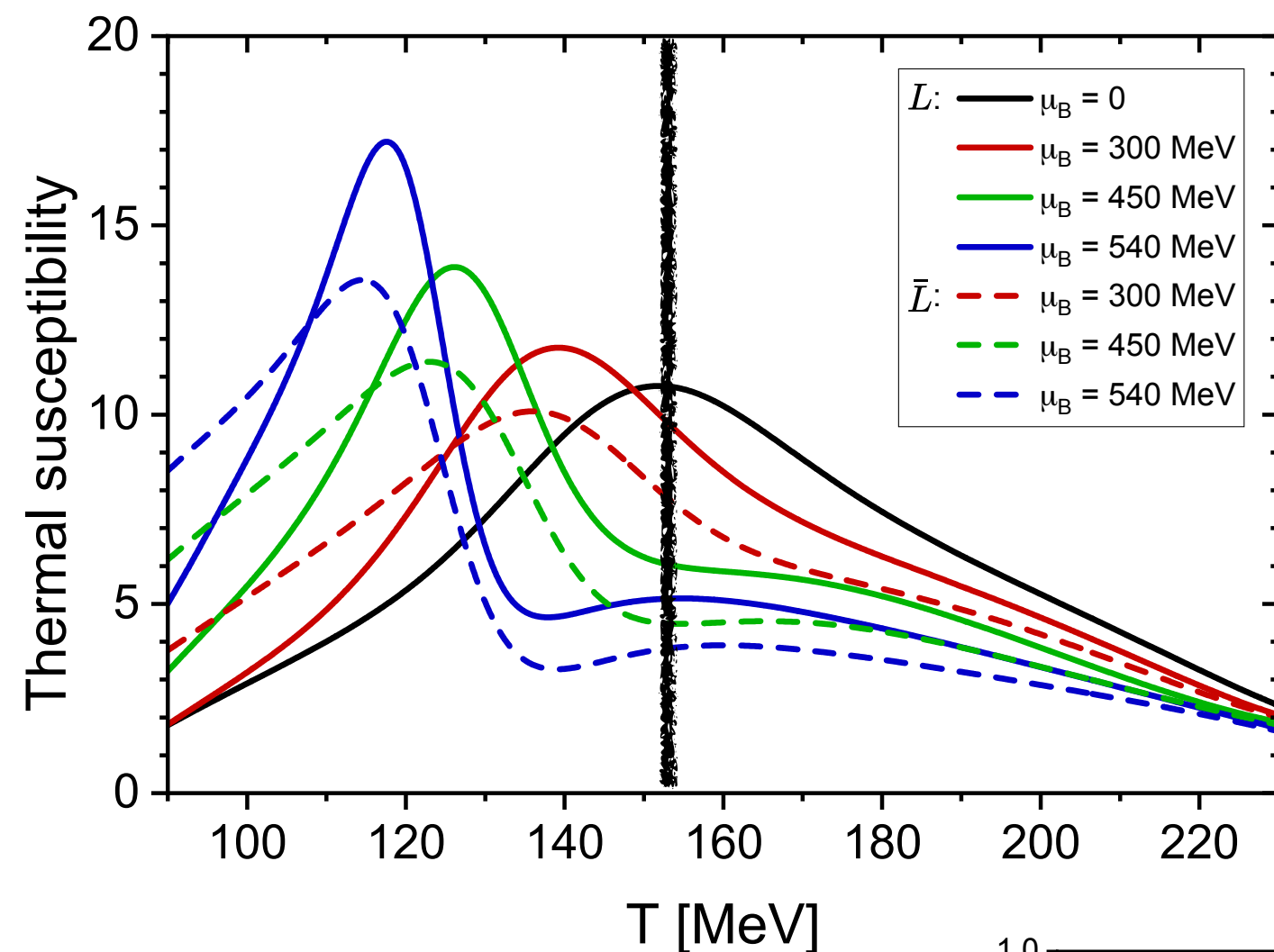
Lu, Fischer, Gao, Liu, JMP, arXiv:2603.09336

fRG & DSE

Strongly correlated physics

‘Confinement’ related ‘crossovers’ at $T_\chi \lesssim T_{\text{conf}} \lesssim 2T_\chi$

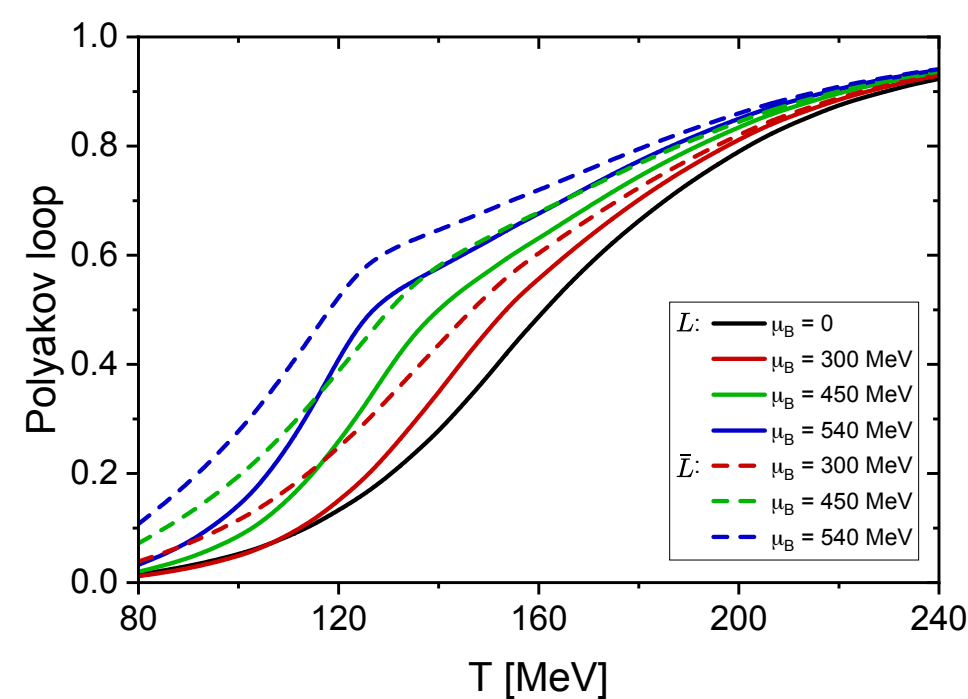
Functional QCD



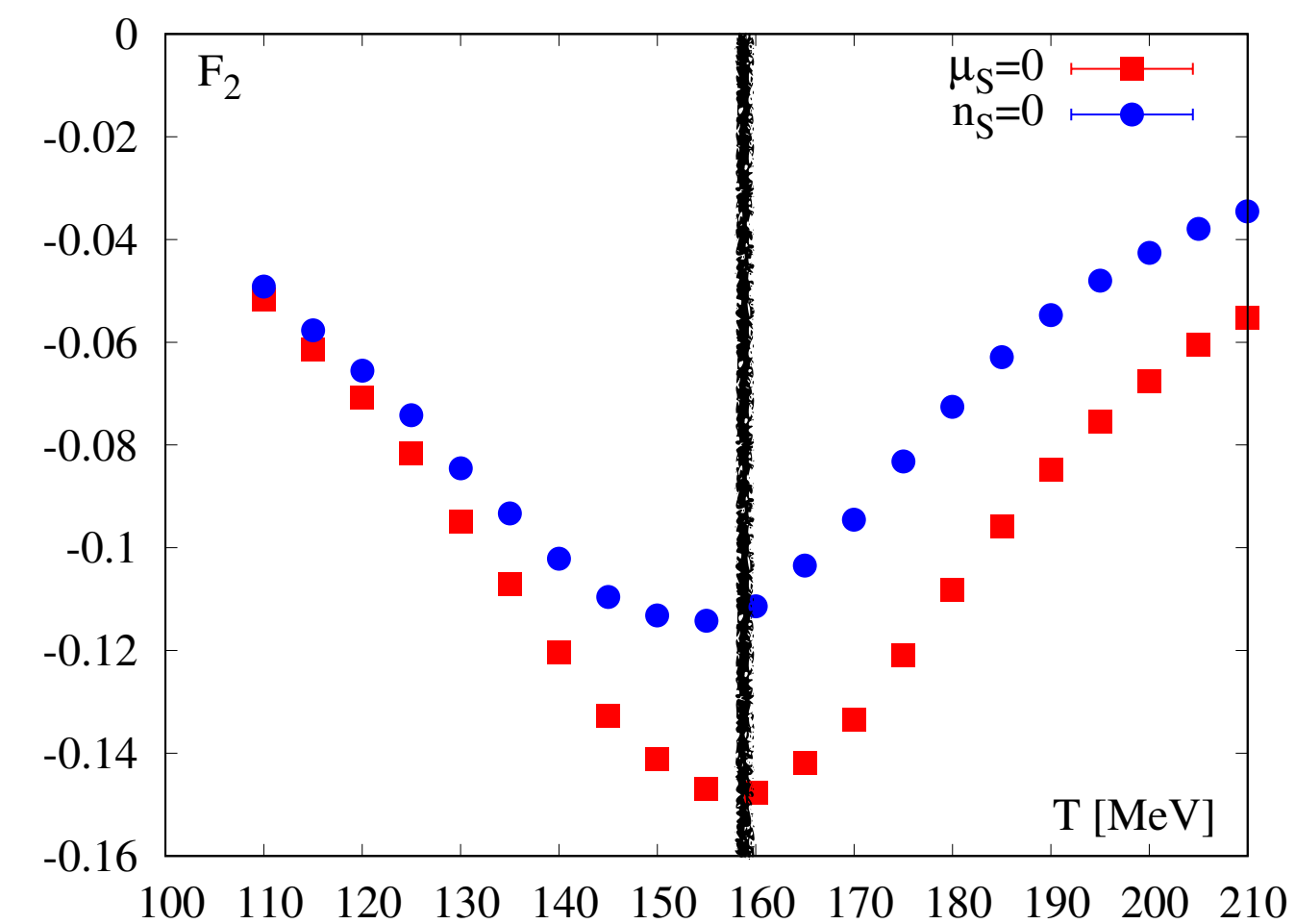
Variants of the traced Polyakov loop

$$P = \frac{1}{N_c} \text{tr} e^{2\pi i \varphi}$$

$$\propto P(\langle \text{ev}(\varphi) \rangle)$$

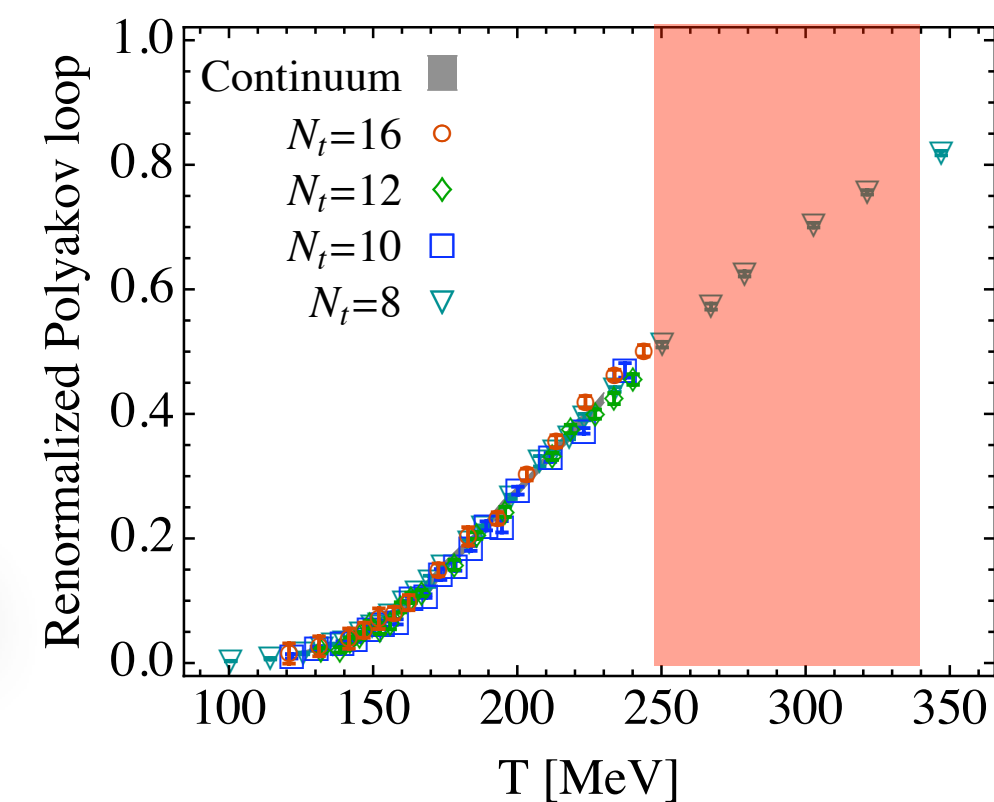


Lattice QCD



$$\propto T \frac{\partial^2 \log |\langle P \rangle|}{(\partial \mu_B / T)^2}$$

$$\propto \langle P \rangle$$



Lu, Gao, Liu, JMP, 113 (2026) 054019

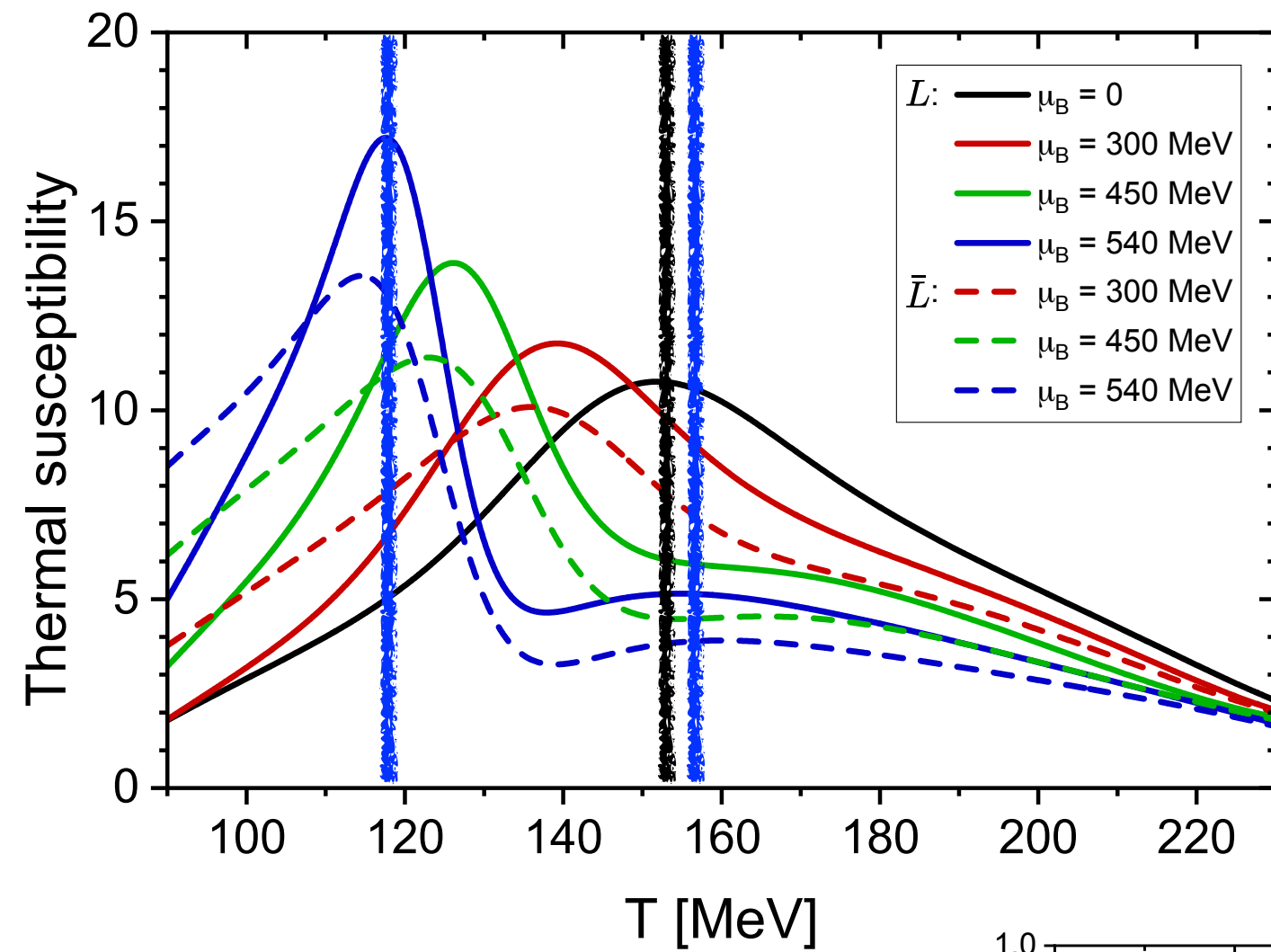
Bazavov, Brambilla, Ding, Petreczky, Schadler, Vairo, Weber, PRD 93 (2016) 11, 114502

Borsányi, Fodor, Guenther, Kara, Paolo Parotto, Pásztor, Pirelli, Wong, PRD 110 (2024) 114507

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‘Confinement’ related ‘crossovers’ at $T_\chi \lesssim T_{\text{conf}} \lesssim 2T_\chi$

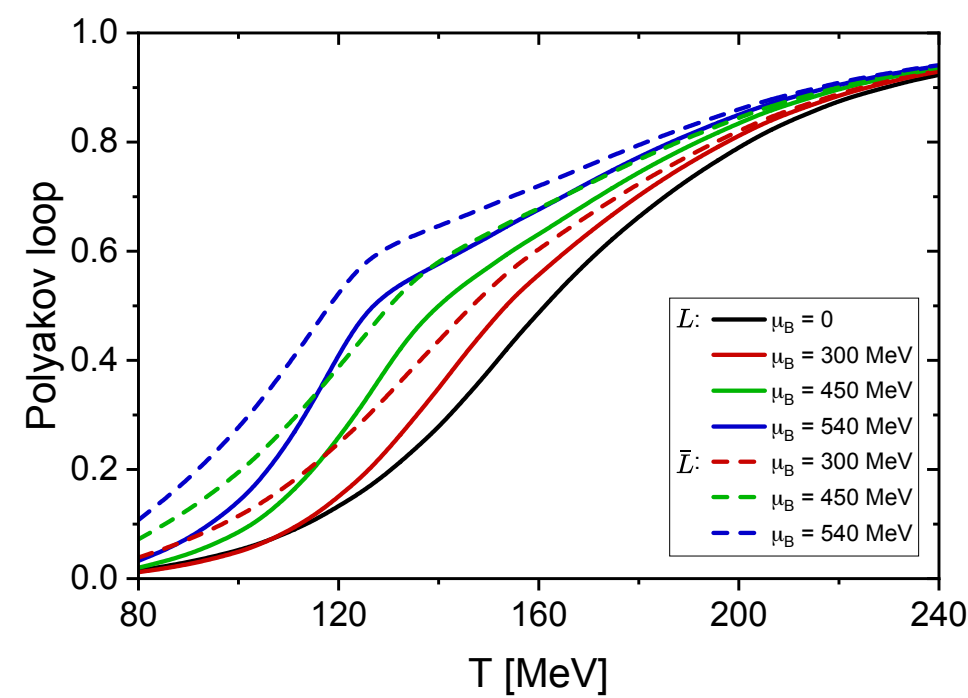
Functional QCD



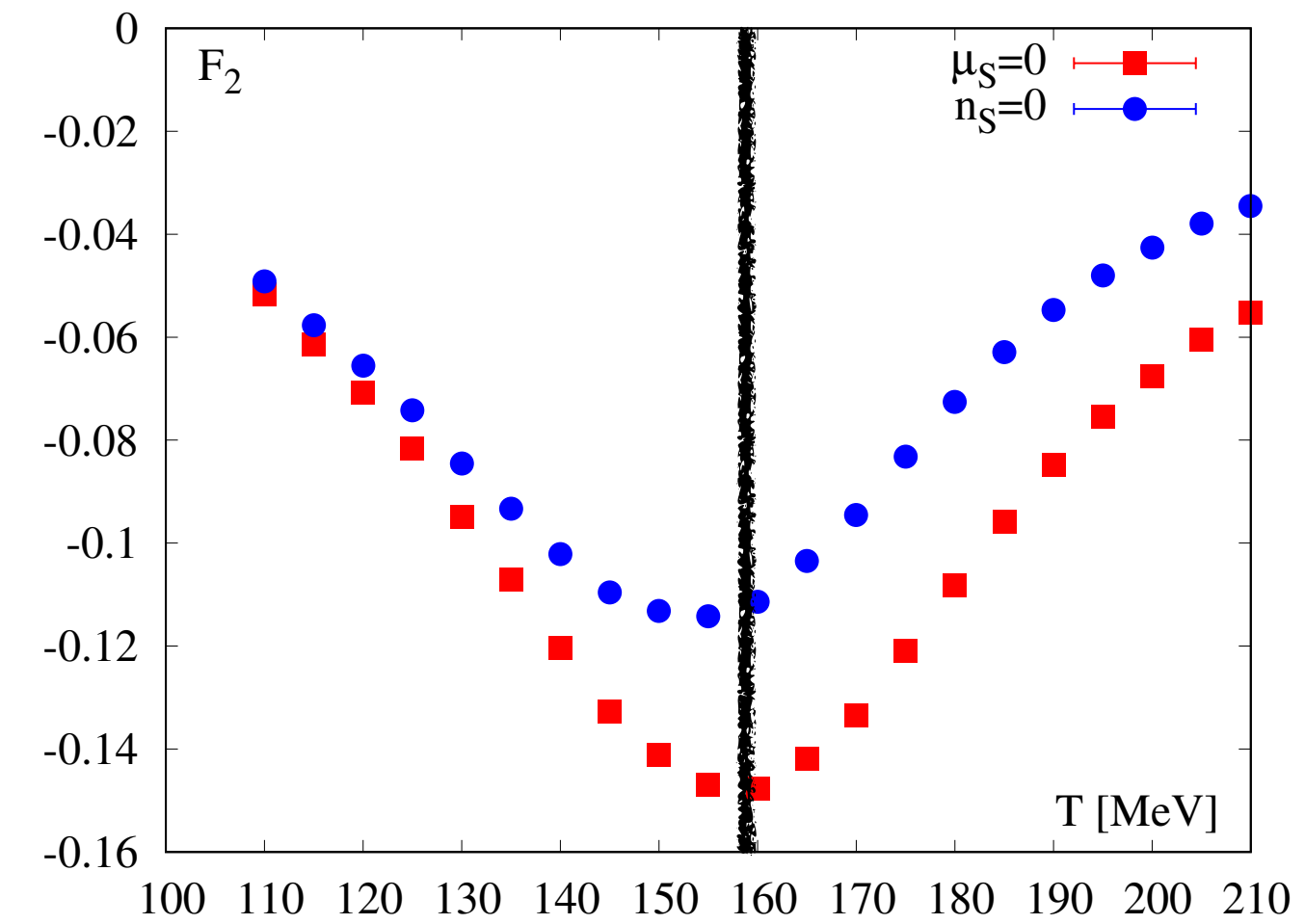
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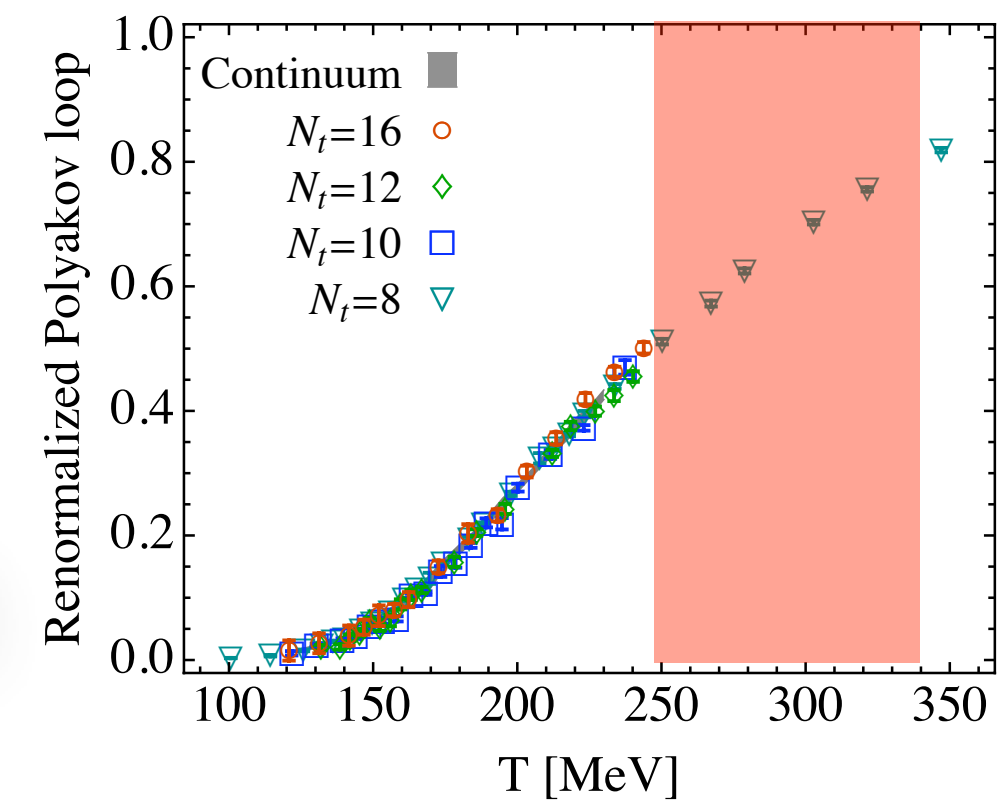


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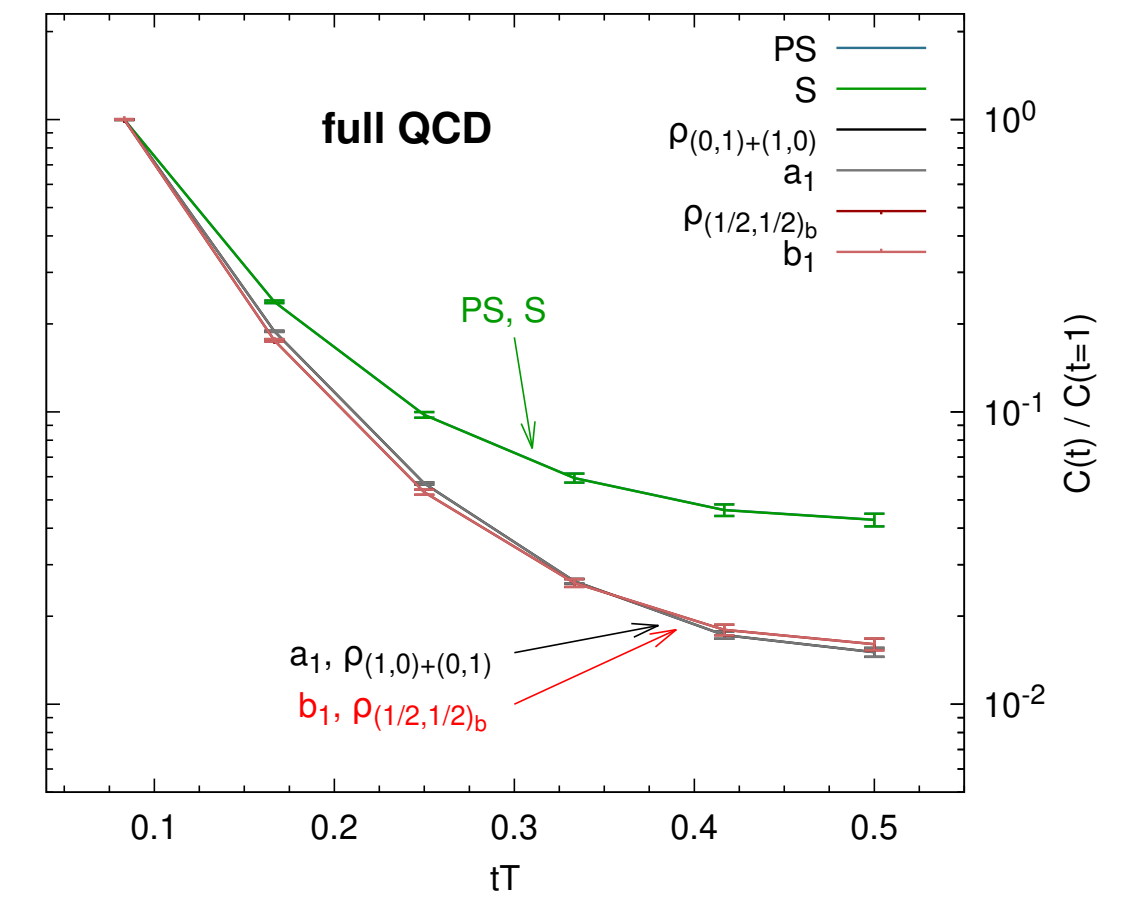
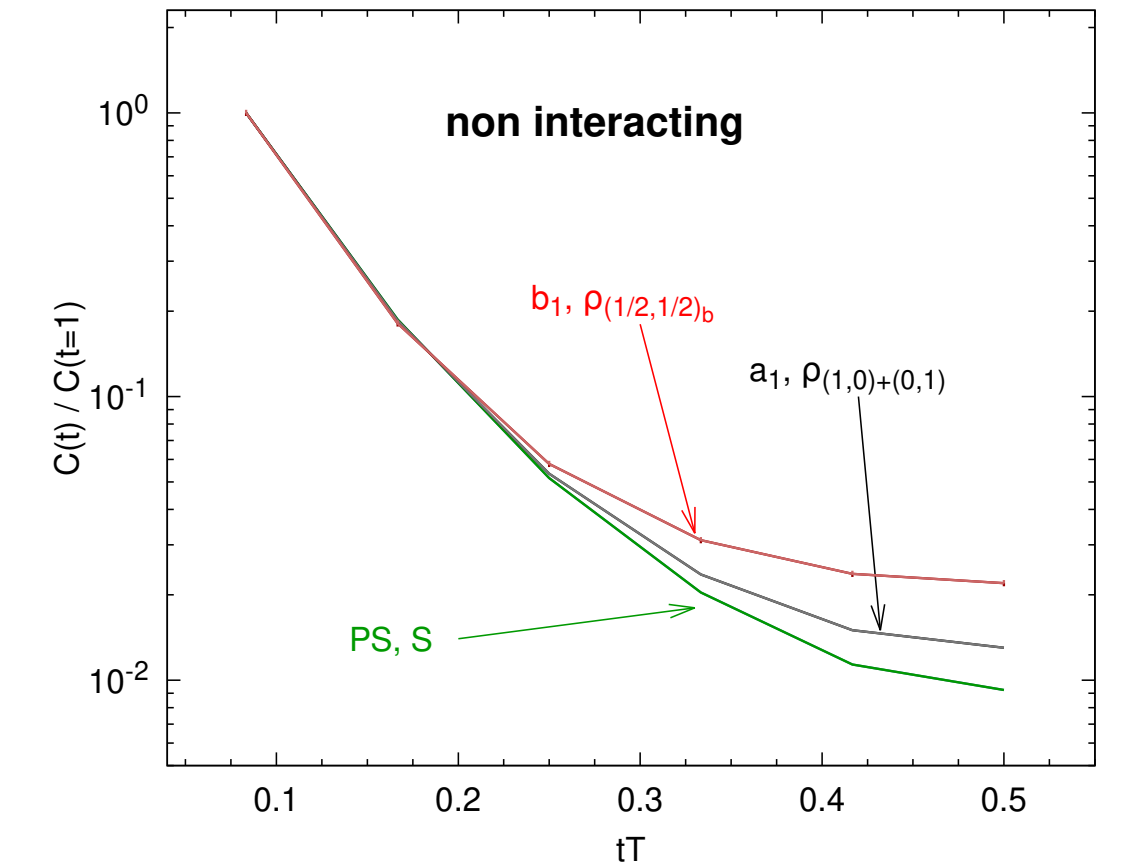
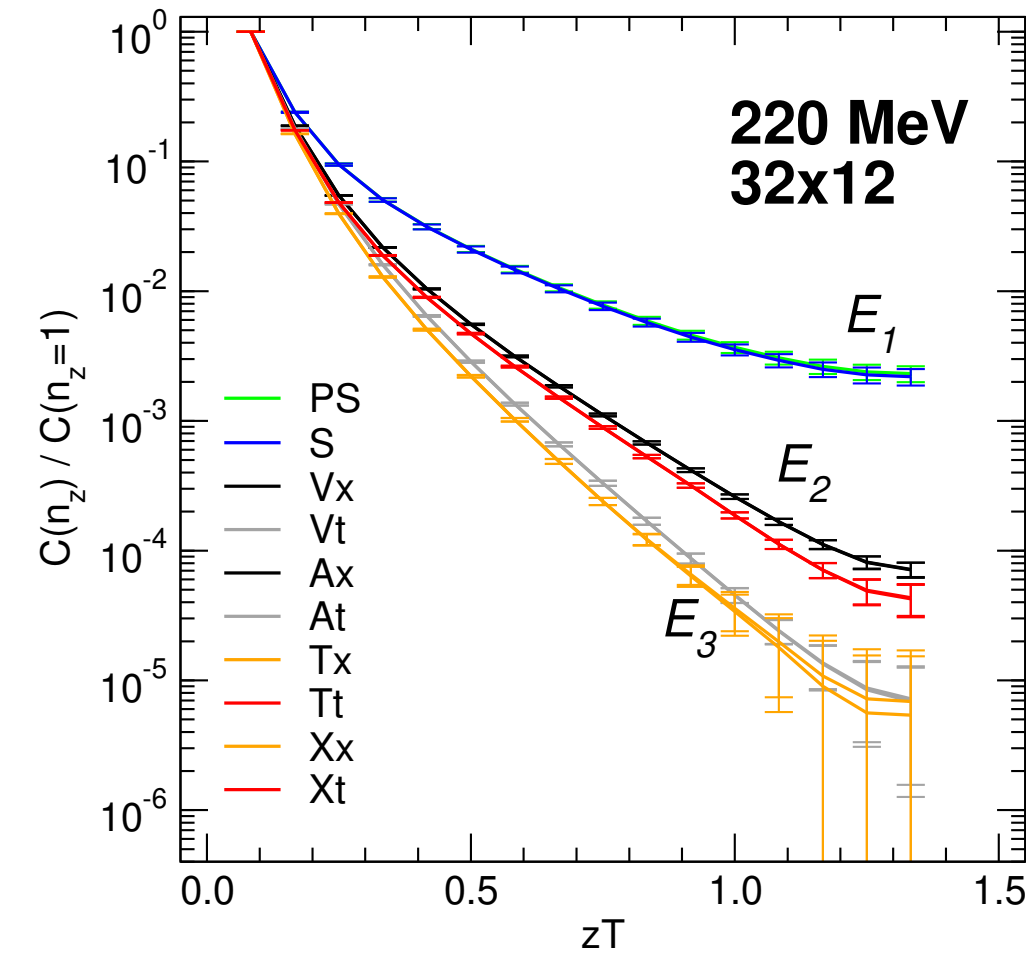
Bazavov, Brambilla, Ding, Petreczky, Schadler, Vairo, Weber, PRD 93 (2016) 11, 114502

Borsányi, Fodor, Guenther, Kara, Paolo Parotto, Pásztor, Pirelli, Wong, PRD 110 (2024) 114507

Strongly correlated physics

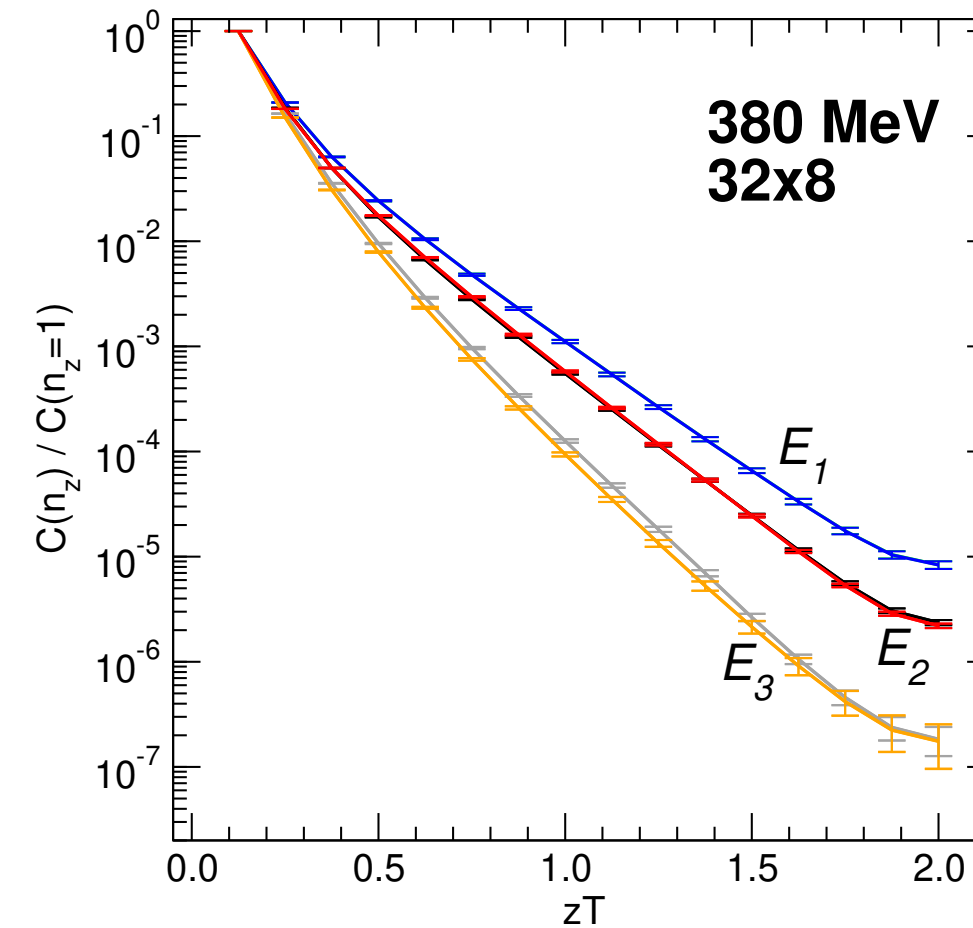
See talk of Leonid

Spin symmetry for $T_\chi \lesssim T \lesssim 2T_\chi$



⋮
Rohrhofer, Aoki, Cossu, Fukaya, Glozman, Hashimoto,
Lang, Prelovsek, PRD 96 (2017) 094501

⋮
Rohrhofer, Aoki, Glozman, Hashimoto, PLB 802 (2020) 135245

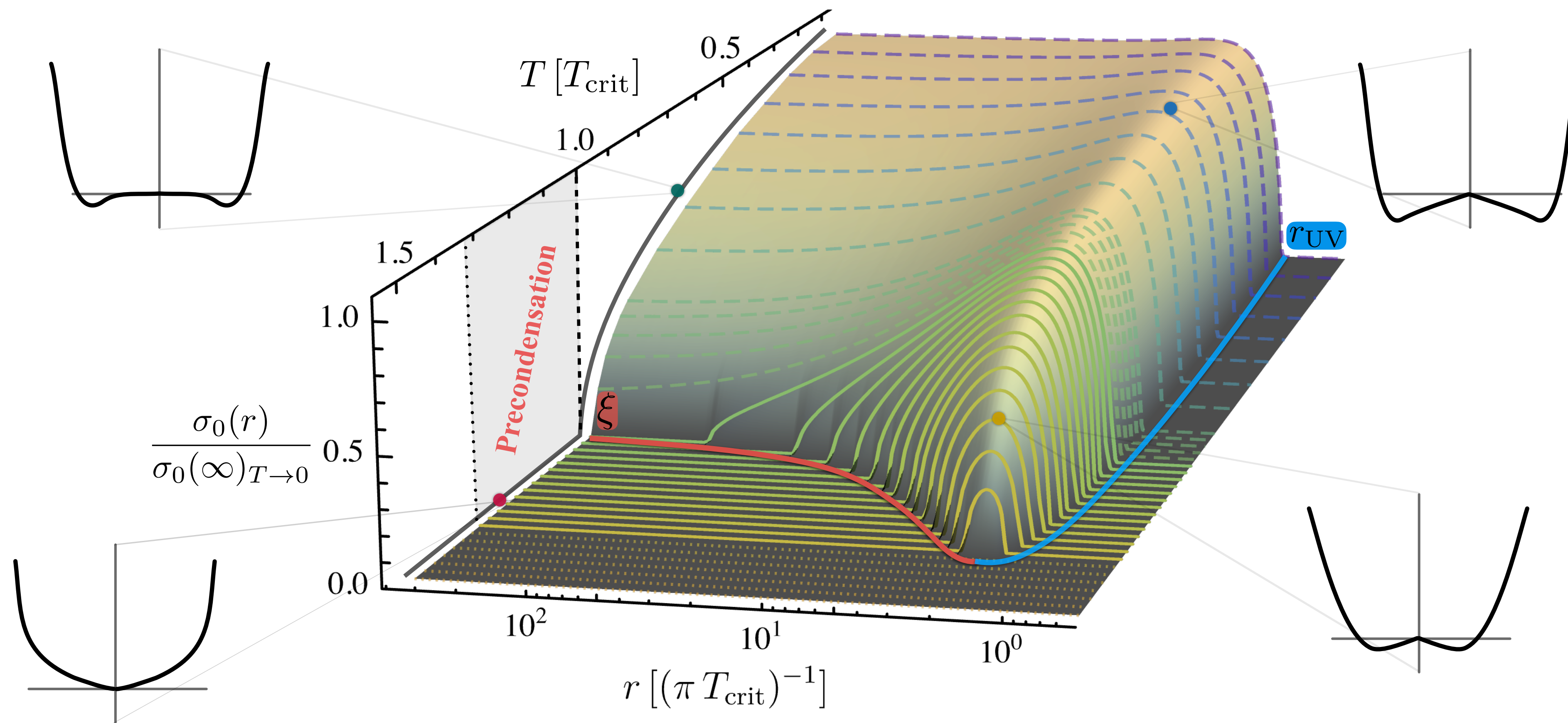


Relation?

Strongly correlated physics

See talk of Álvaro

Precondensation in chiral QCD

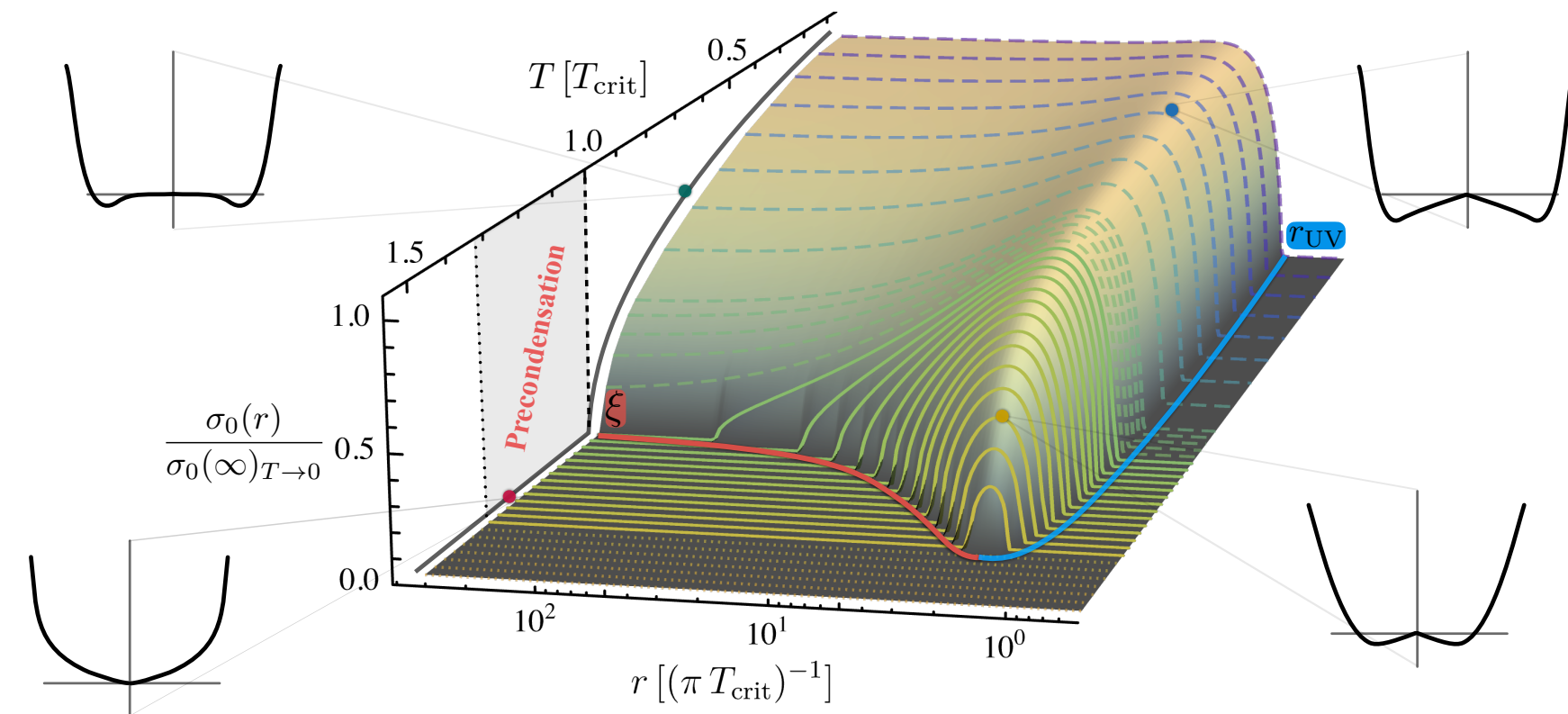


Strongly correlated physics

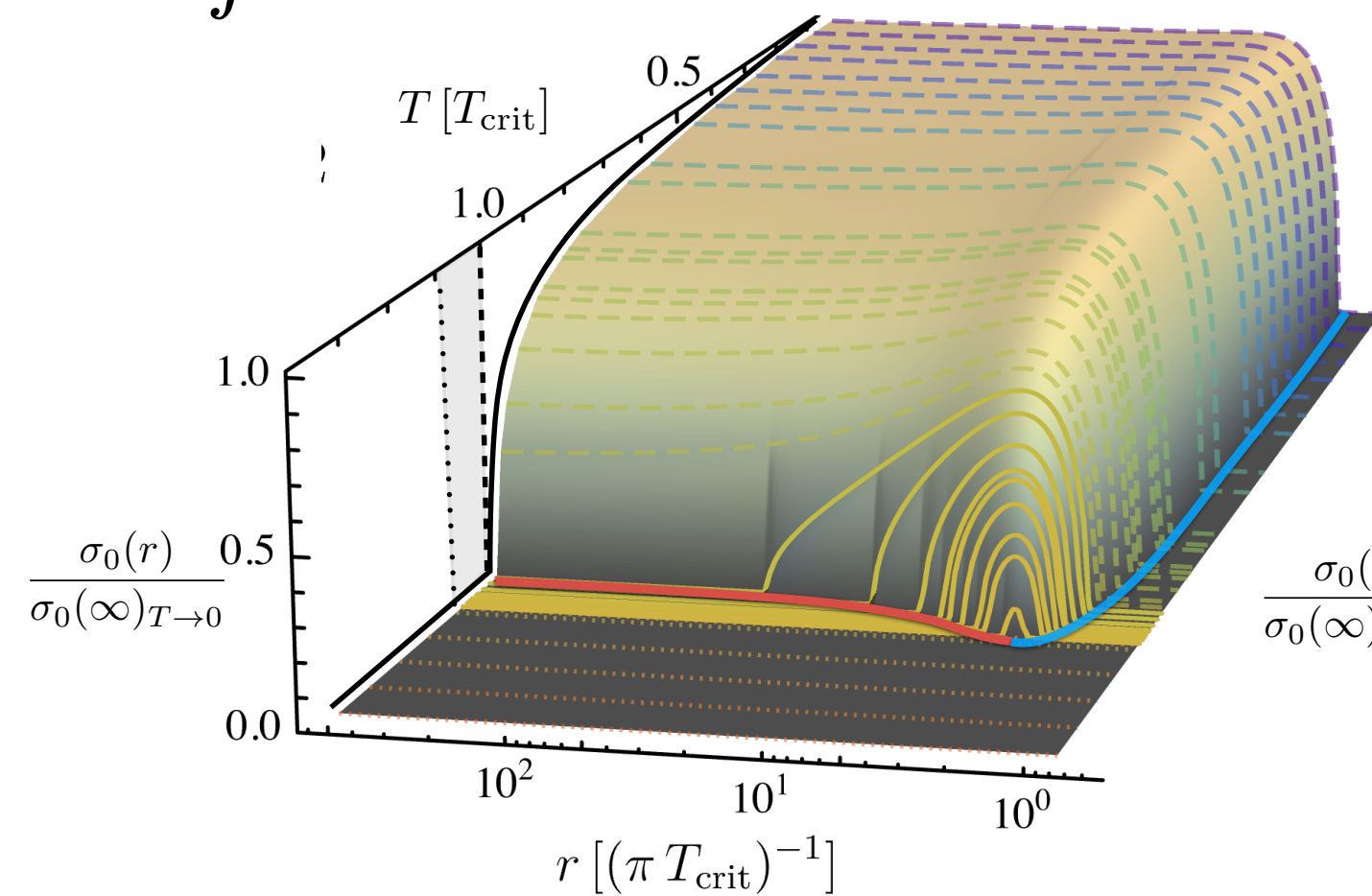
See talk of **Álvaro**

Precondensation for different flavours

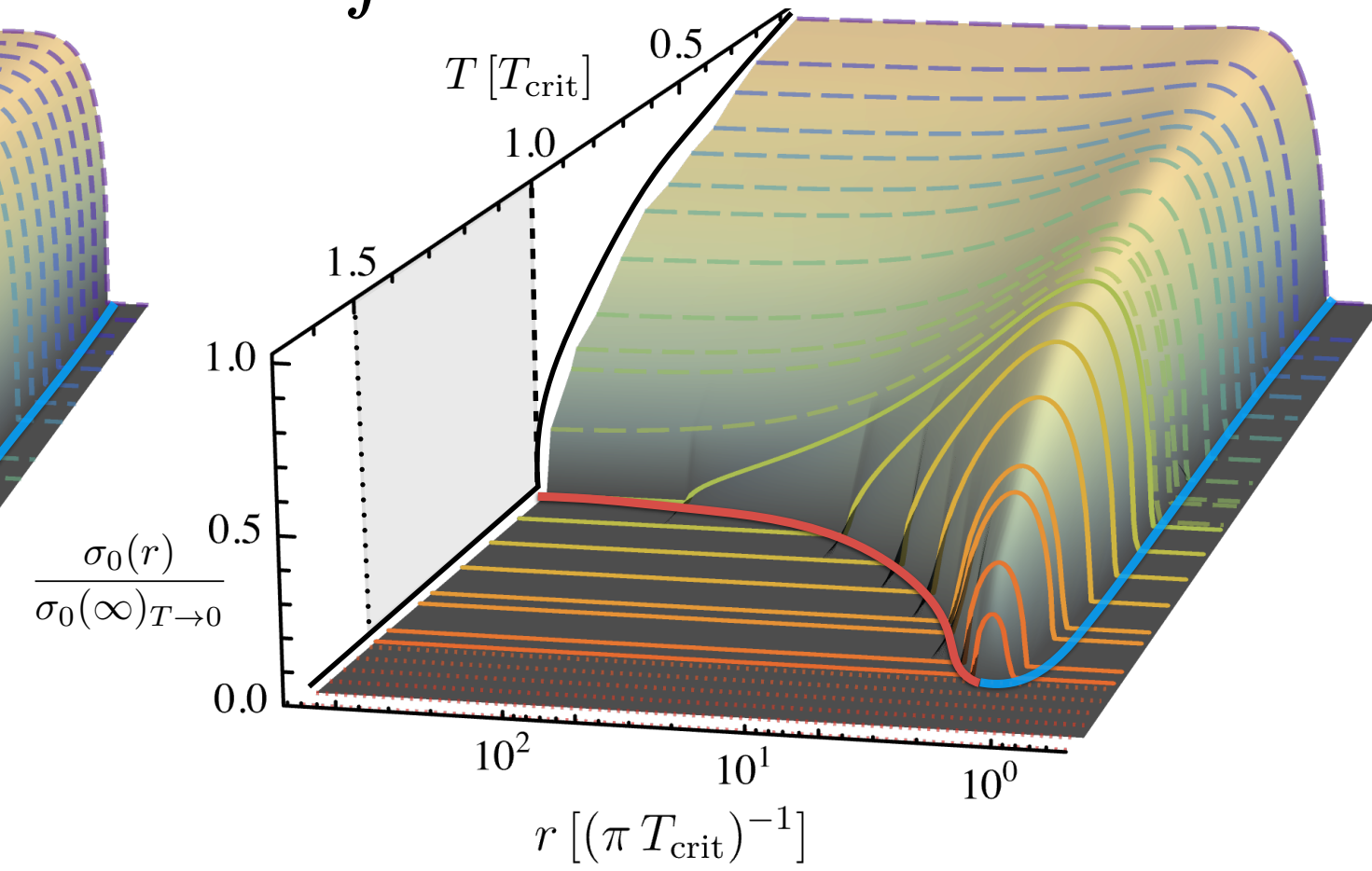
$N_f = 3$



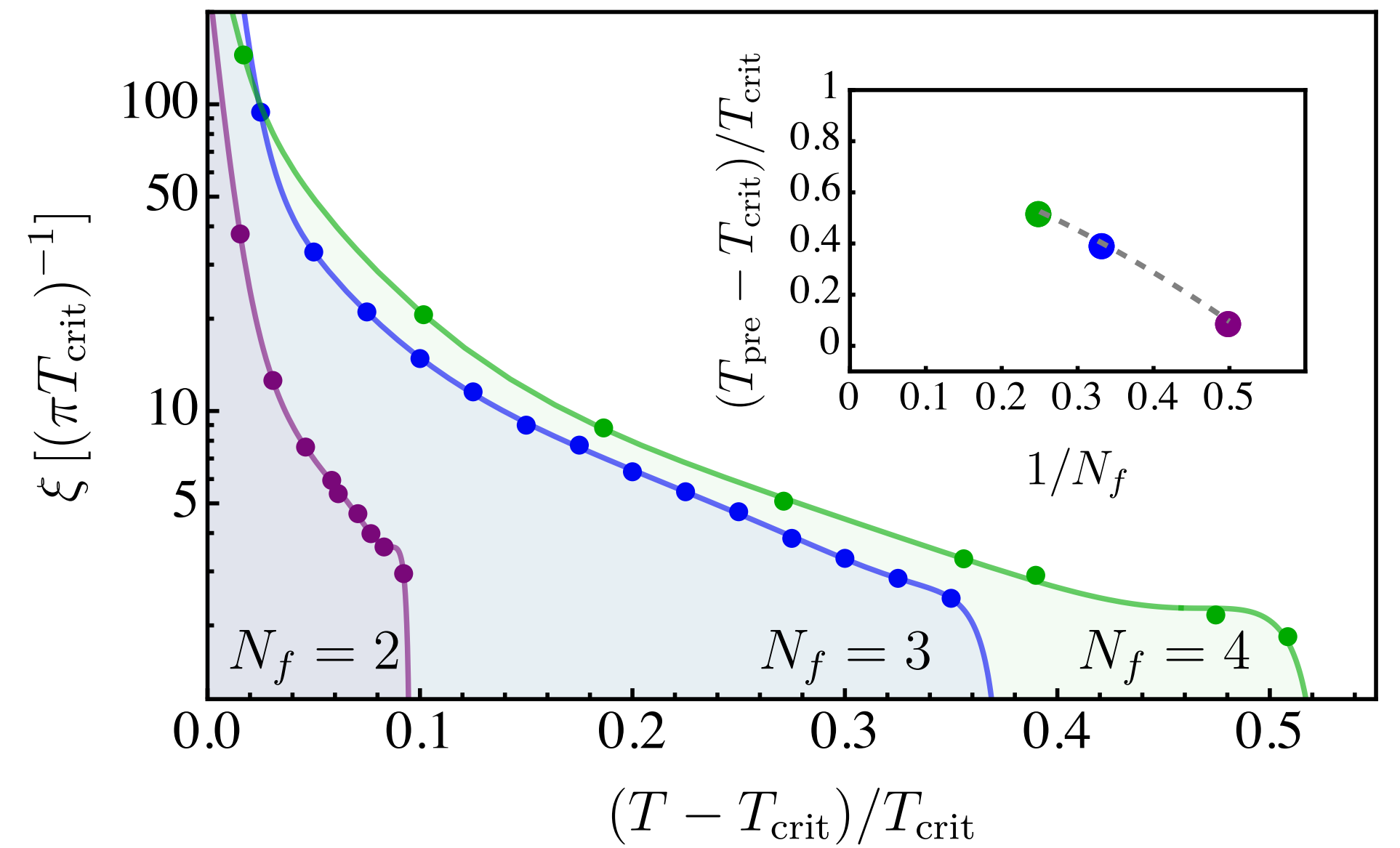
$N_f = 2$

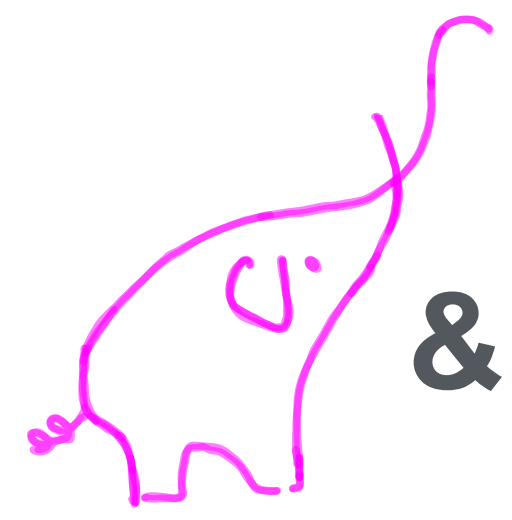


$N_f = 4$



Correlation length of 'domains'



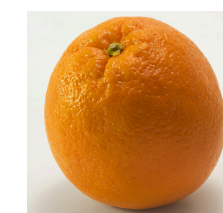


& functional QCD

Ripples of the CEP

aka

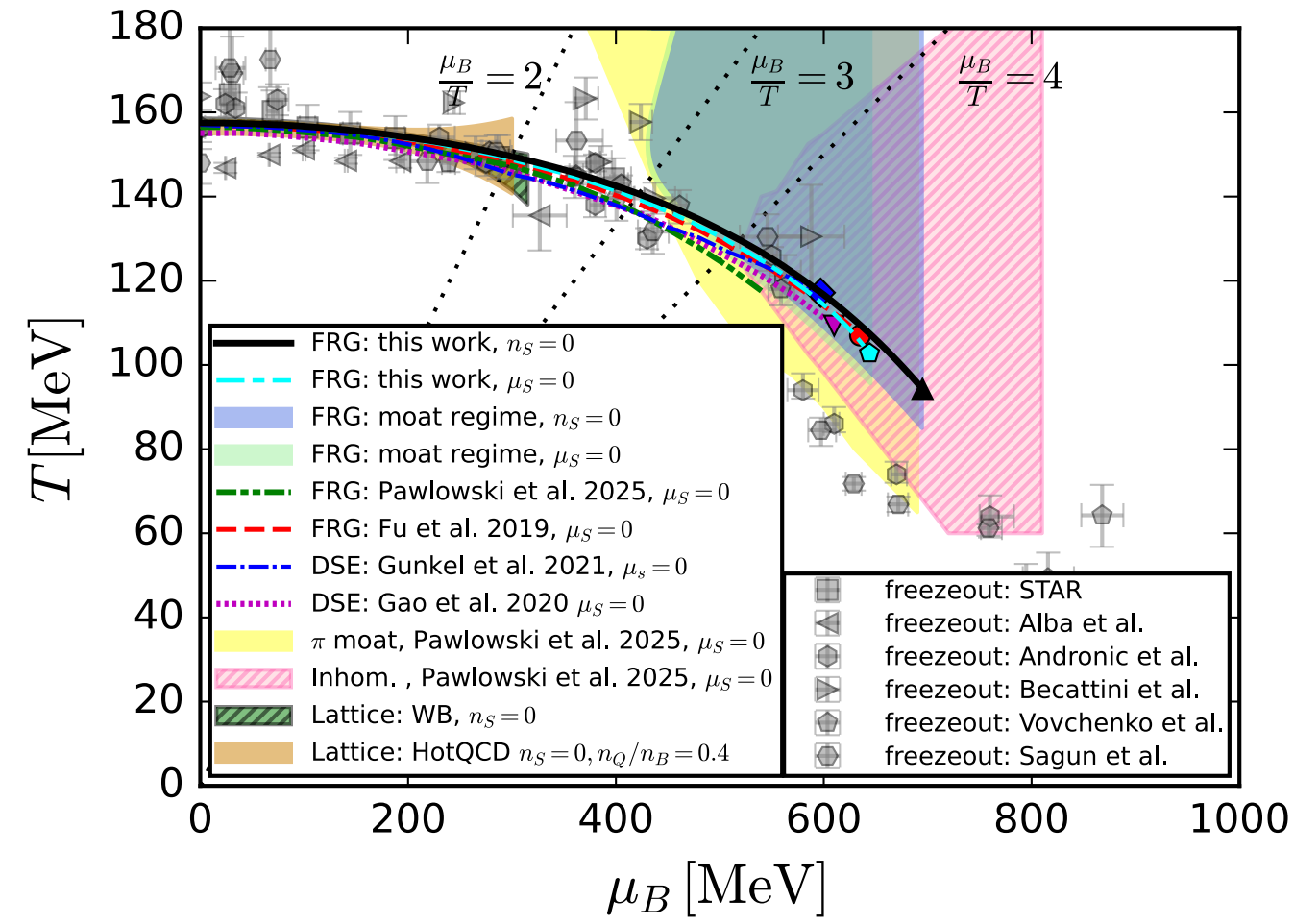
(Strong) signals of the ONP



QCD-assisted low energy effective theory

Direct QCD input

chiral phase structure

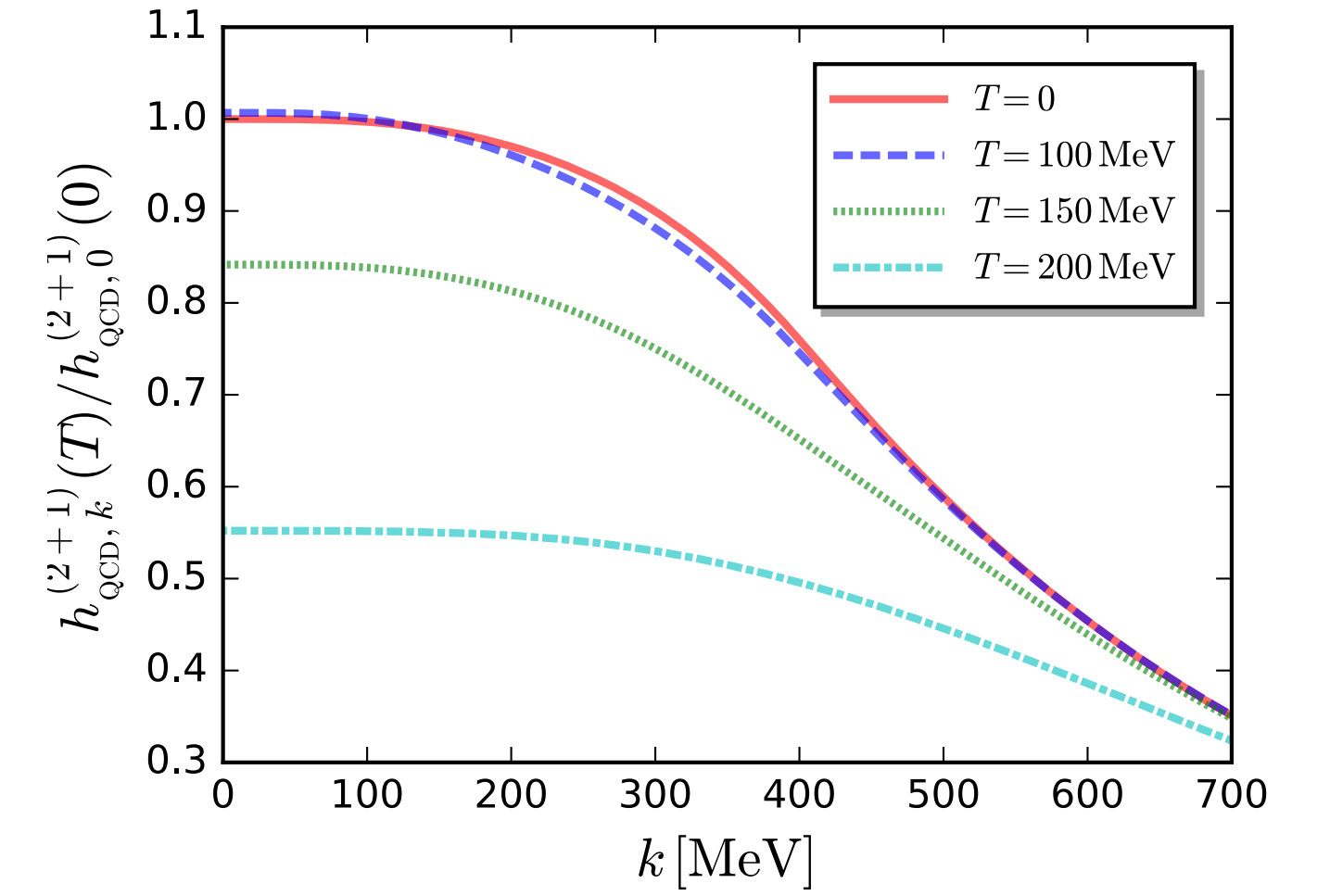


+



Fu, JMP, Rennecke, PRD 101 (2020) 054032

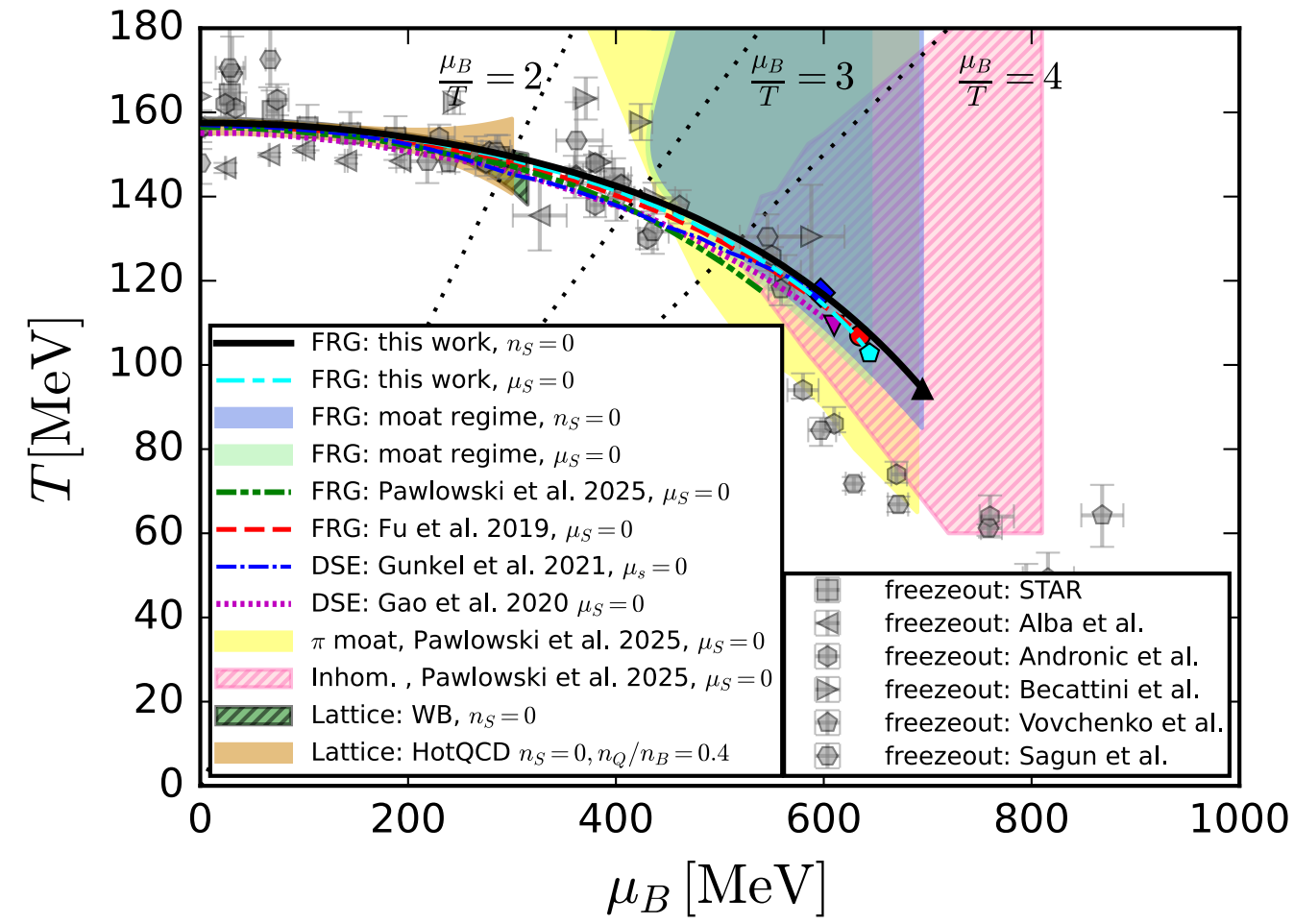
quark-antiquark — meson scattering



QCD-assisted low energy effective theory

Direct QCD input

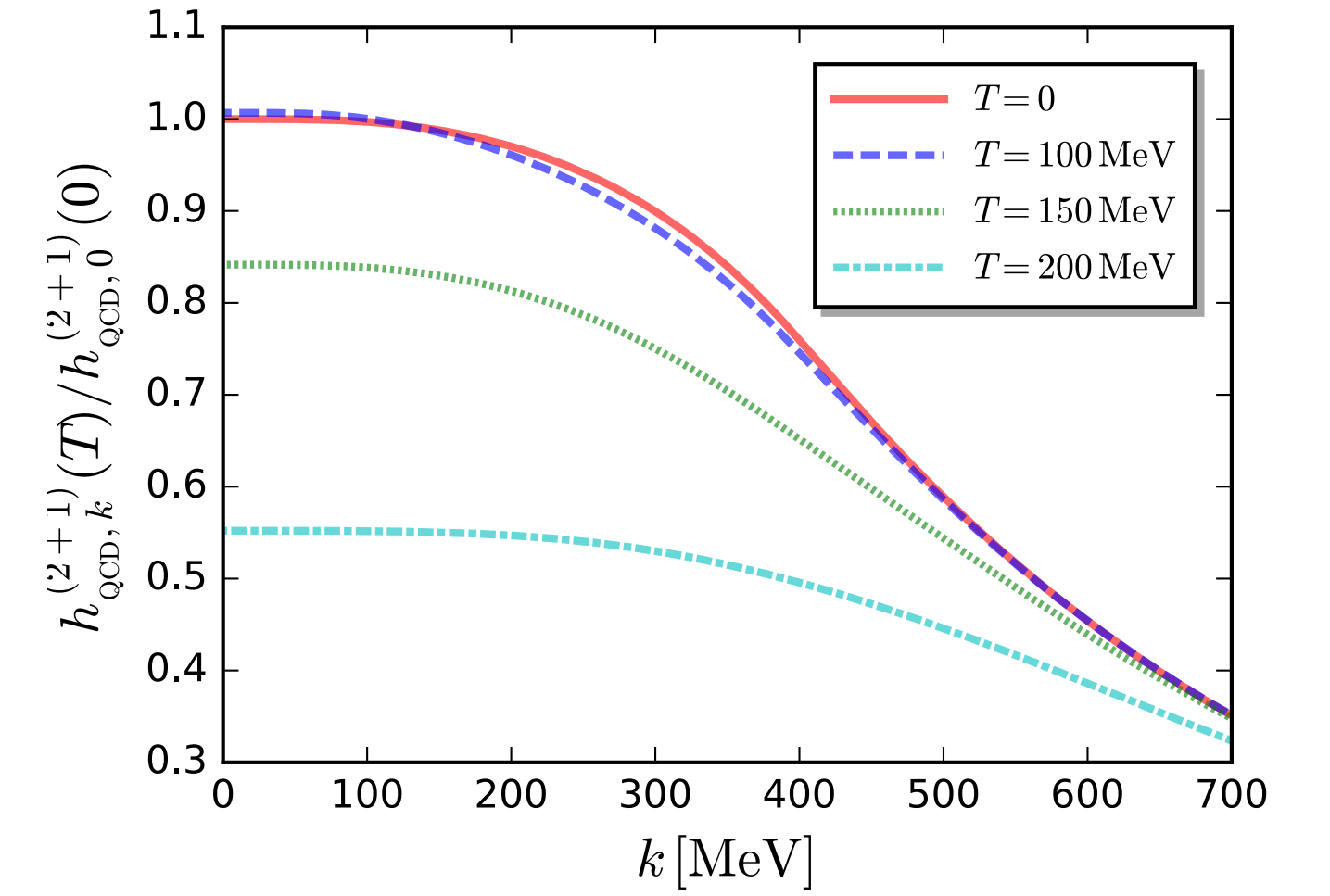
chiral phase structure



+



quark-antiquark — meson scattering



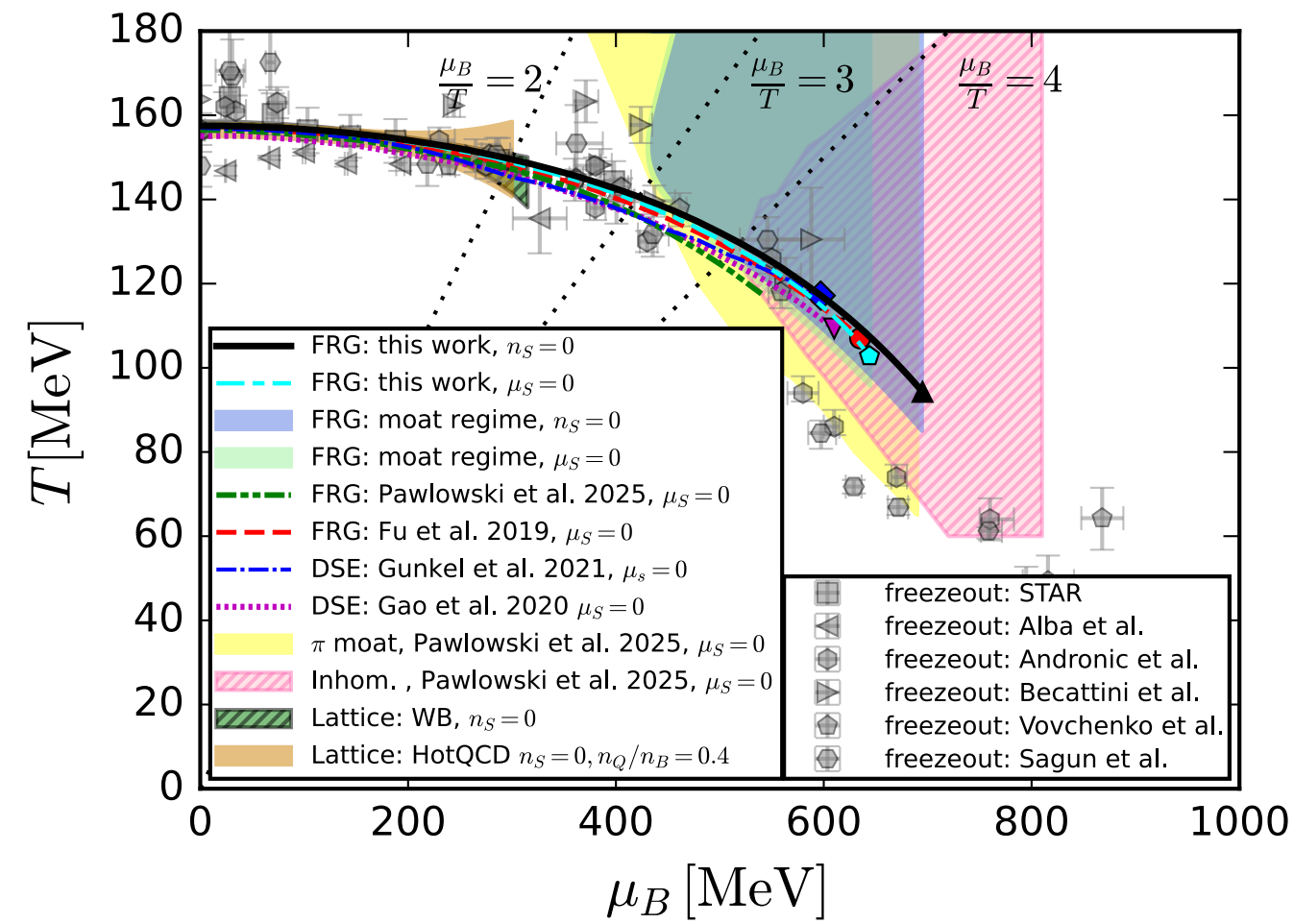
Fu, JMP, Rennecke, PRD 101 (2020) 054032

low energy quantum, thermal & density fluctuations via fRG (QCD-assisted PQM model)

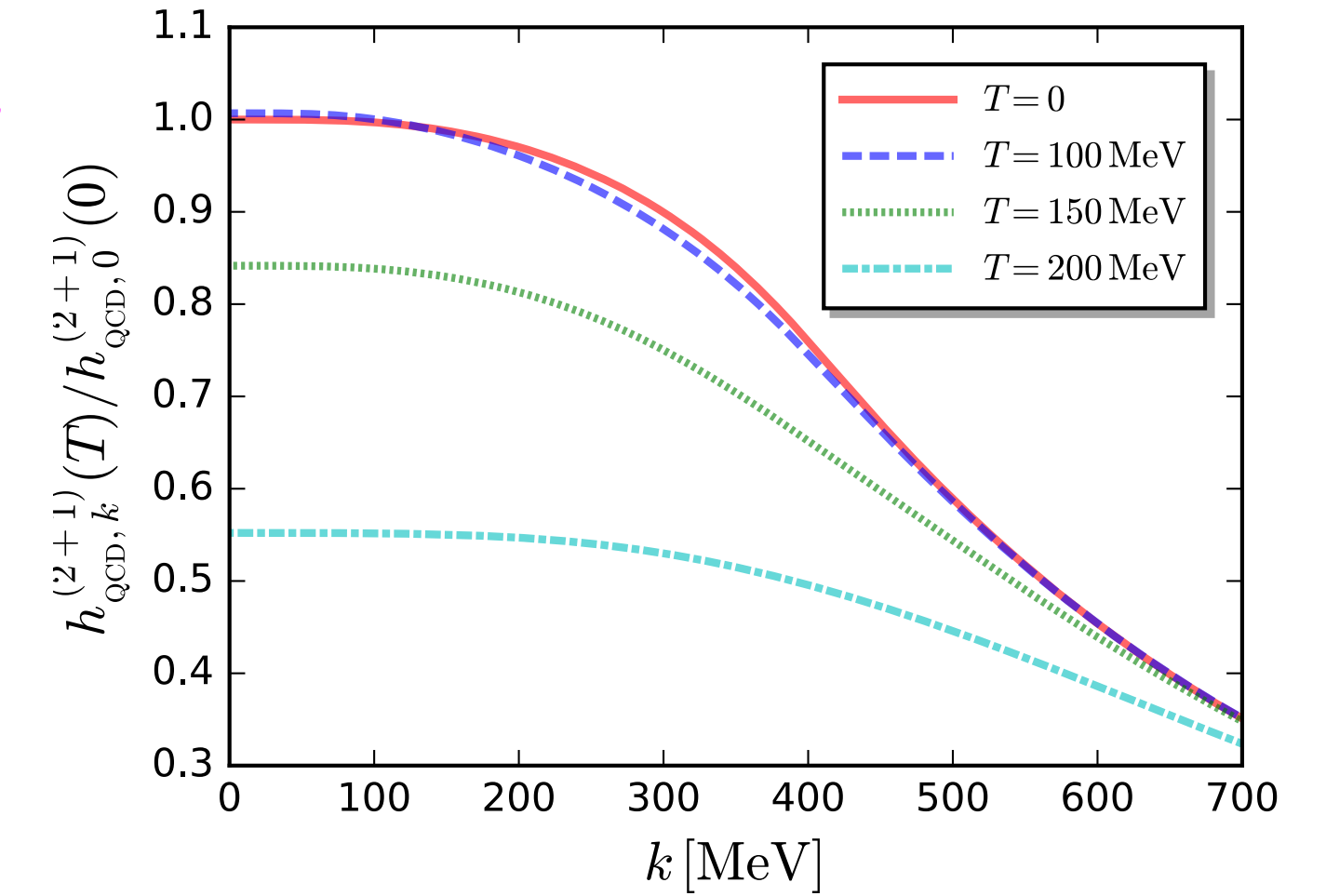
QCD-assisted low energy effective theory

Direct QCD input

chiral phase structure



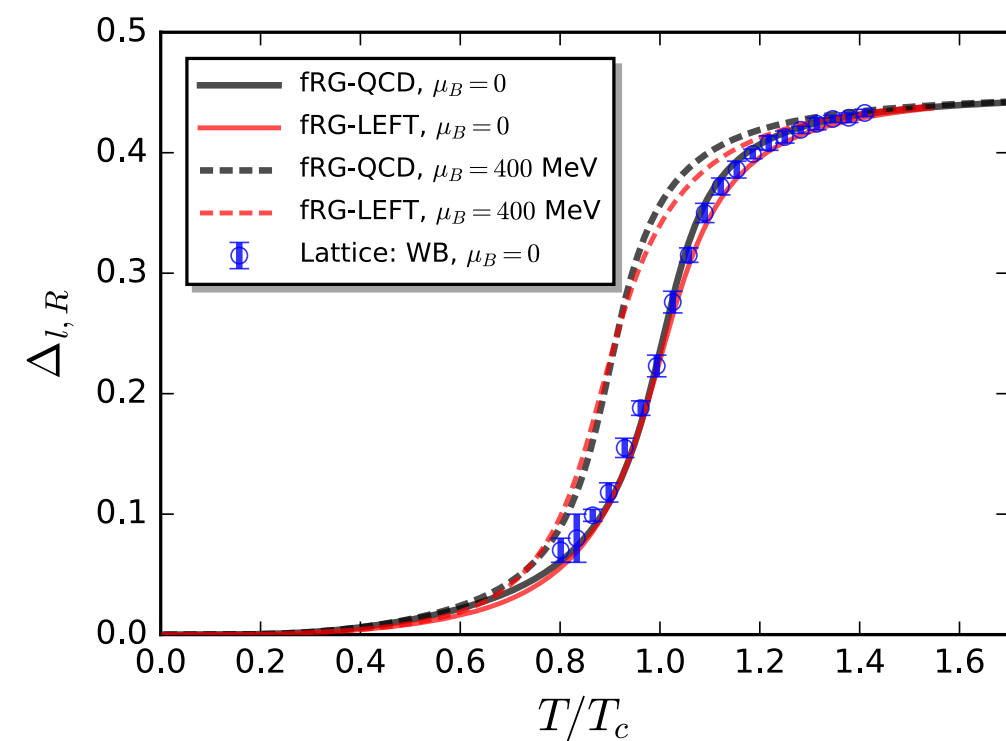
quark-antiquark — meson scattering



Fu, JMP, Rennecke, PRD 101 (2020) 054032

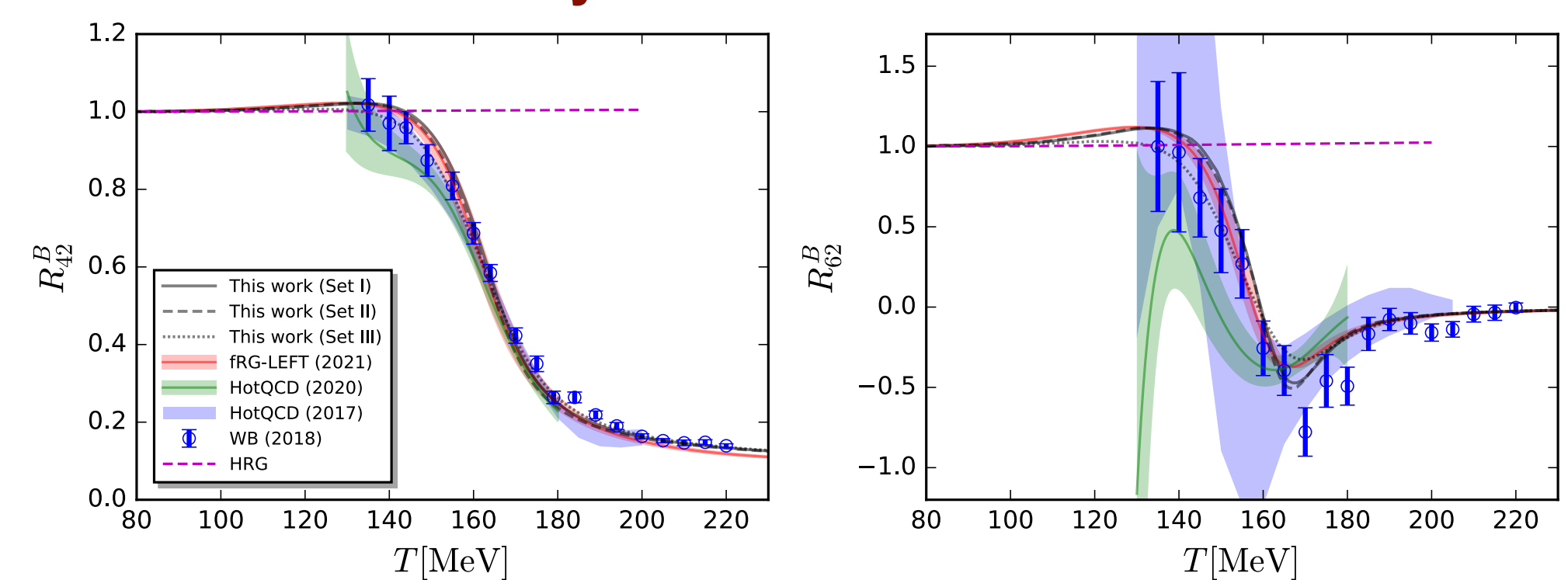
low energy quantum, thermal & density fluctuations via fRG (QCD-assisted PQM model)

renormalised chiral condensate



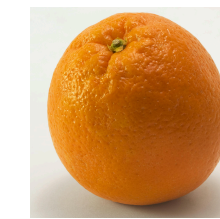
Benchmarks with lattice and fQCD
at
vanishing density and fQCD at finite density

baryon number fluctuations



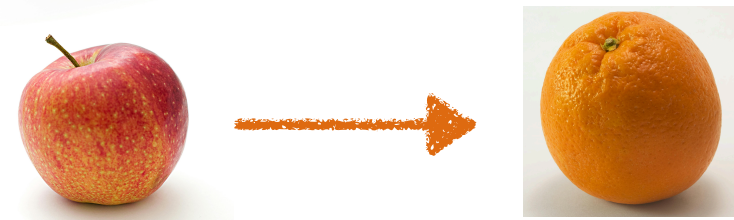


Ripples of the critical point at chemical freeze-out



Canonical corrections via subensemble acceptance

Vovchenko, Savchuk, Poberezhnyuk, Gorenstein, Koch, PLB 811, 135868 (2020)

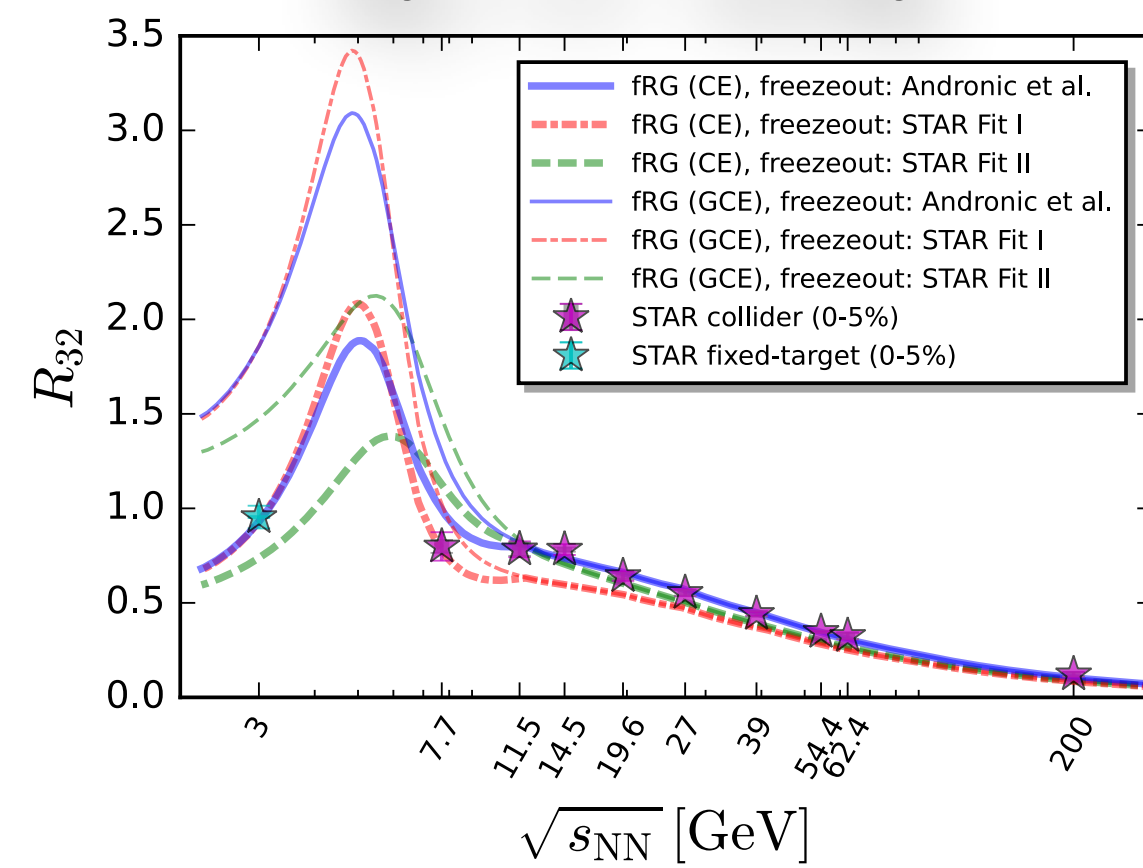


fixing the subensemble volume

subensemble volume system volume

$$V_1 = \alpha V$$

$$\bar{R}_{32}^B = (1 - 2\alpha)R_{32}^B$$



qualitative adjustment

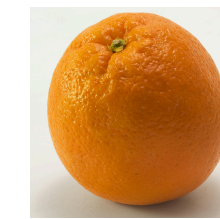
$$\alpha(\bar{s}) = a \left(1 - \sqrt{\bar{s}}\right) \theta(1 - \bar{s})$$

$$a = 0.33$$

$$\sqrt{\bar{s}} = \frac{\sqrt{s_{NN}}}{11.9 \text{ GeV}}$$

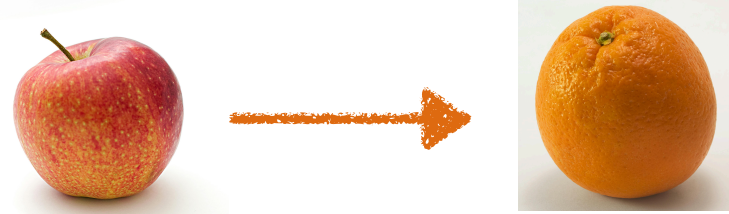


Ripples of the critical point at chemical freeze-out



Canonical corrections via subensemble acceptance

Vovchenko, Savchuk, Poberezhnyuk, Gorenstein, Koch, PLB 811, 135868 (2020)



fixing the subensemble volume

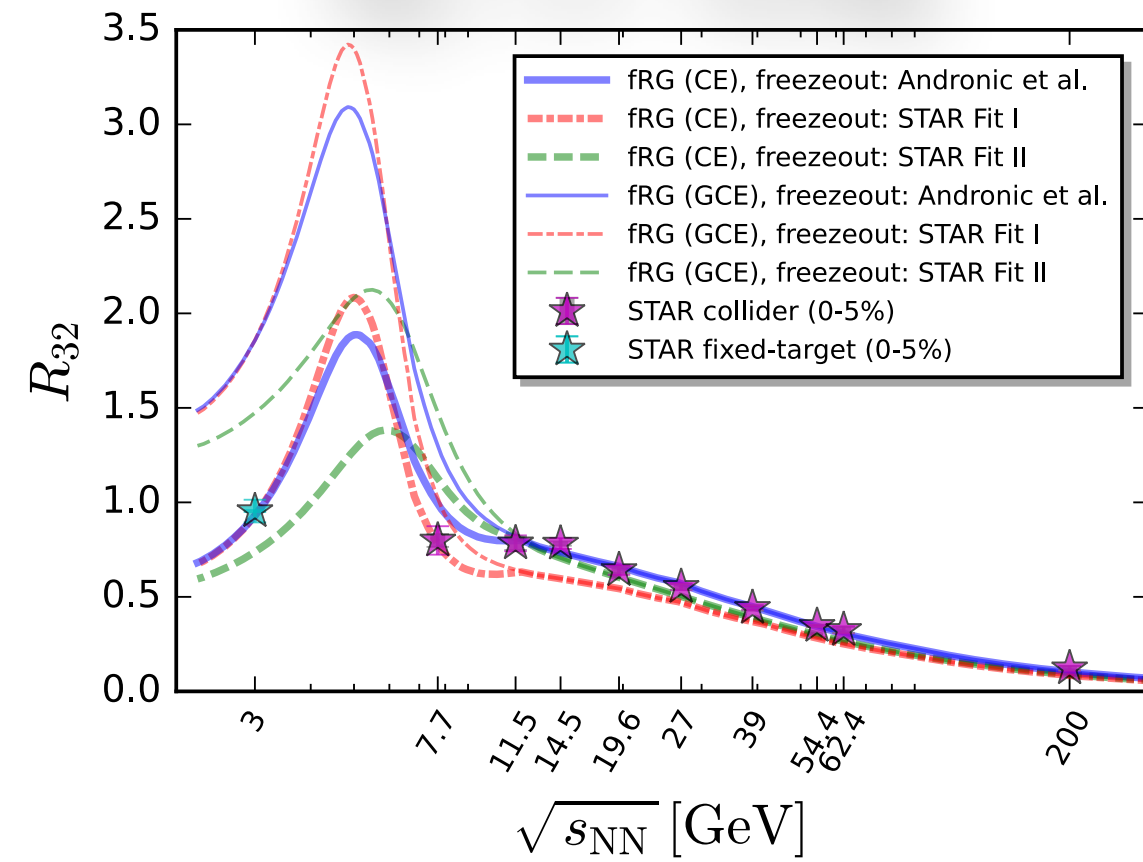
baryon & proton number fluctuations

baryon fluctuations with functional QCD

subensemble volume system volume

$$V_1 = \alpha V$$

$$\bar{R}_{32}^B = (1 - 2\alpha)R_{32}^B$$

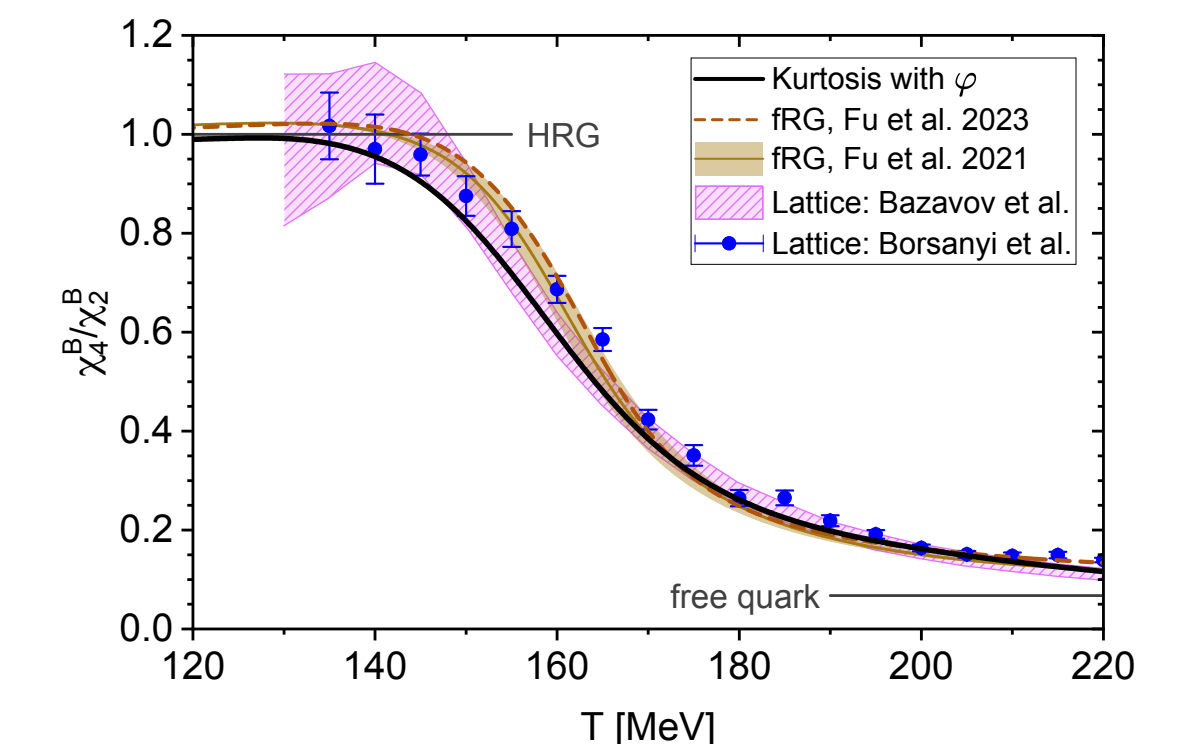
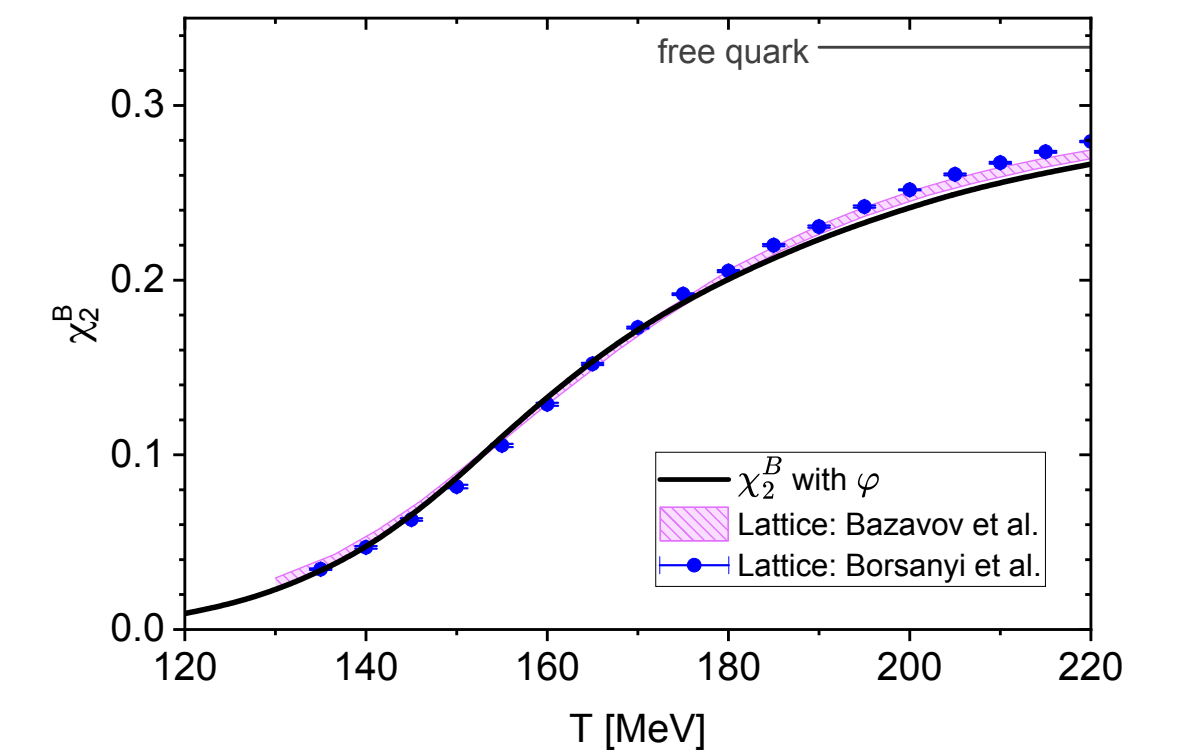
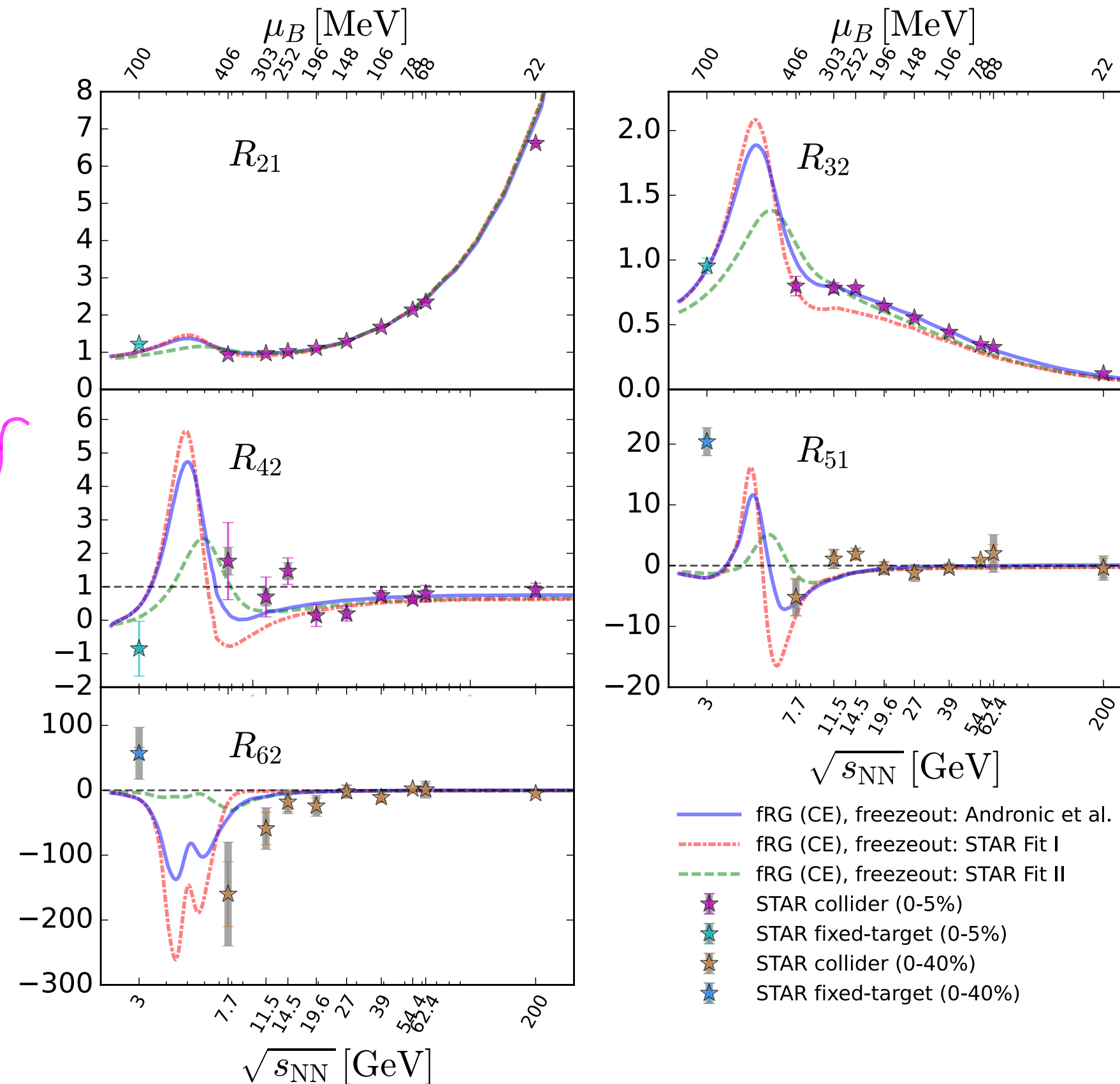


qualitative adjustment

$$\alpha(\bar{s}) = a \left(1 - \sqrt{\bar{s}}\right) \theta(1 - \bar{s})$$

$$a = 0.33$$

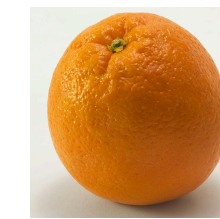
$$\sqrt{\bar{s}} = \frac{\sqrt{s_{NN}}}{11.9 \text{ GeV}}$$



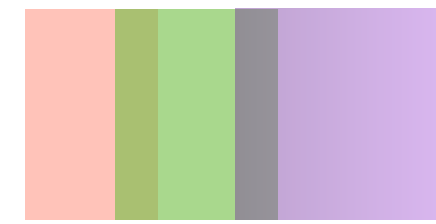
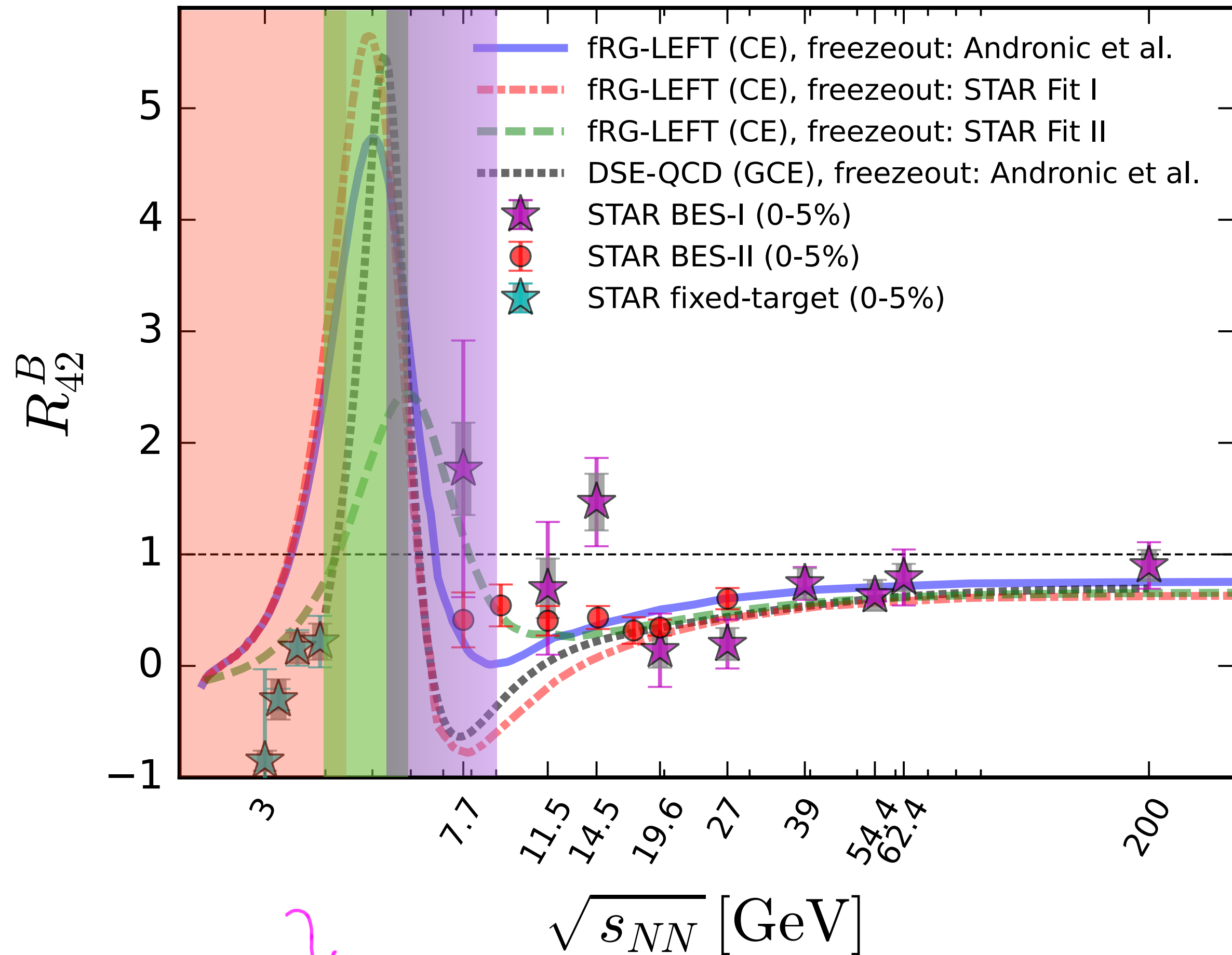
Gao, Liu, Lu, JMP, PRD 113 (2026) 054019



Ripples of the critical point at chemical freeze-out



net-baryon fluctuations in QCD vs net-proton fluctuations at STAR



Dominated by non-critical soft modes

Results:
**1st principles functional QCD computations
 & low energy effective theories/extrapolations**



& functional QCD



Fu, Luo, JMP, Rennecke, Wen, Yin, PRD 104 (2021) 9

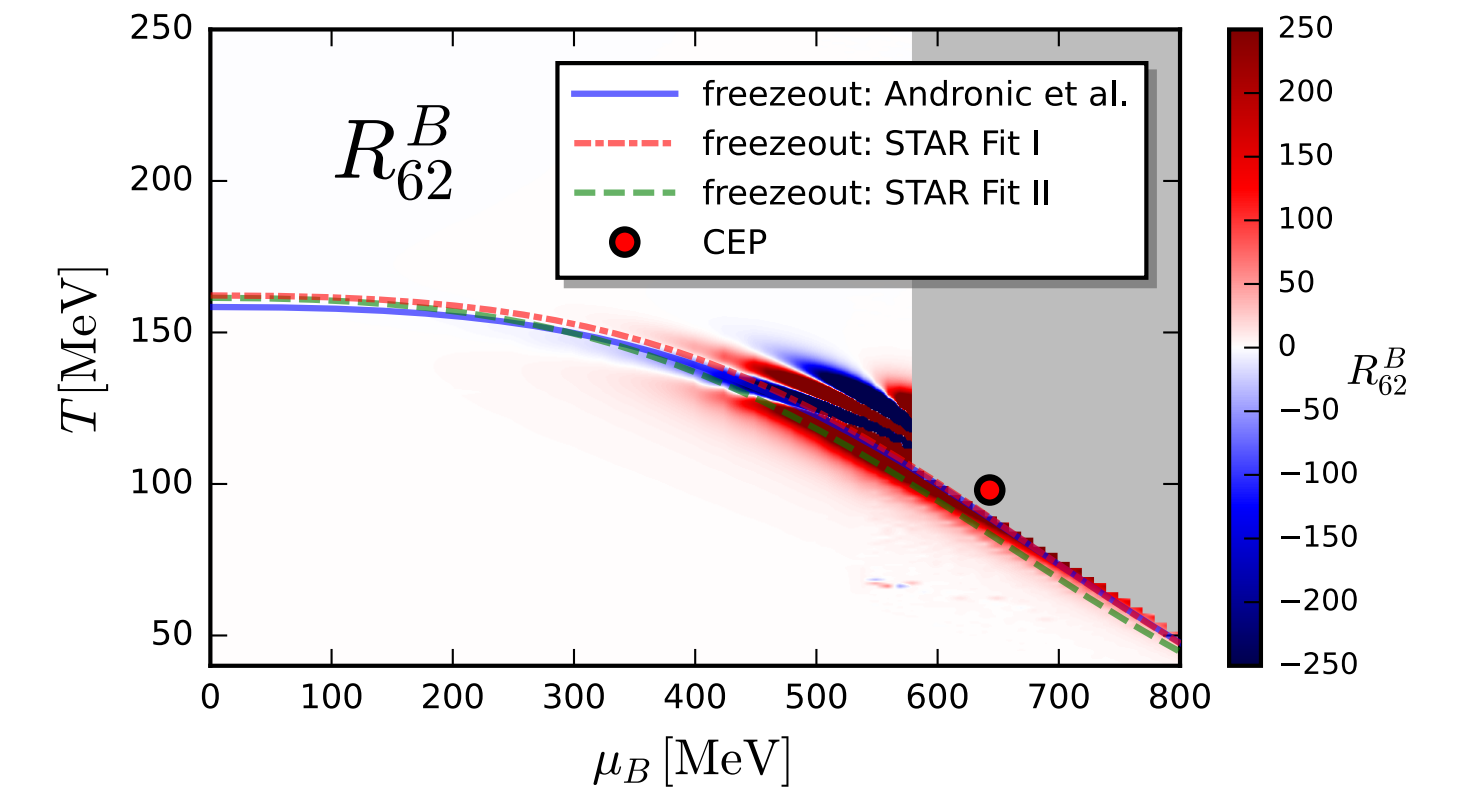
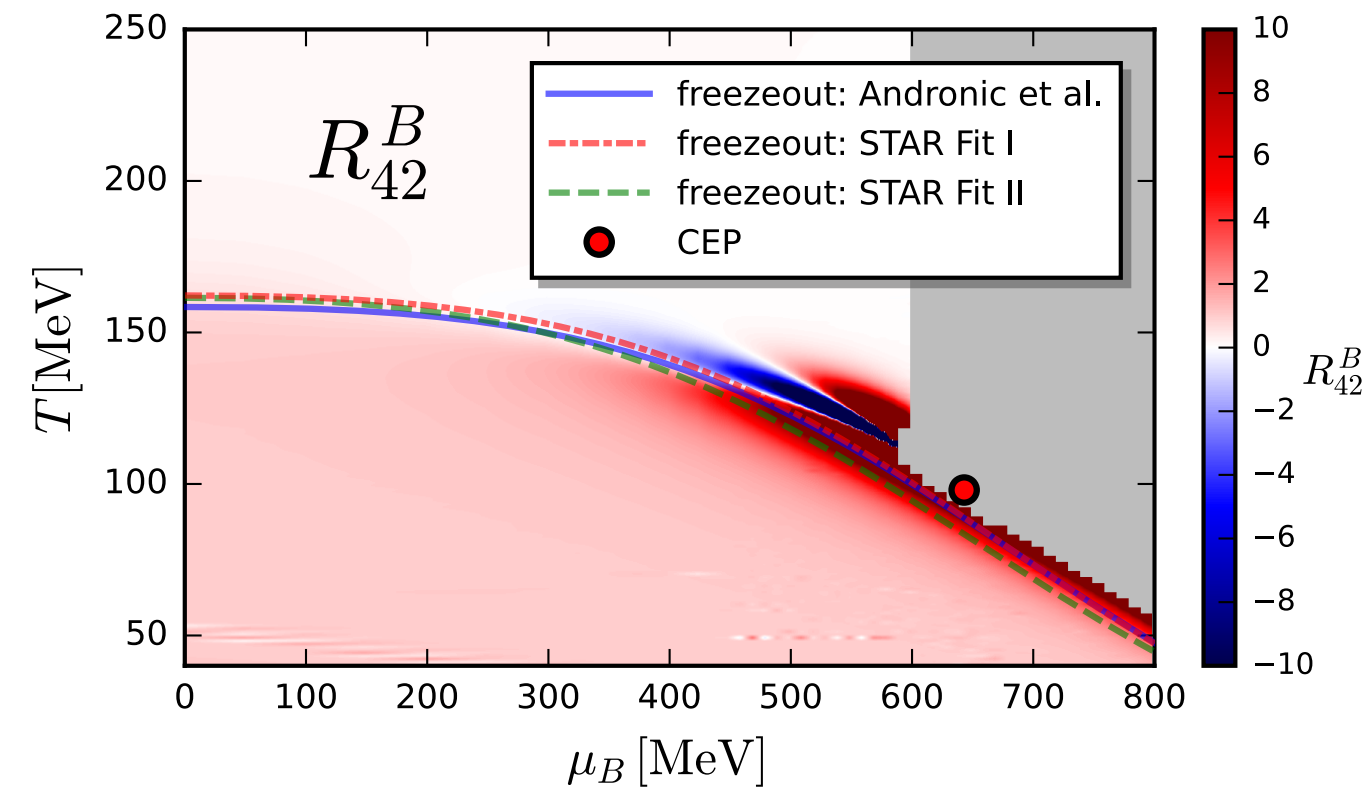
Fu, Luo, JMP, Rennecke, Yin, PRD 111, L031502

Functional QCD: Lu, Gao, Liu, JMP, 113 (2026) 054019

Ripples of the critical point

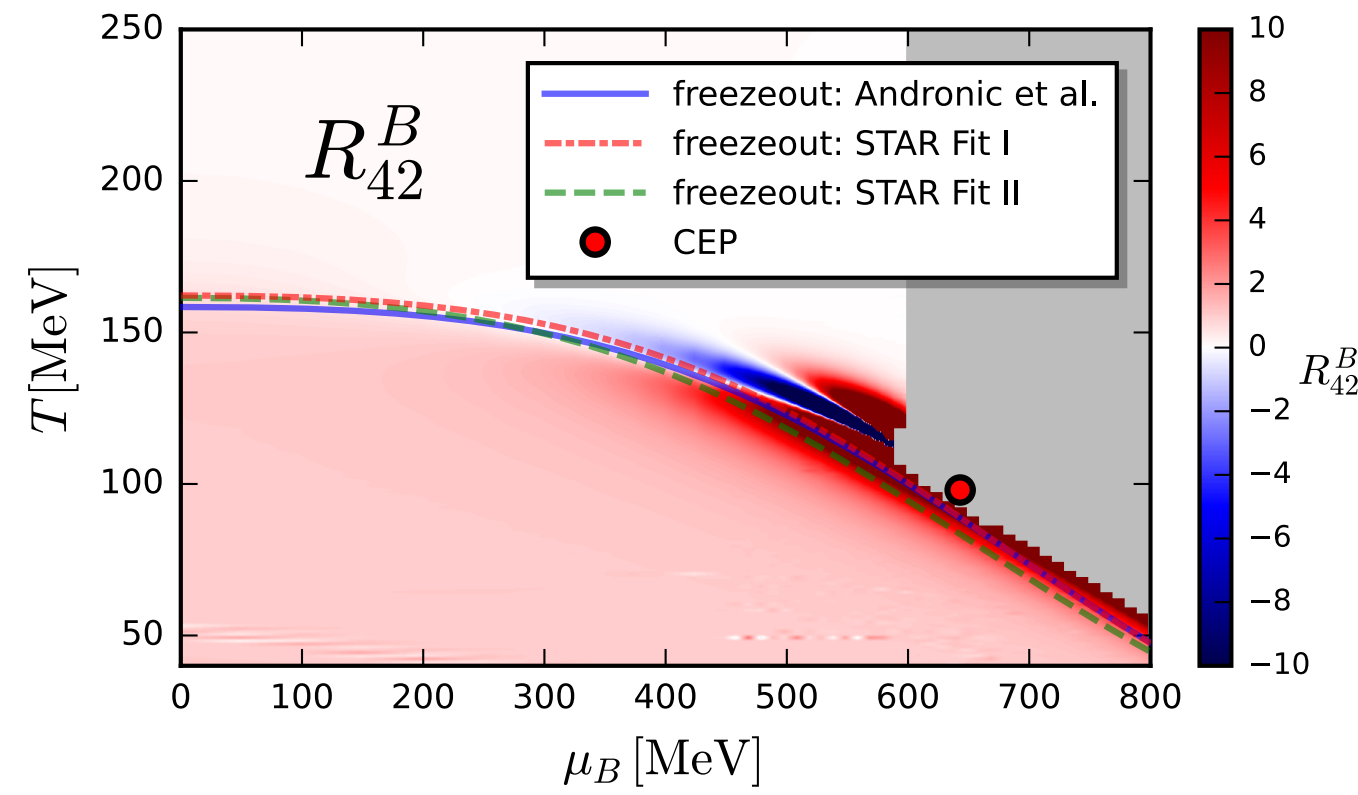
baryon number fluctuations in the phase structure

$$(T_{\text{CEP}}, \mu_{B_{\text{CEP}}}) = (98, 643) \text{ MeV}$$



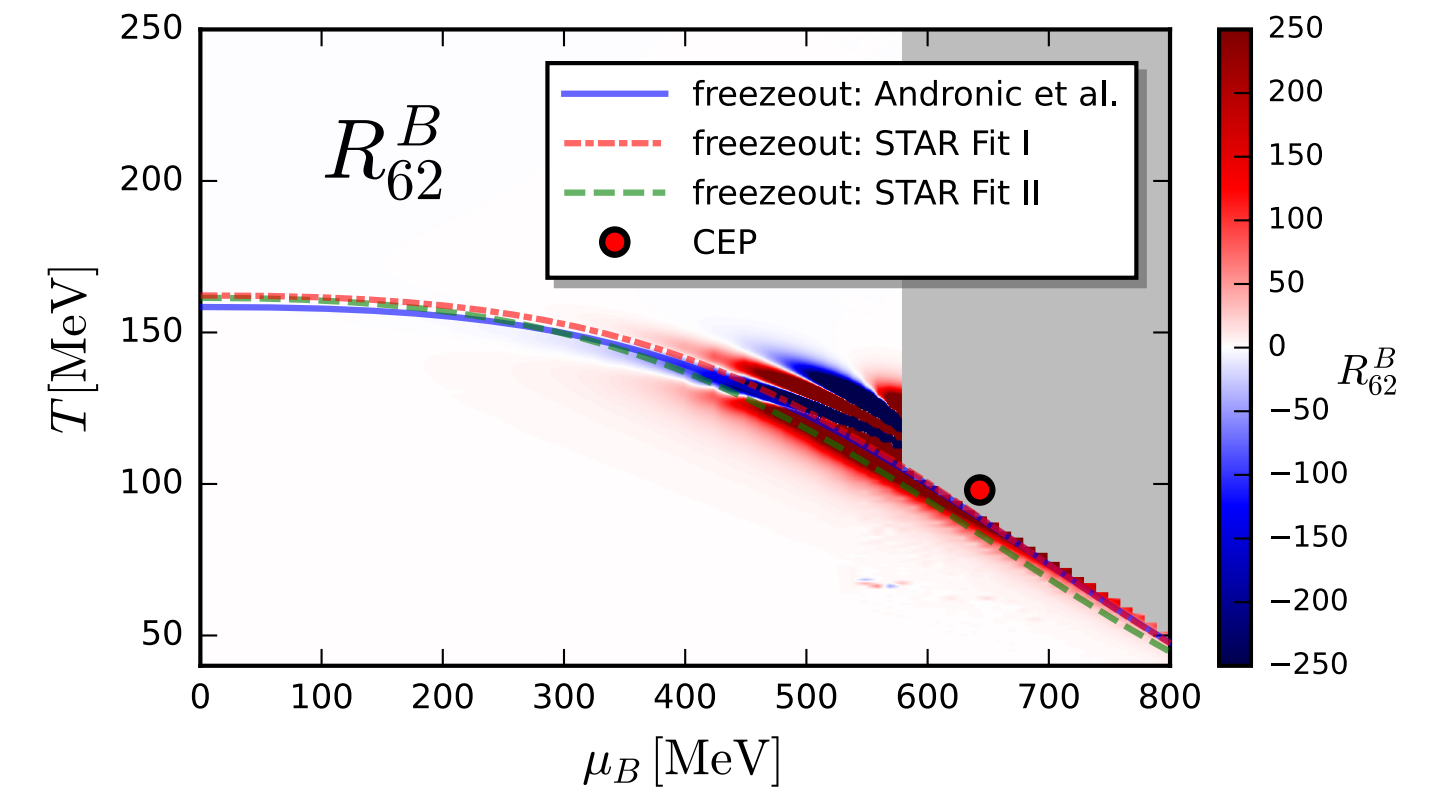
Ripples of the critical point

baryon number fluctuations in the phase structure

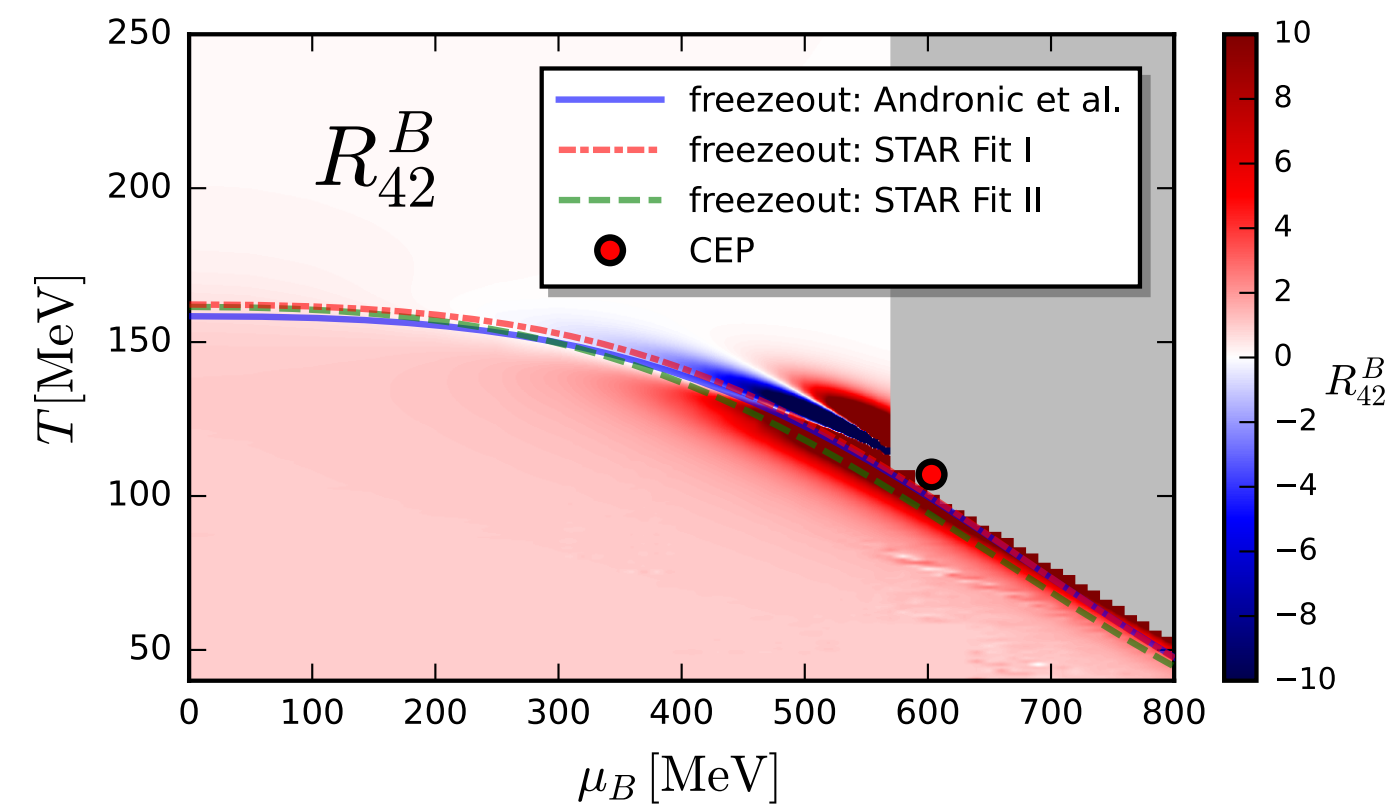


$$(T_{\text{CEP}}, \mu_{B_{\text{CEP}}}) = (98, 643) \text{ MeV}$$

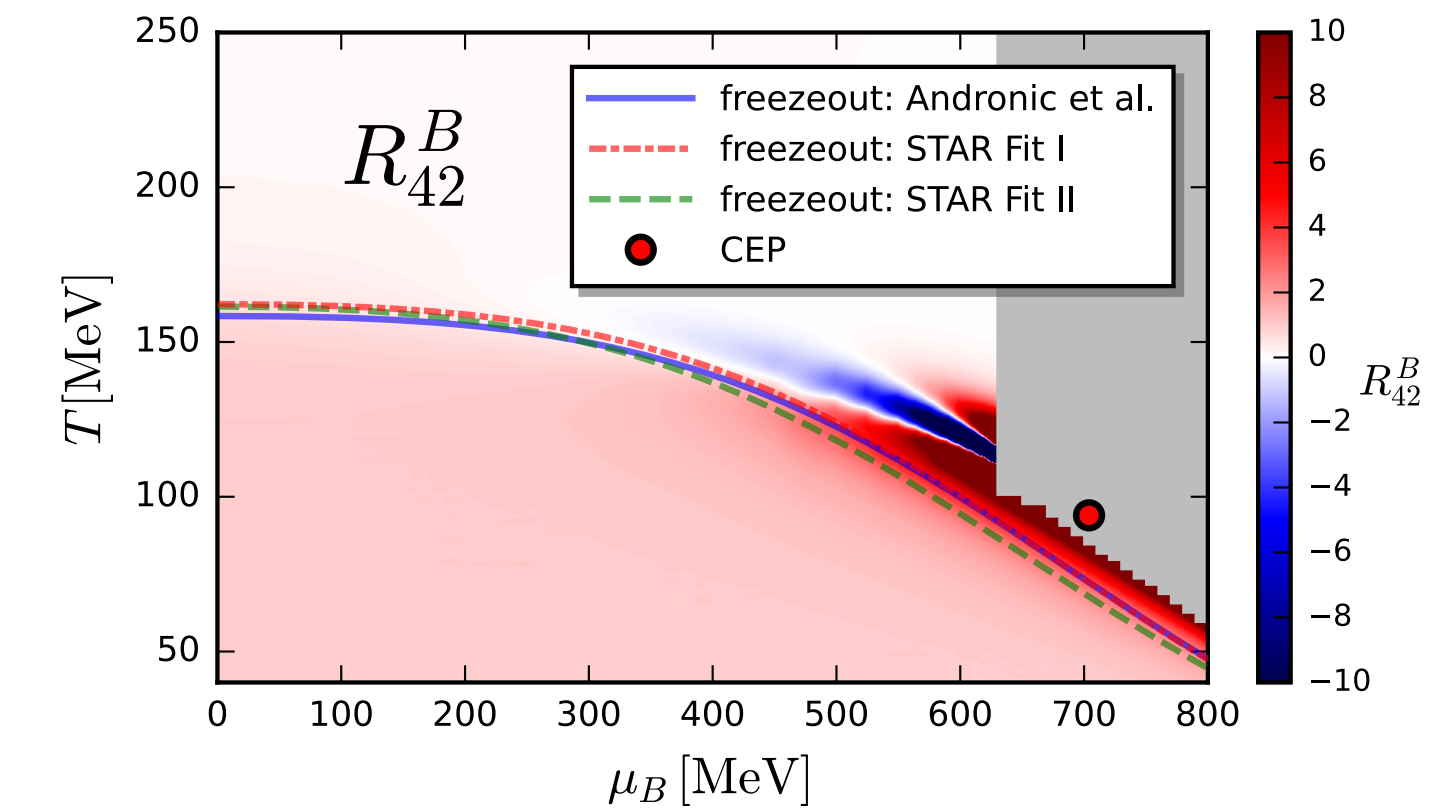
Ride the



Variations of the CEP in the allowed estimate regime



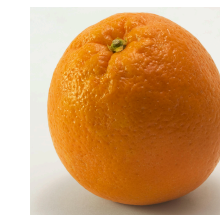
$$(T_{\text{CEP}}, \mu_{B_{\text{CEP}}}) = (108, 604) \text{ MeV}$$



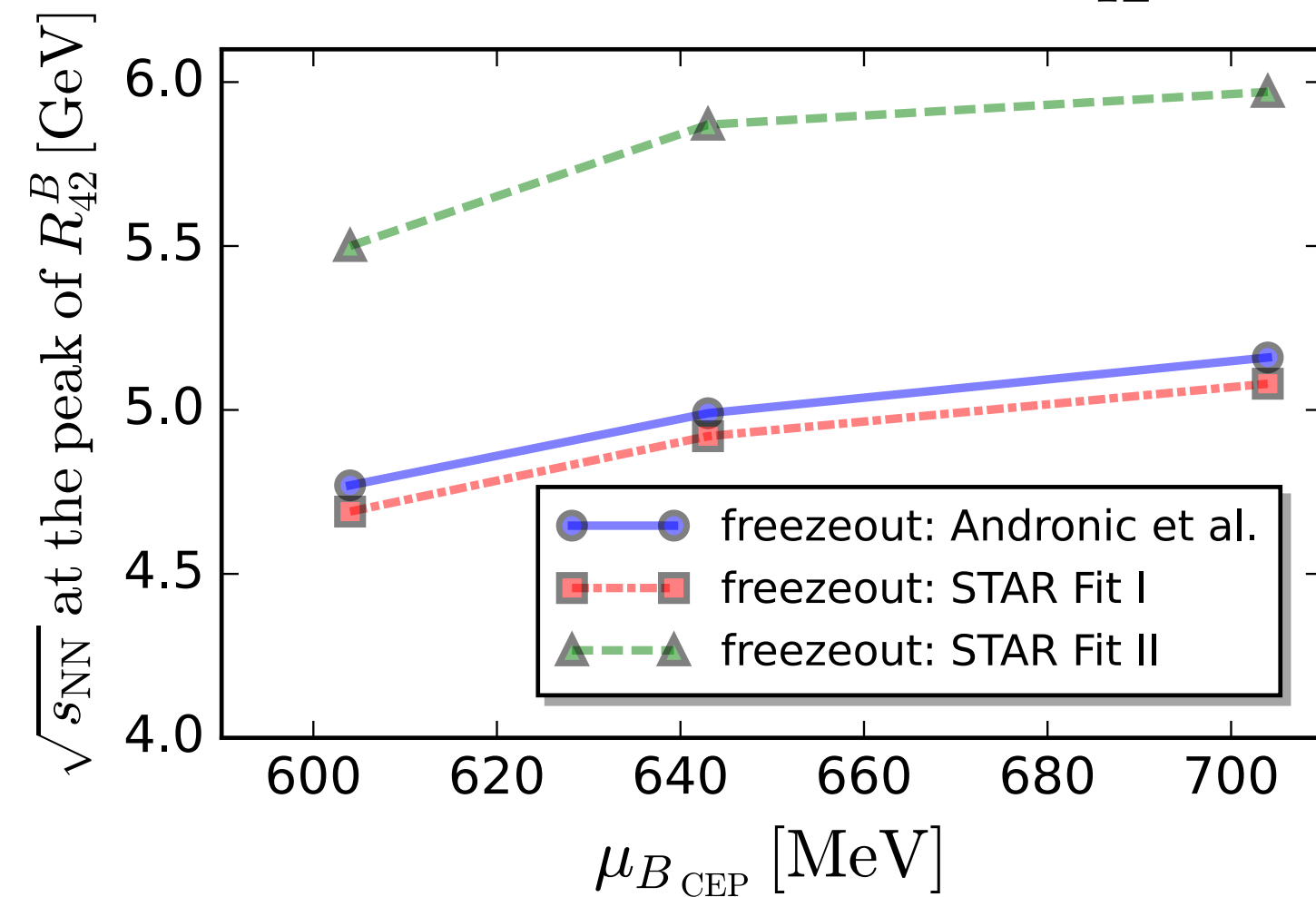
$$(T_{\text{CEP}}, \mu_{B_{\text{CEP}}}) = (94, 704) \text{ MeV}$$



Ripples of the critical point at chemical freeze-out

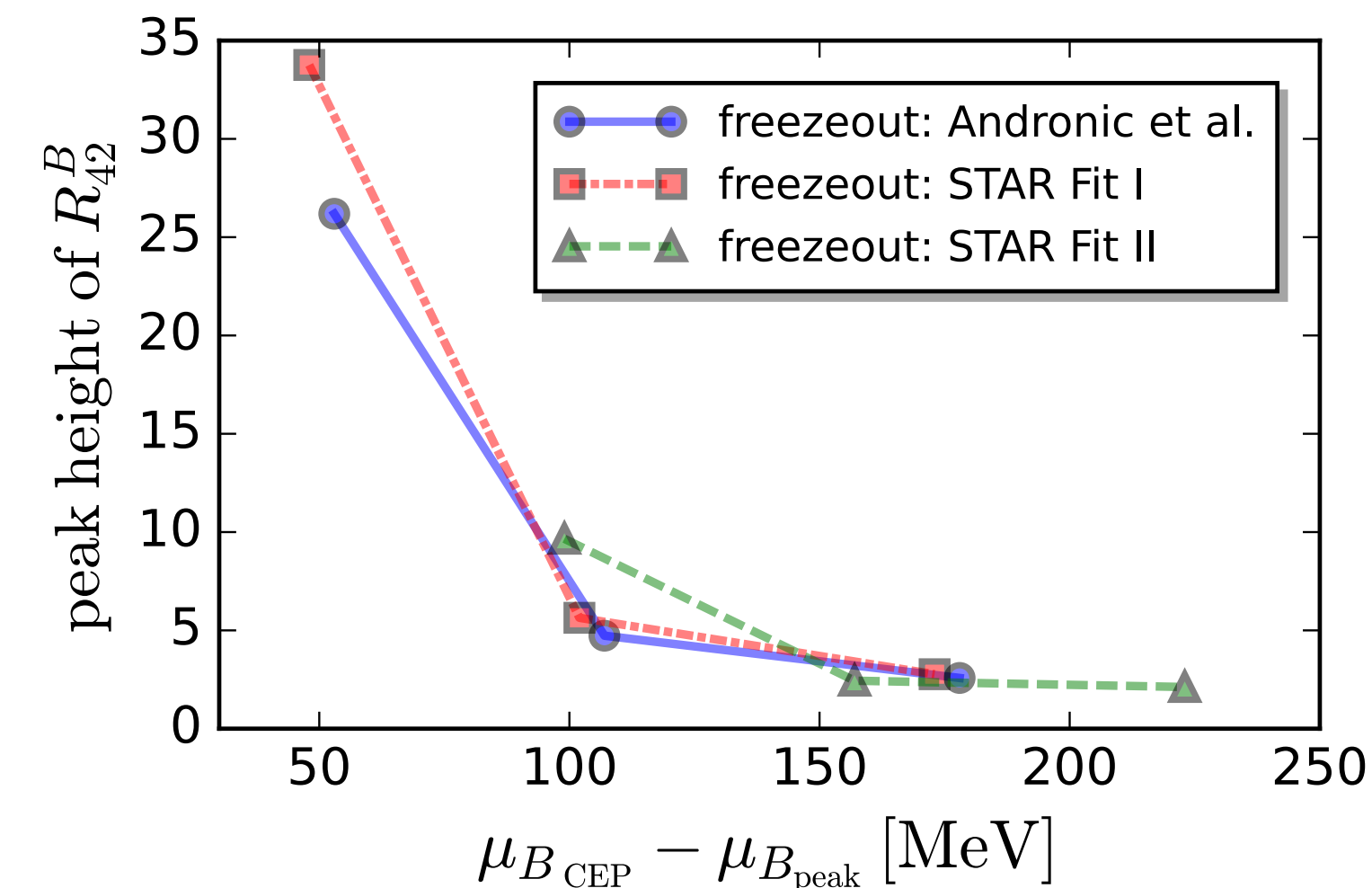


Position of the peak of R_{42}^B



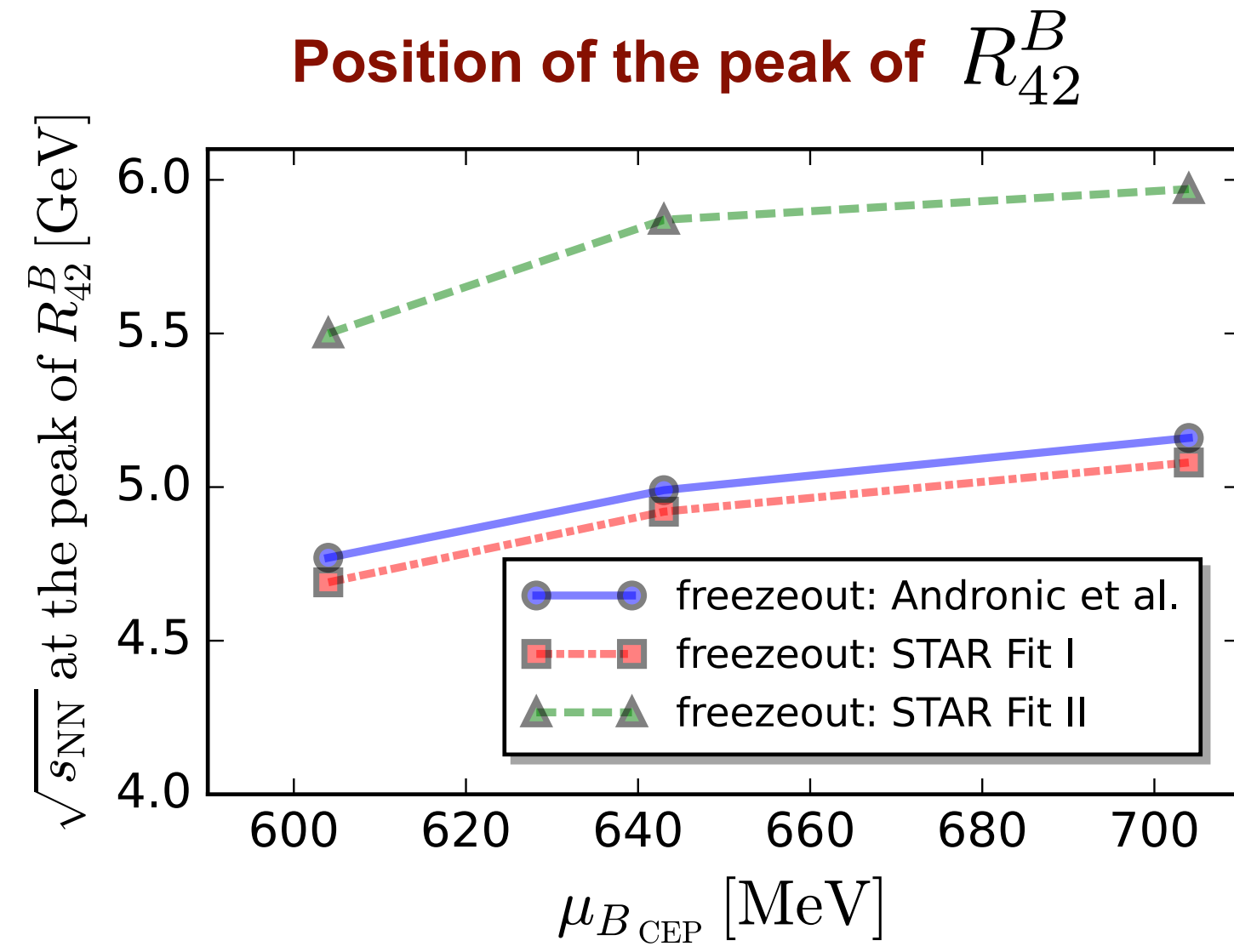
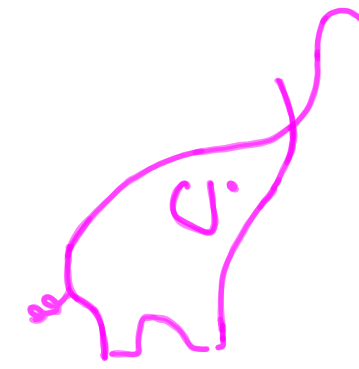
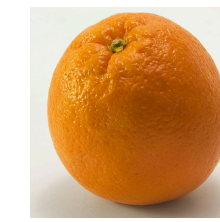
Reconstructing the CEP

Height of the peak of R_{42}^B

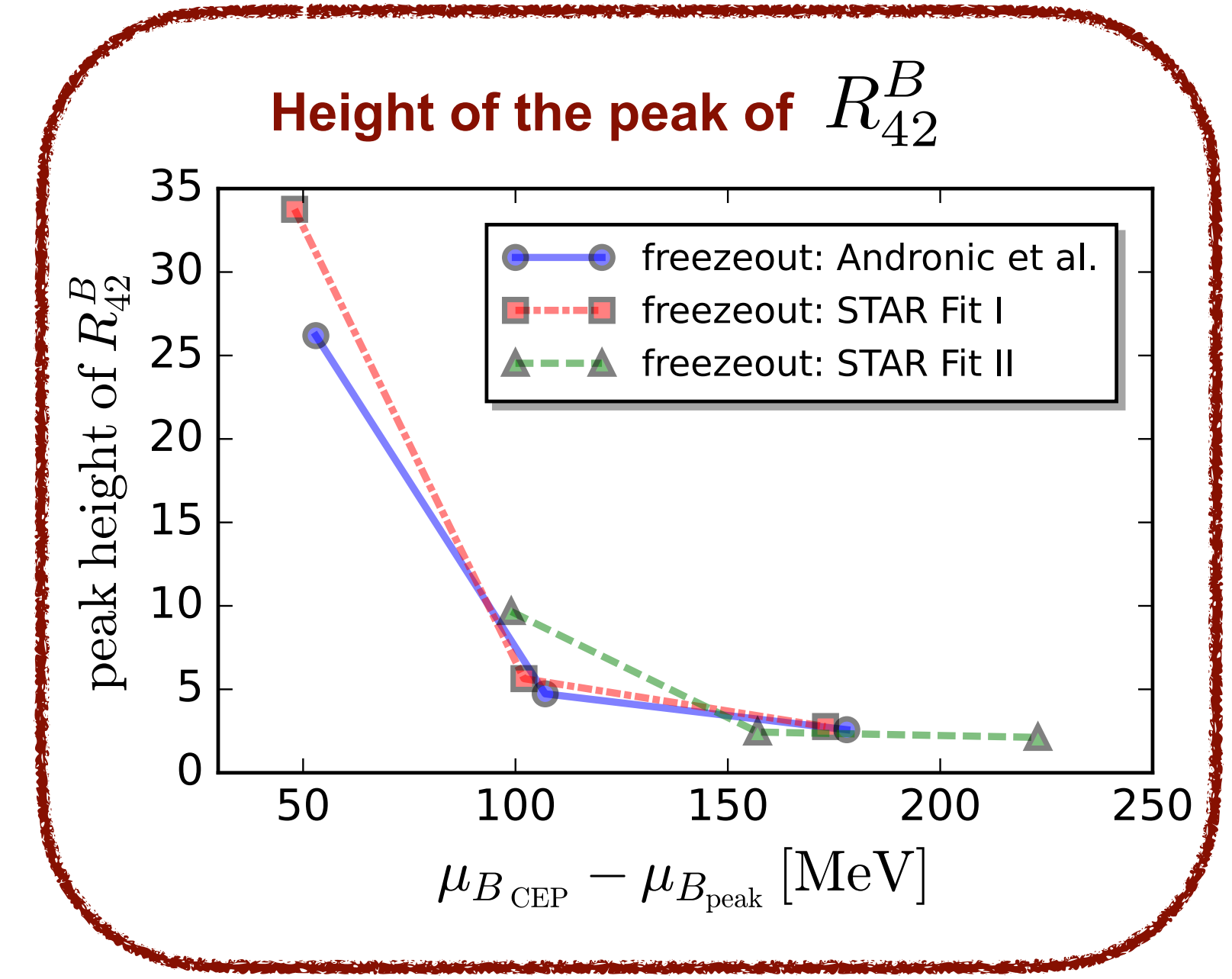




Ripples of the critical point at chemical freeze-out

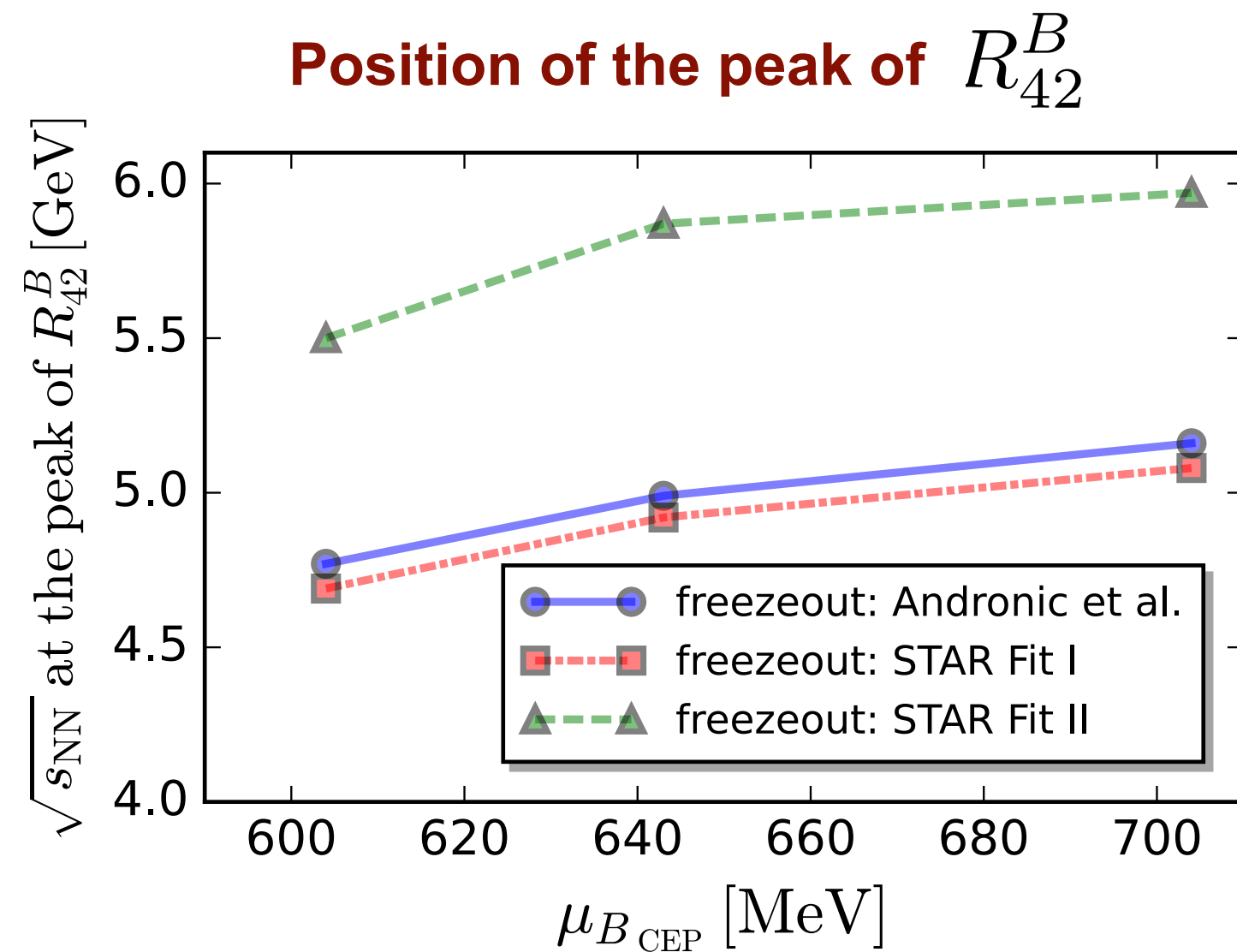
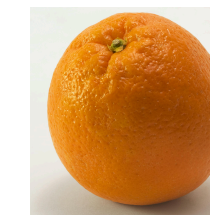


Reconstructing the CEP

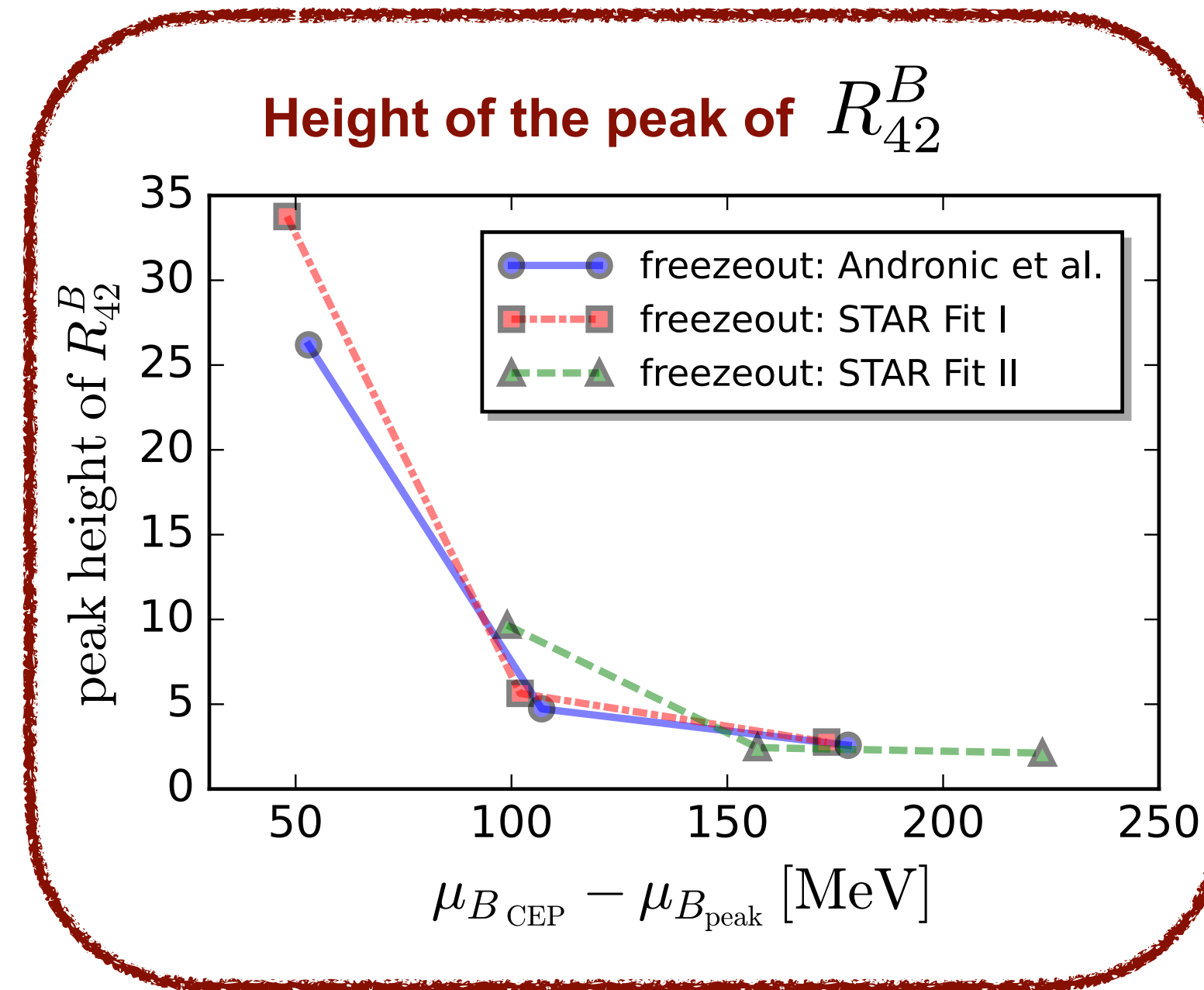




Ripples of the critical point at chemical freeze-out



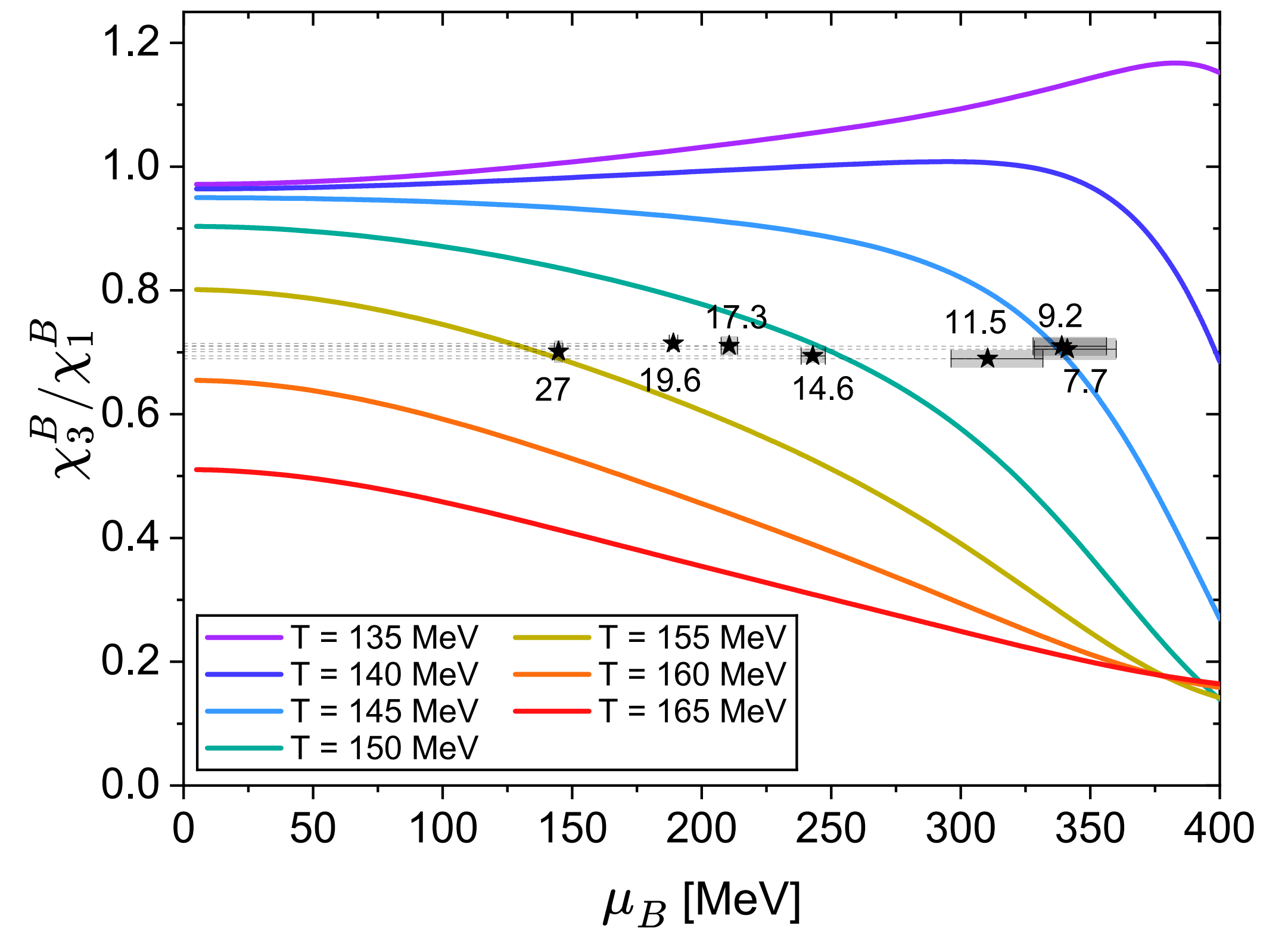
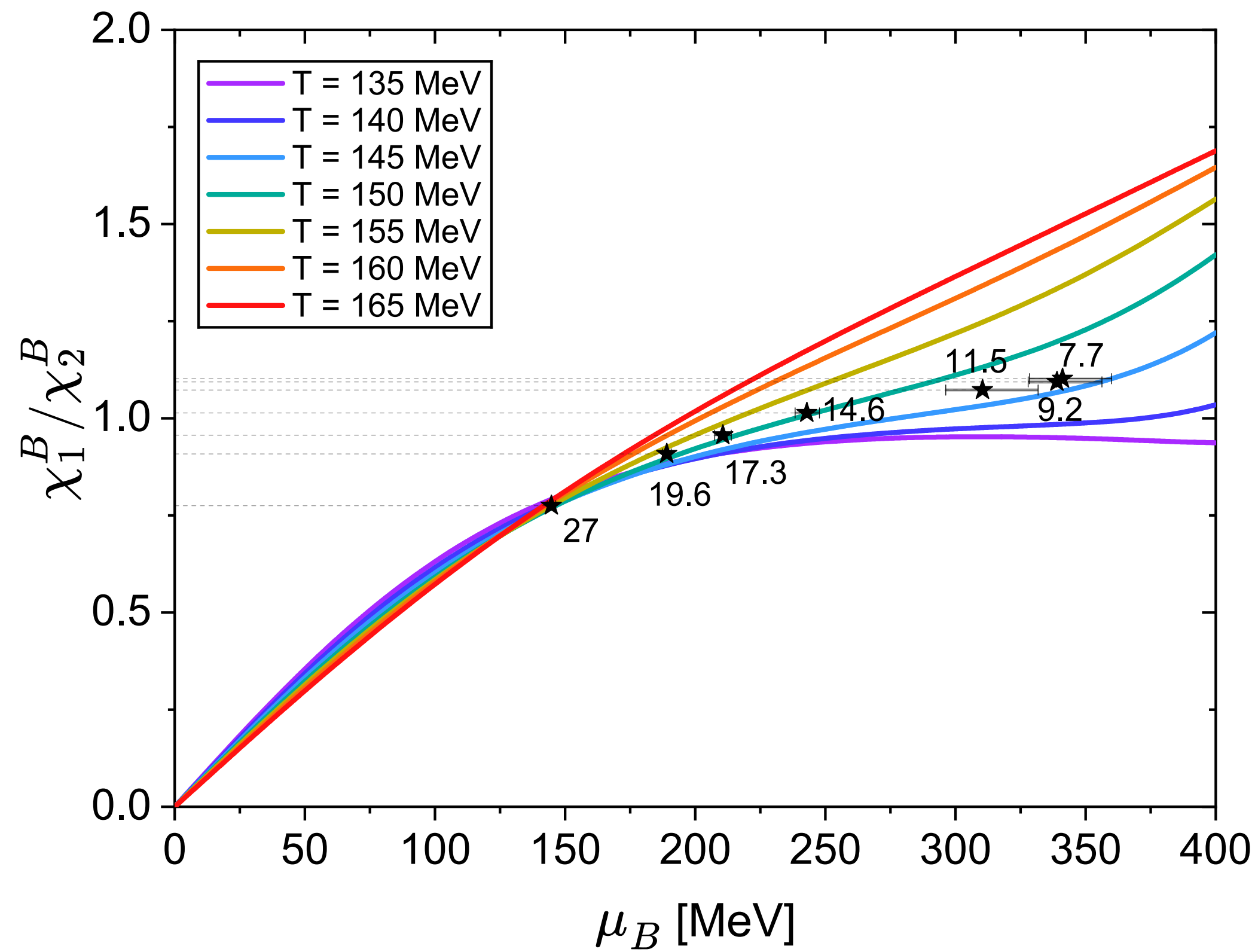
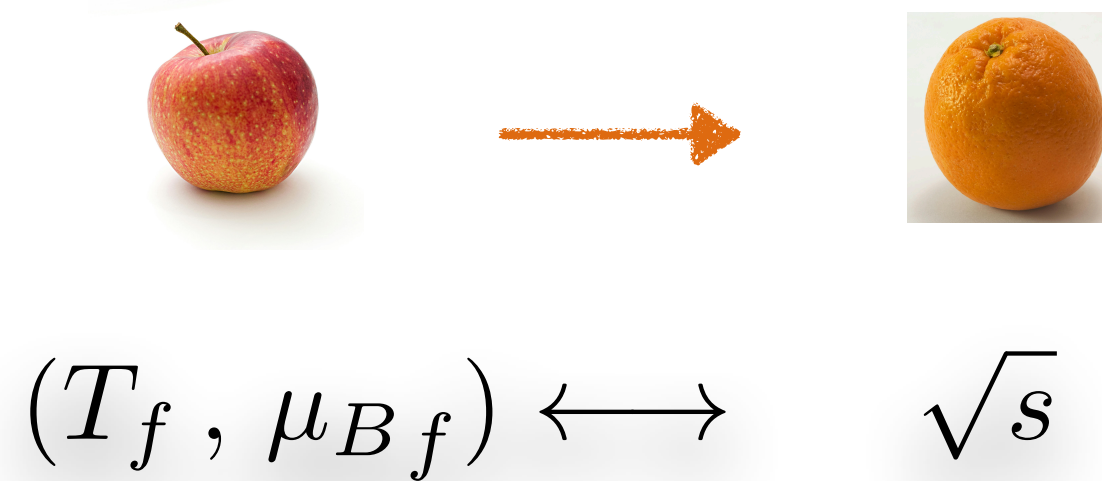
Reconstructing the CEP



Unfolding the high density regime with new phases & physics

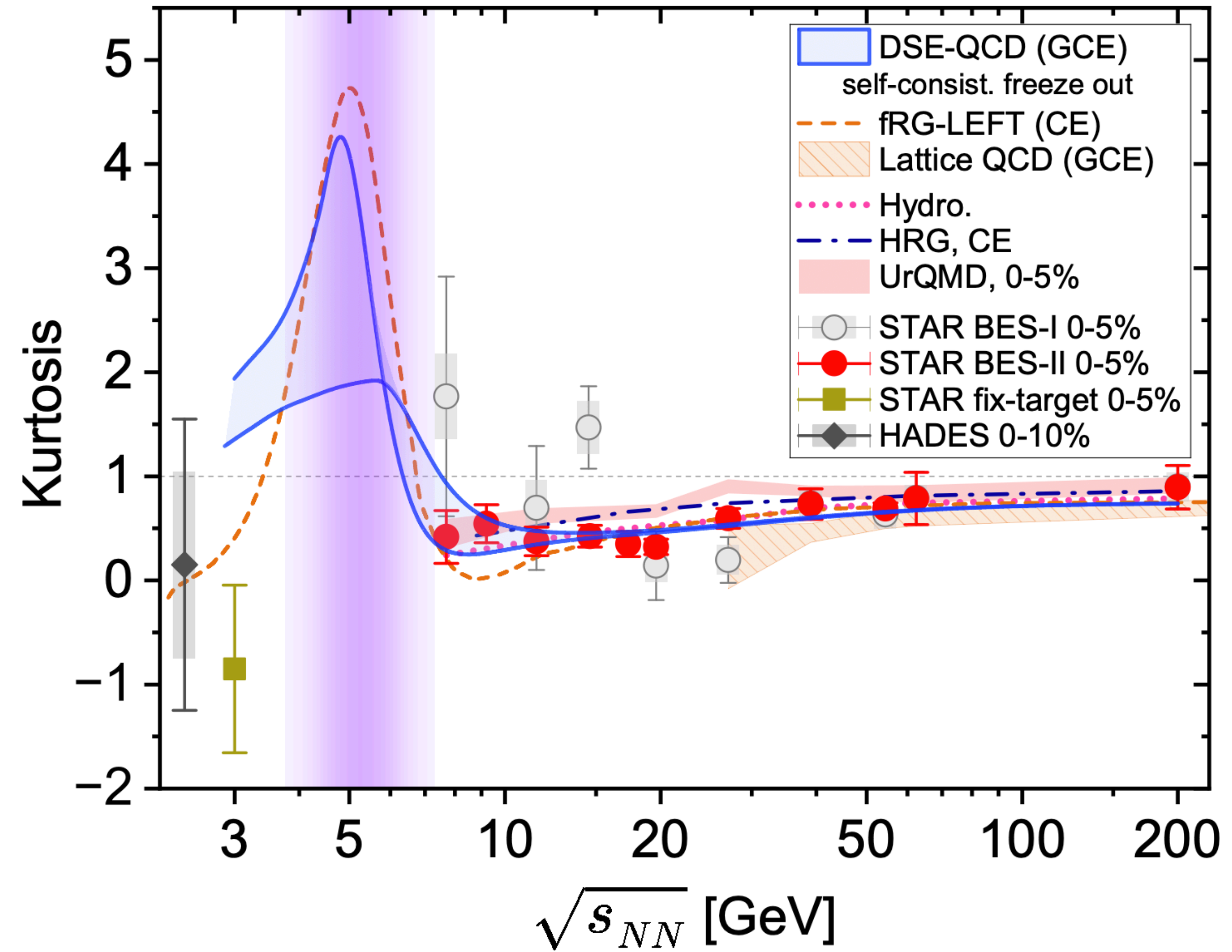
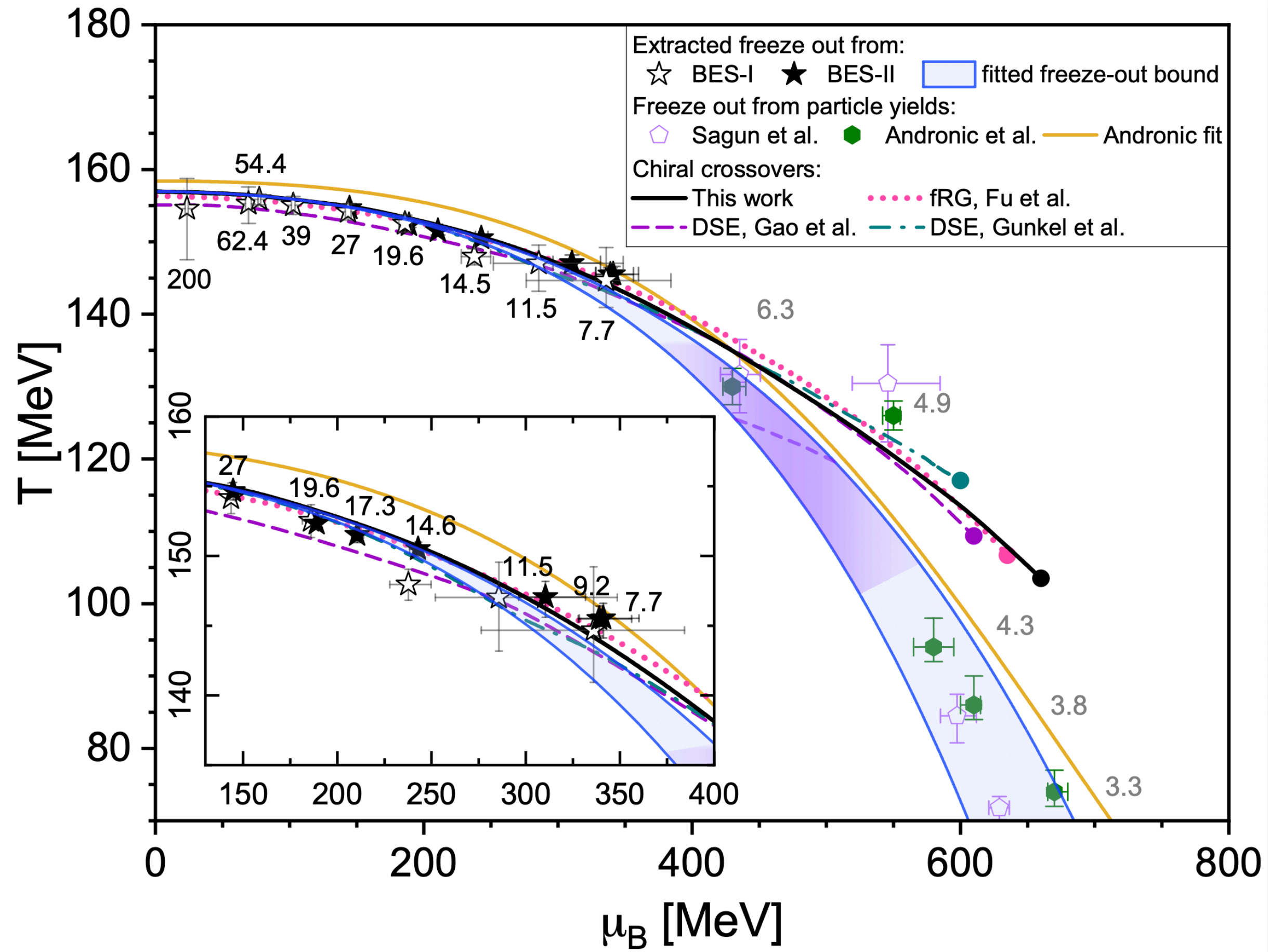
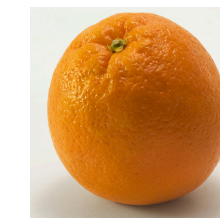
Great opportunity for a combined high precision analysis of high density QCD (Exp. data + lattice QCD + functional QCD)

Functional Freeze-out



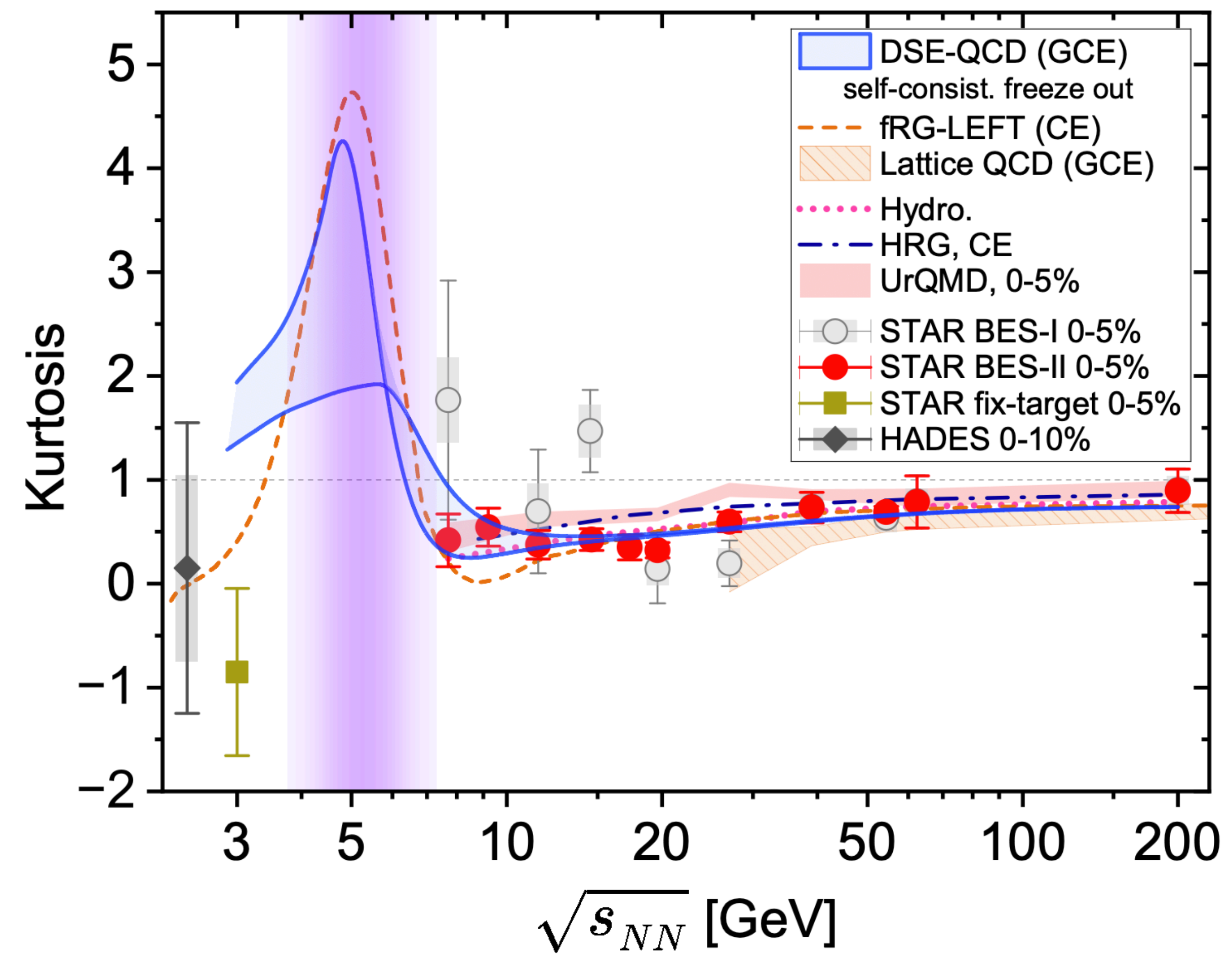
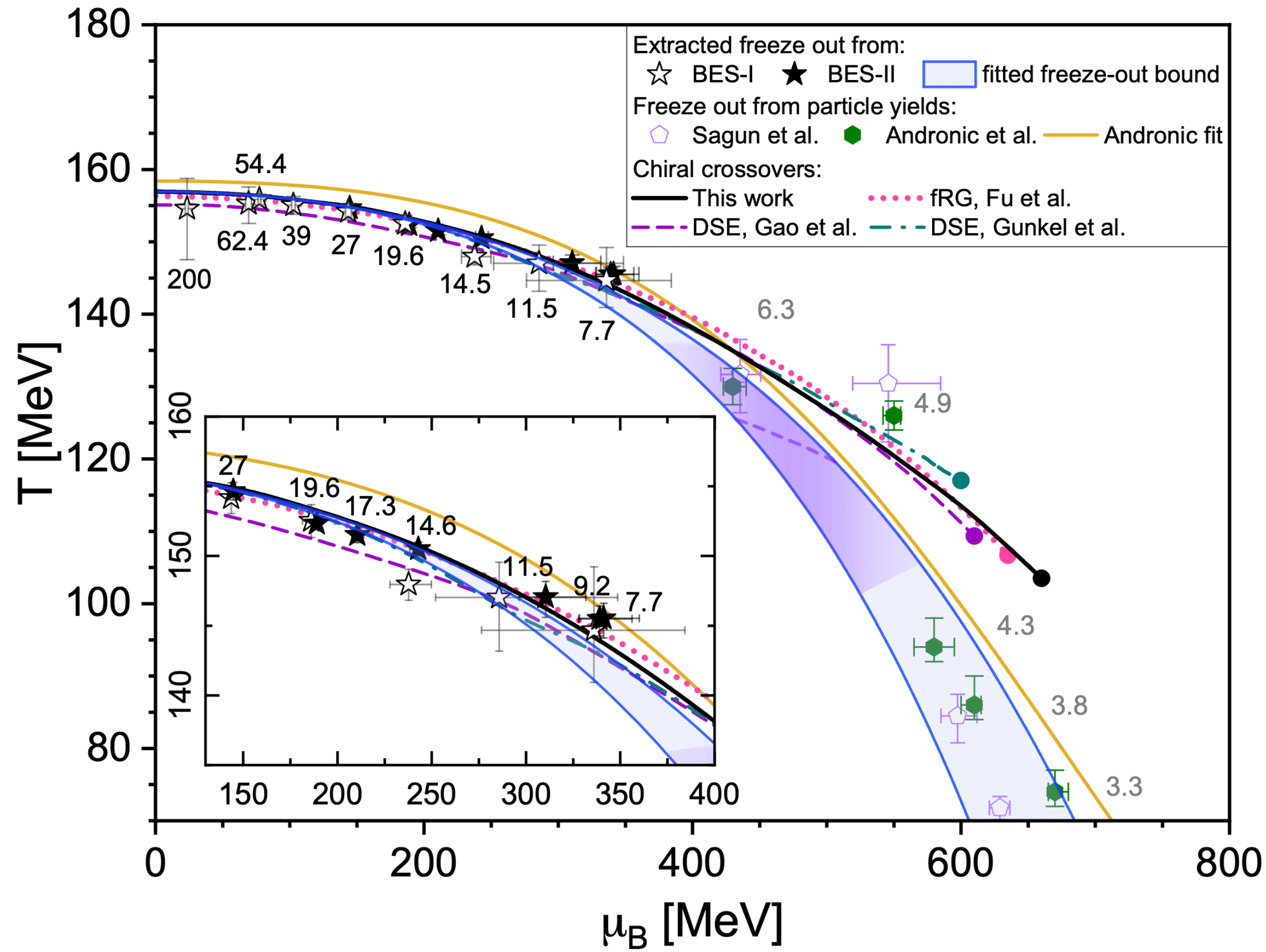
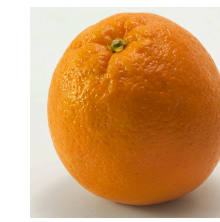


Ripples of the critical point at chemical freeze-out



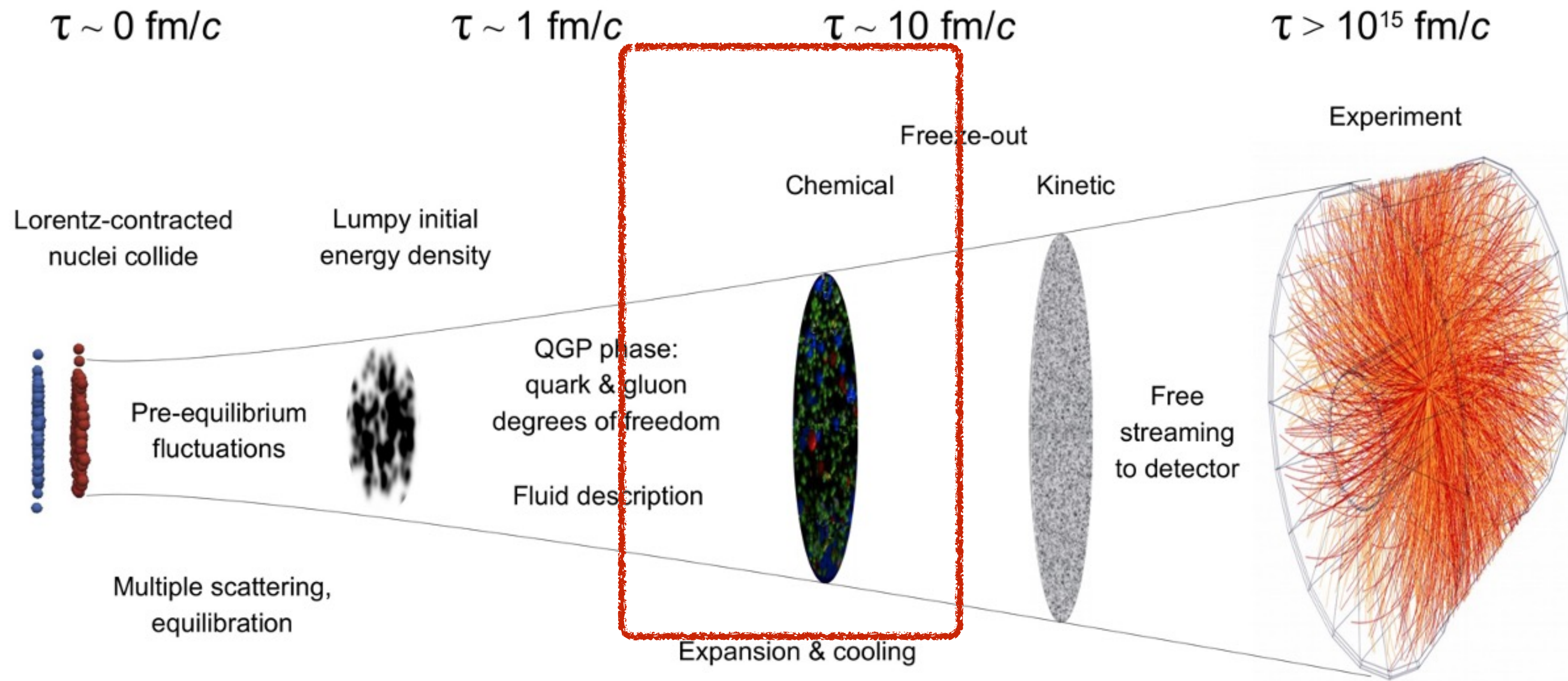


Ripples of the critical point at chemical freeze-out



Demand: build in dynamics

Unfolding strongly correlated QCD with heavy ion collisions (extreme QCD)



How to unfold: inverse problem!

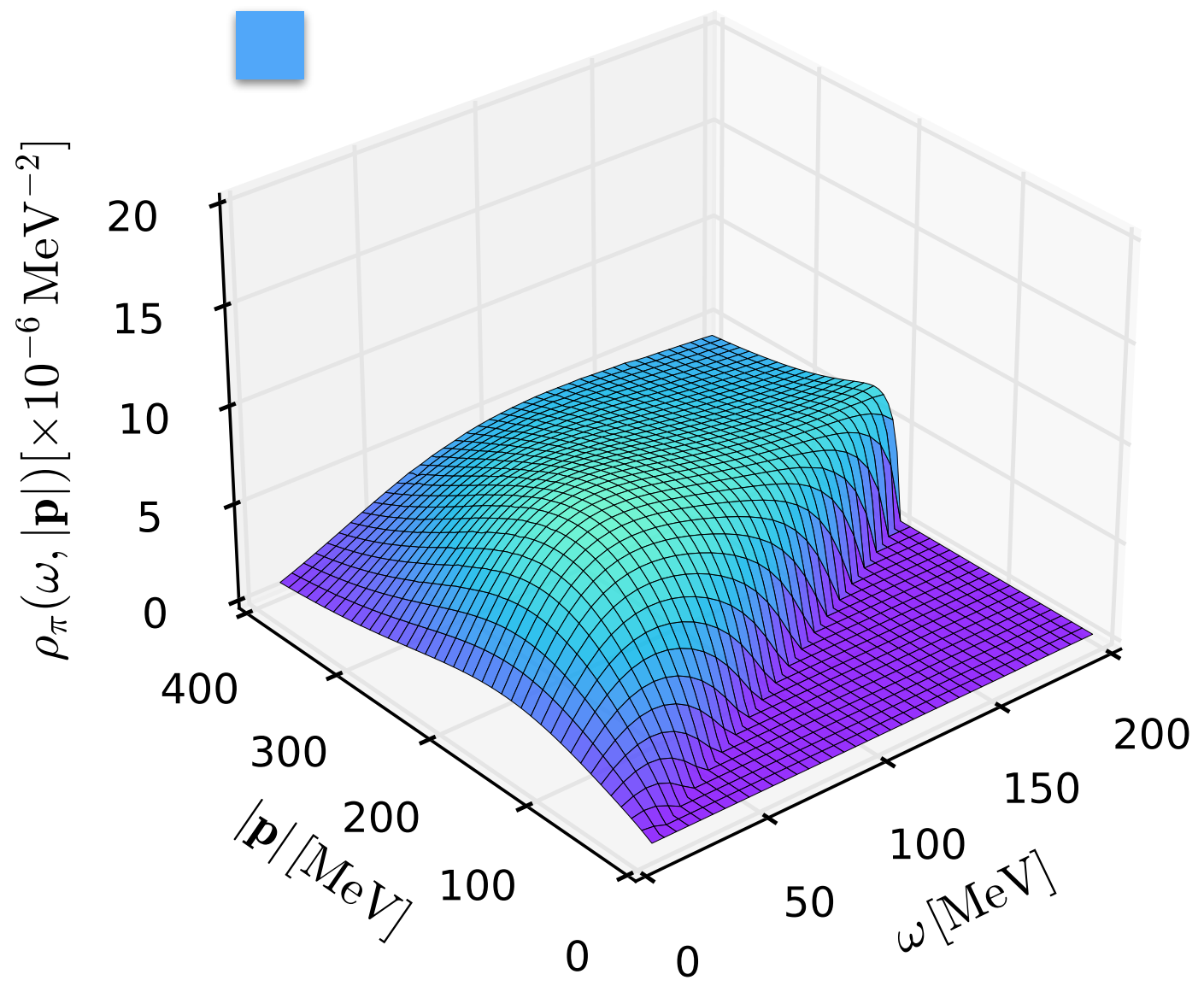
Demand: unfolding HICs

The QCD moat and inhomogeneous phases

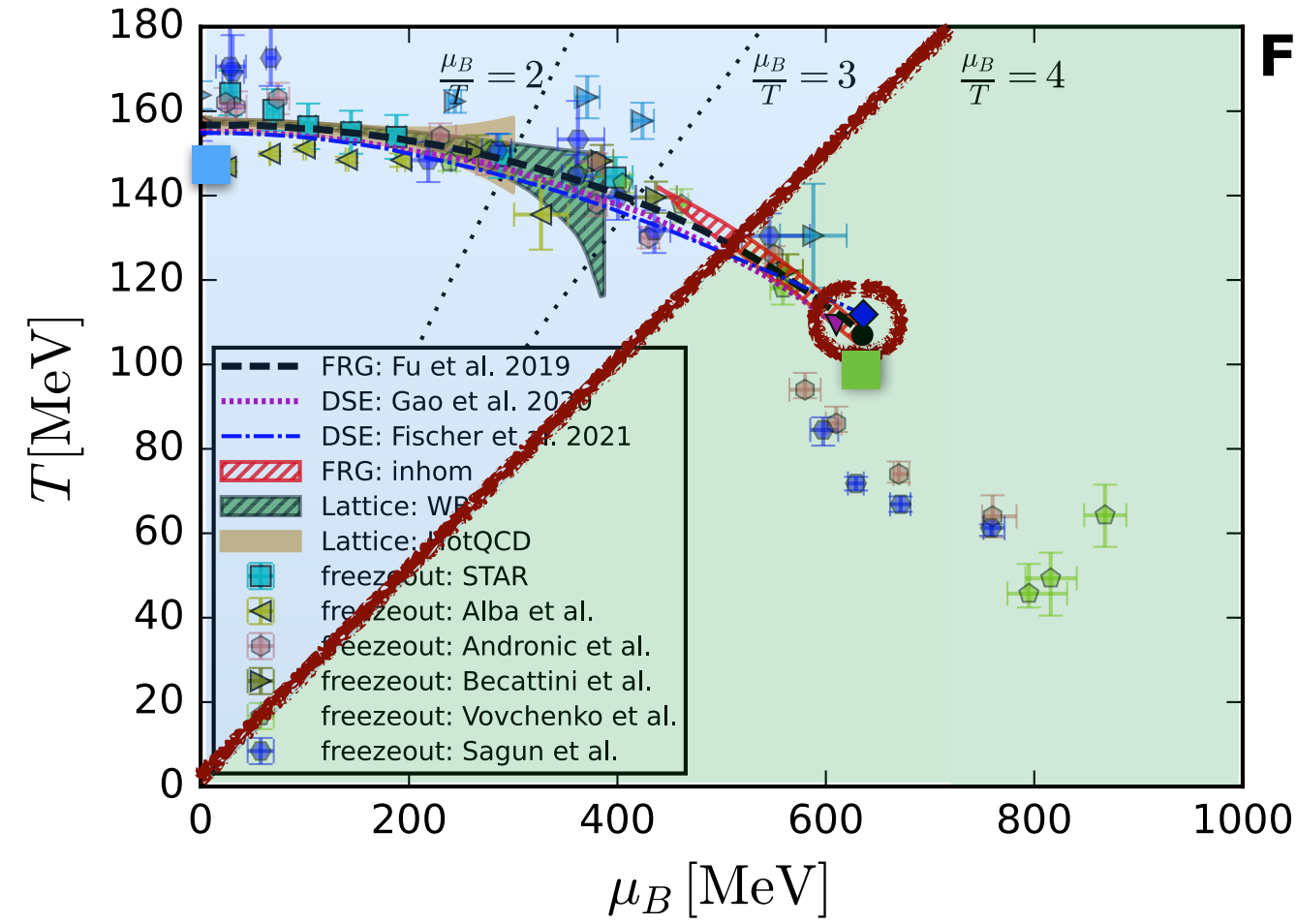
Moat regime

Pisarski, Rennecke, PRL 127 (2021) 152302

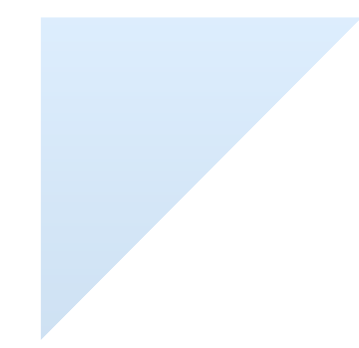
$T=160 \text{ MeV} \ \& \ \mu_B=0 \text{ MeV}$



Prediction



Fu, JMP, Rennecke, PRD 101 (2020) 054032

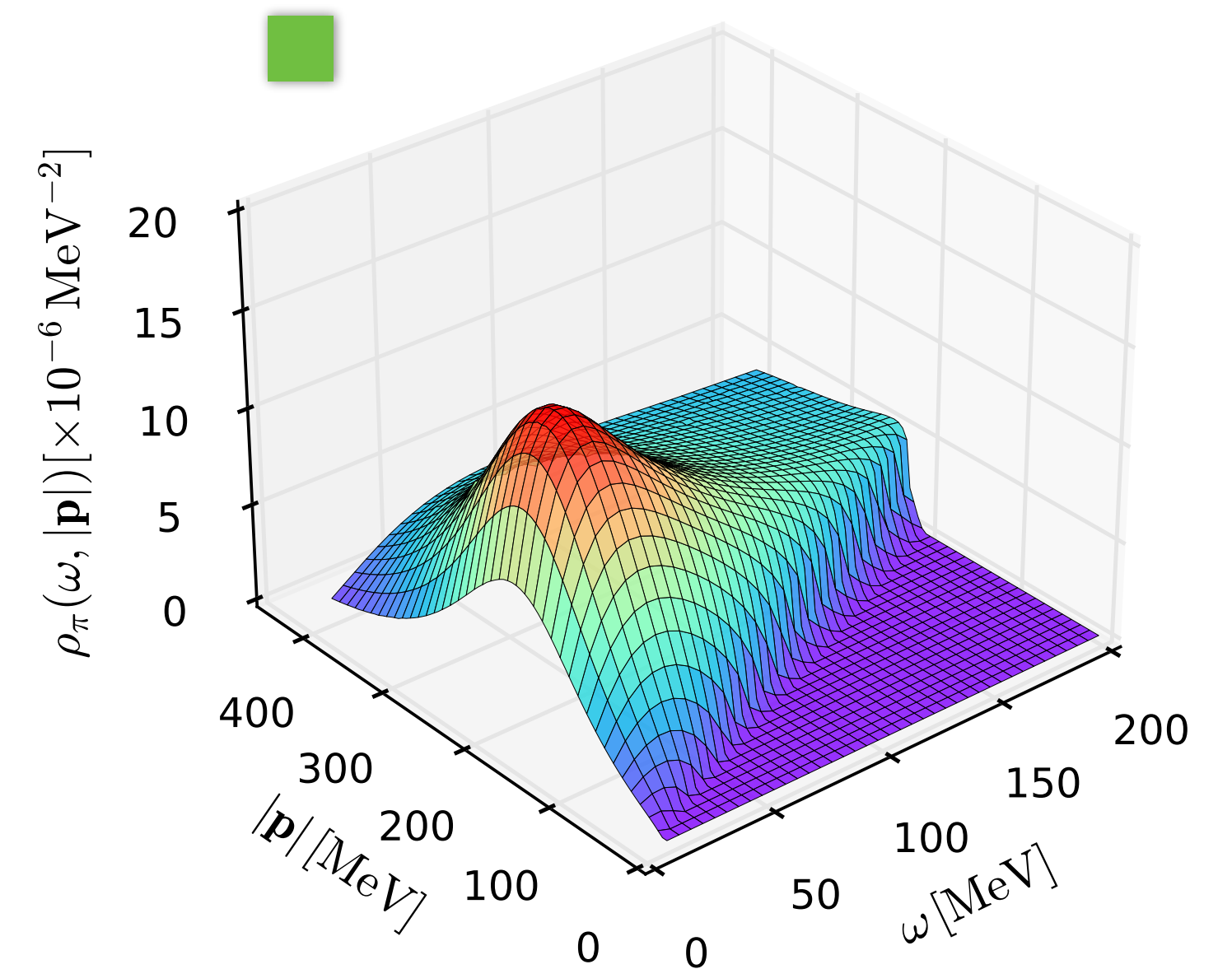


Regime of quantitative reliability of current best truncation

Estimate

Moat regime was not captured quantitatively

$T=114 \text{ MeV} \ \& \ \mu_B=630 \text{ MeV}$

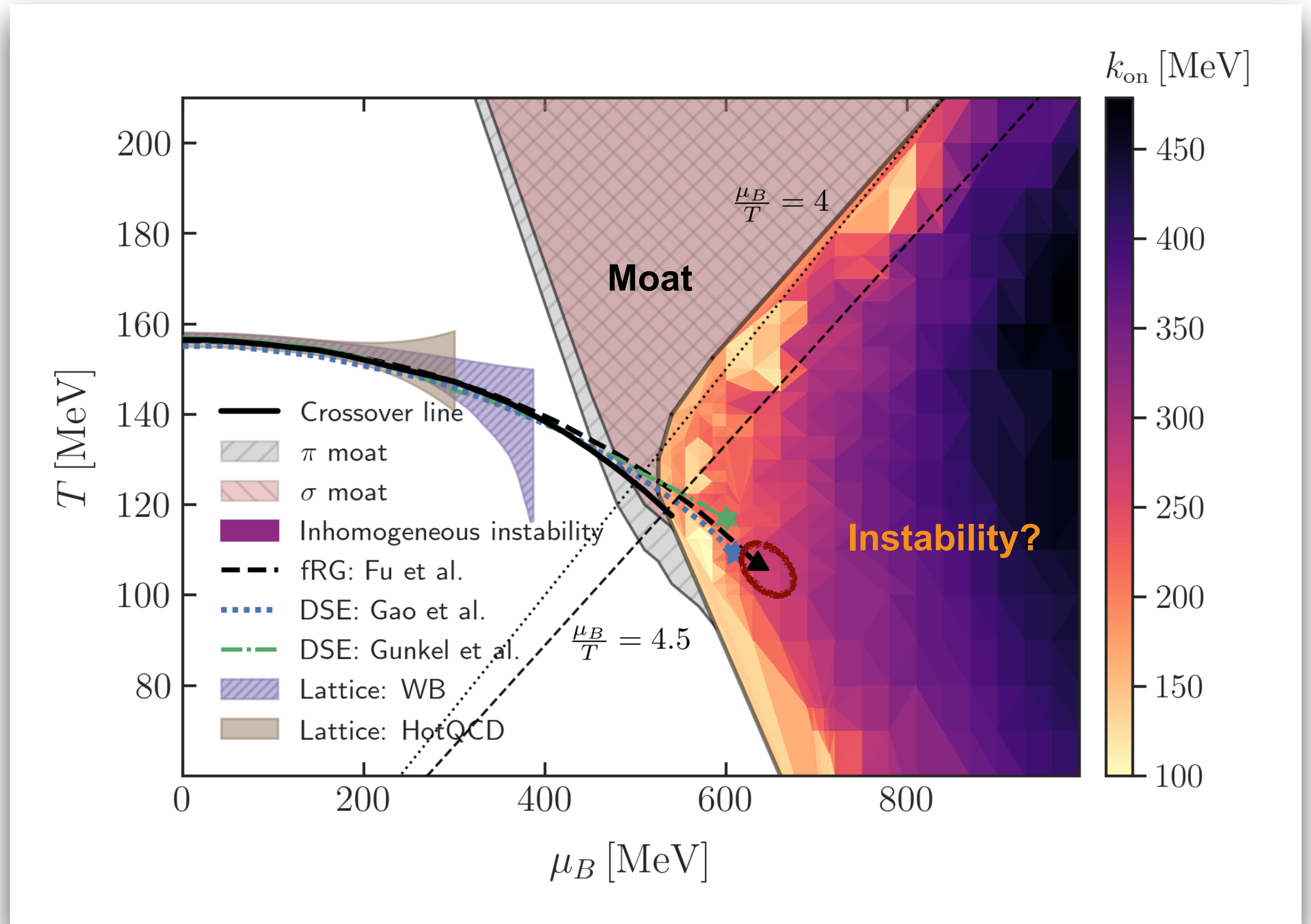


Pion spectral functions

Fu, JMP, Pisarski, Rennecke, Wen, Yin, PRD 111 (2025) 094026

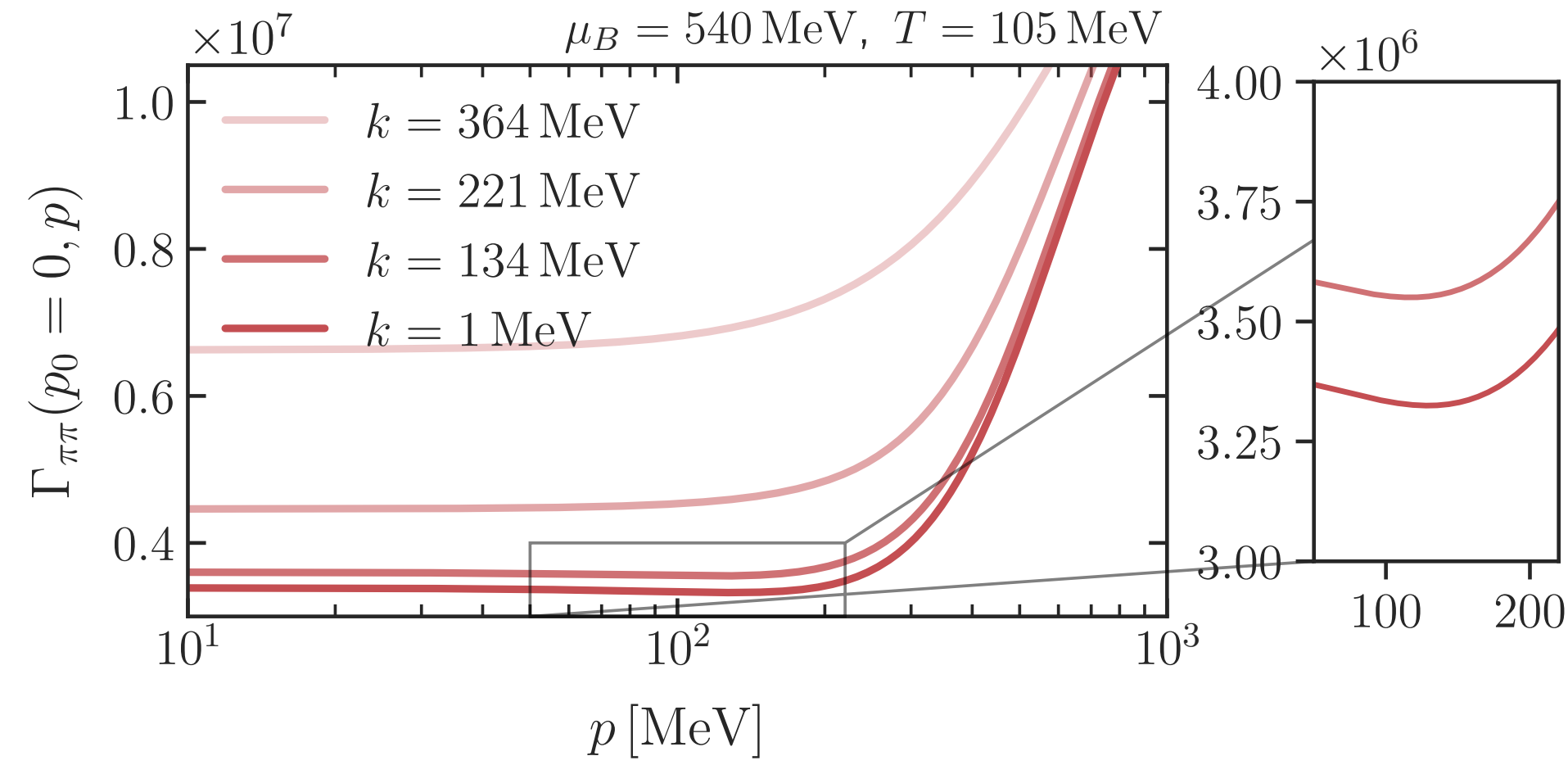
The QCD Moat reloaded

 **Estimated location of CEP**

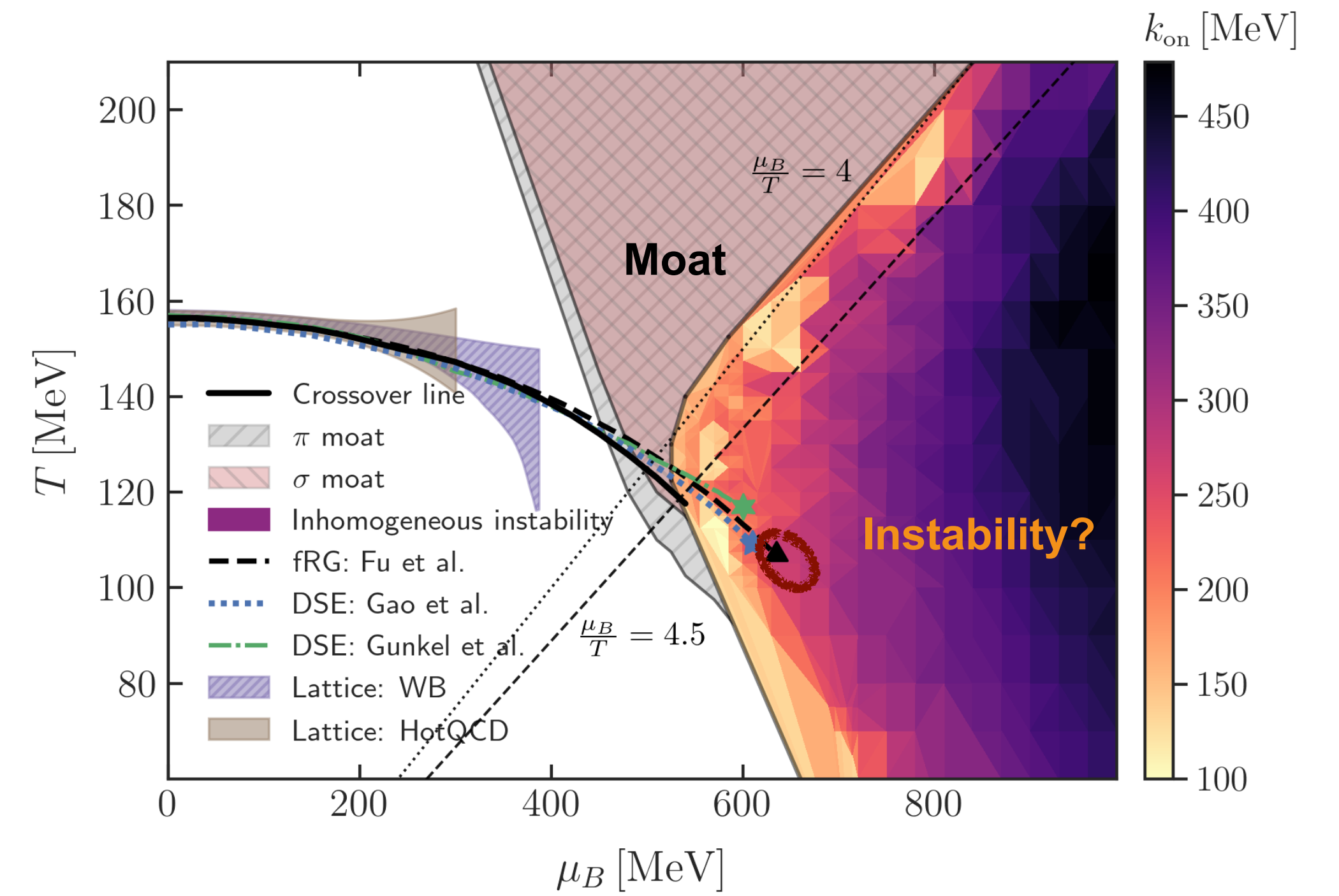
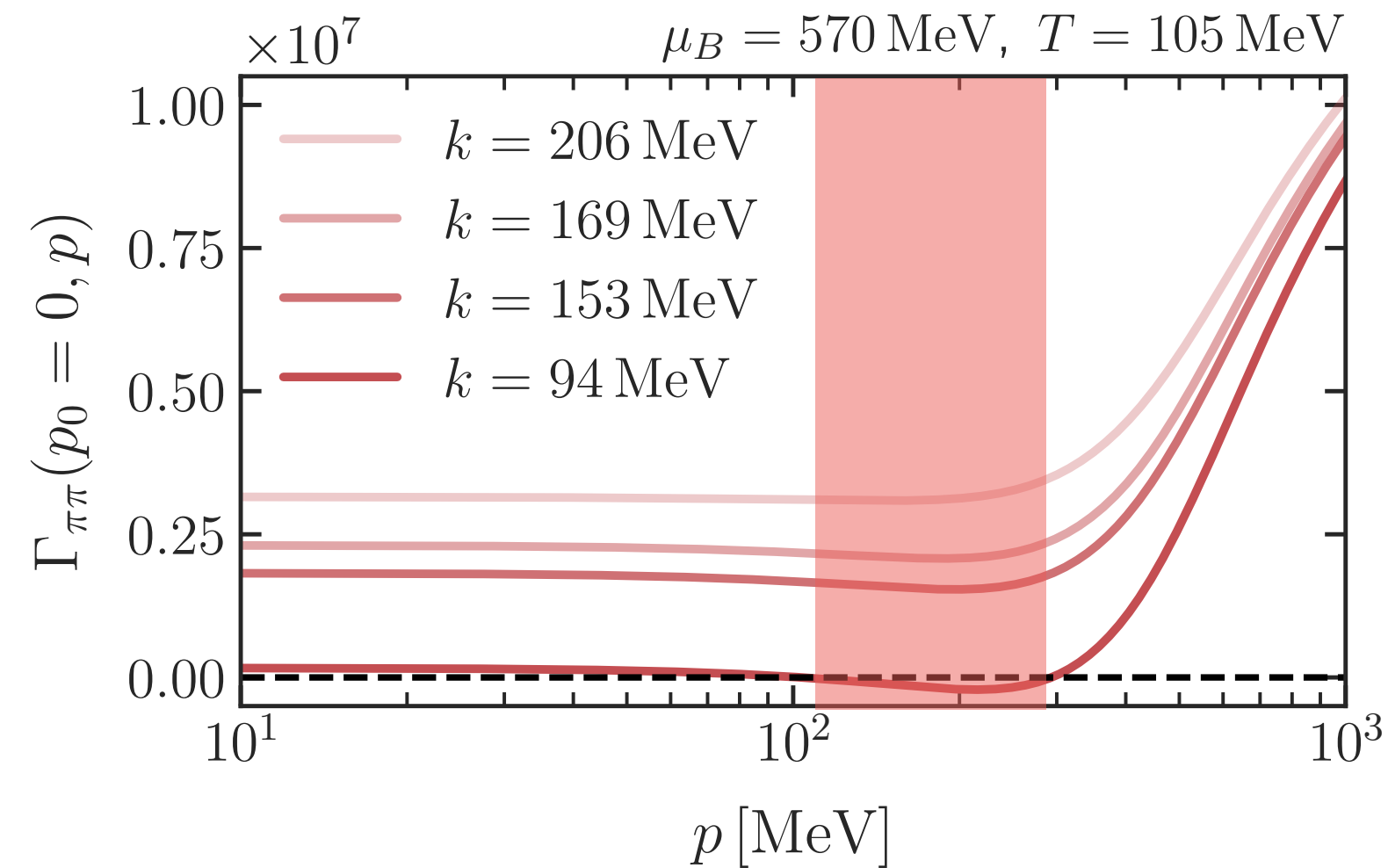


The QCD Moat reloaded

Moat



Instability



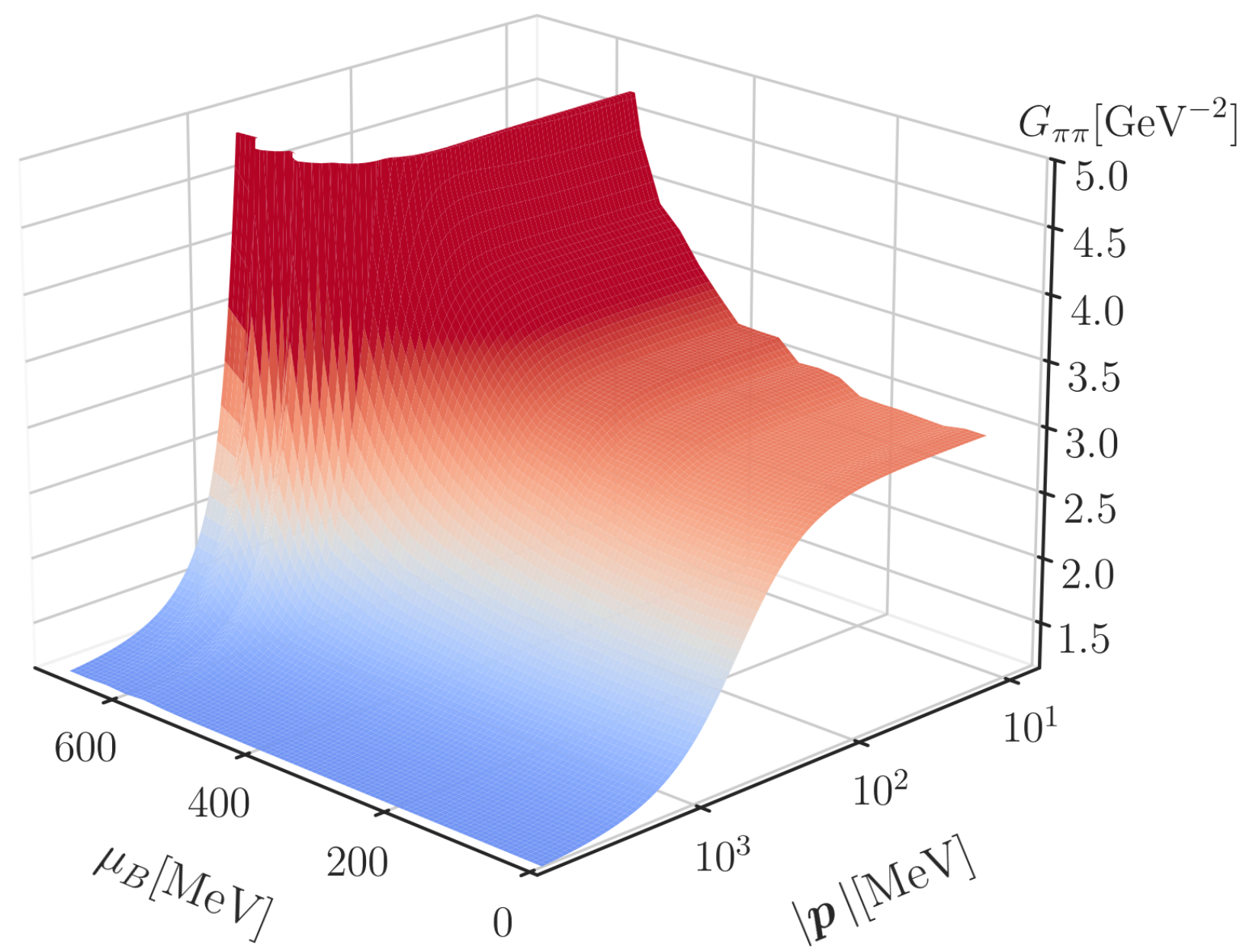
No full computation deep inside the instability regime

Estimated location of CEP

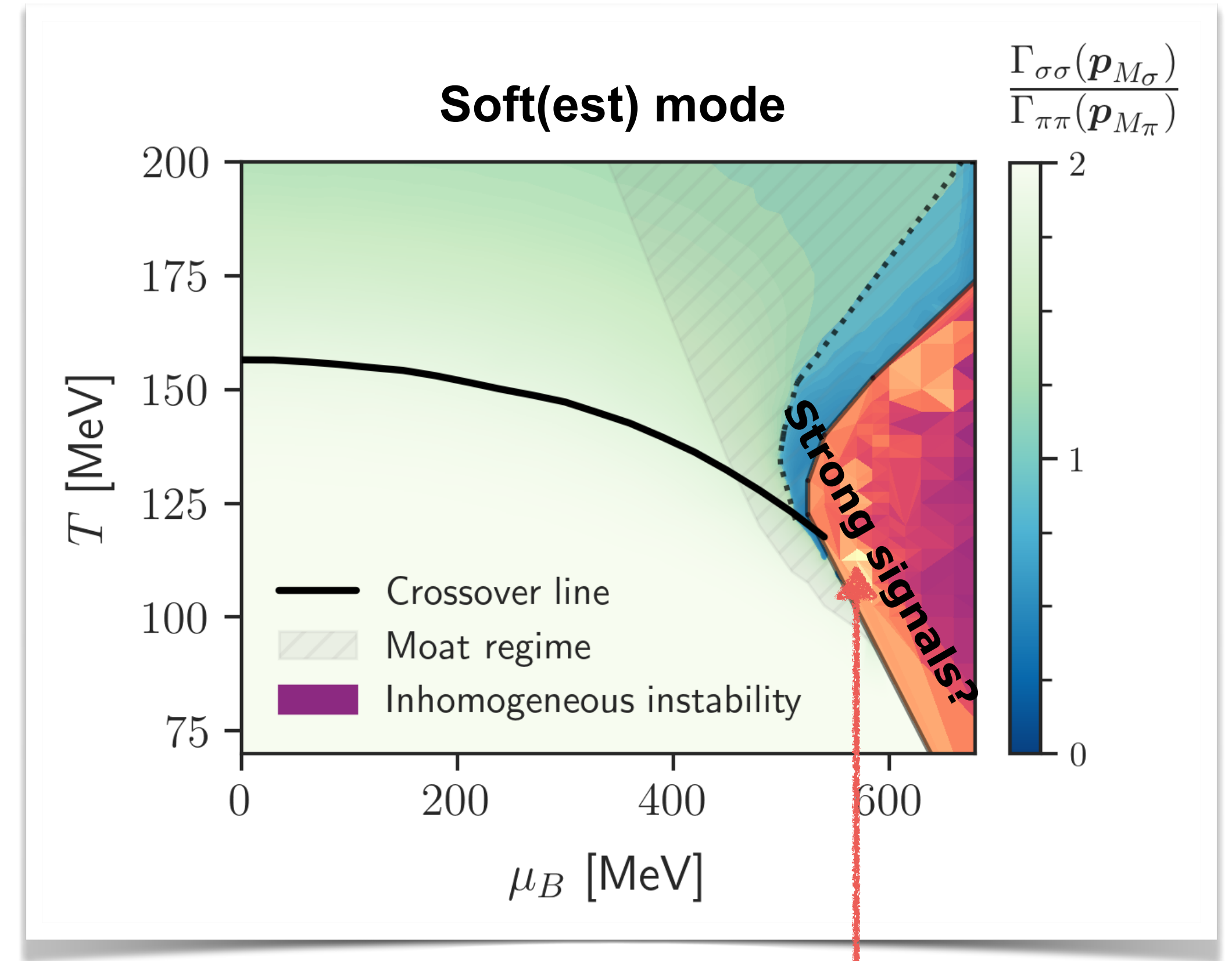
The QCD Moat reloaded

Soft mode

Pion propagator



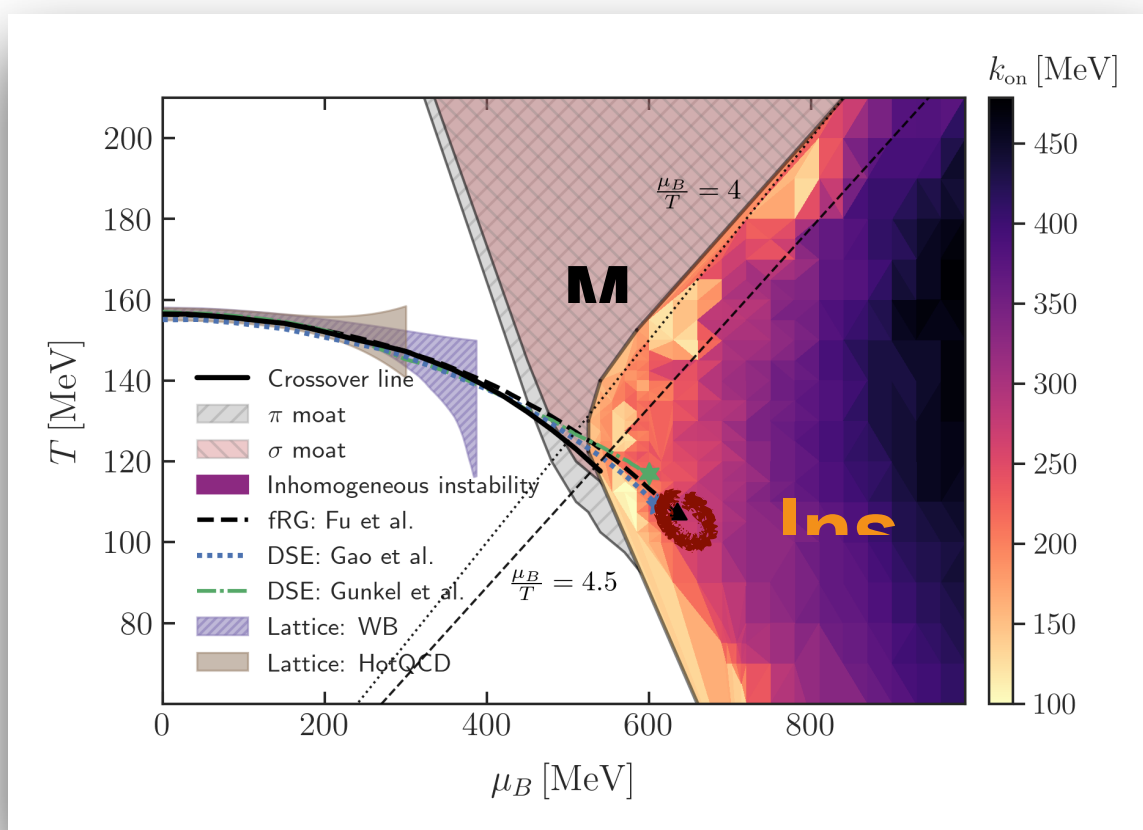
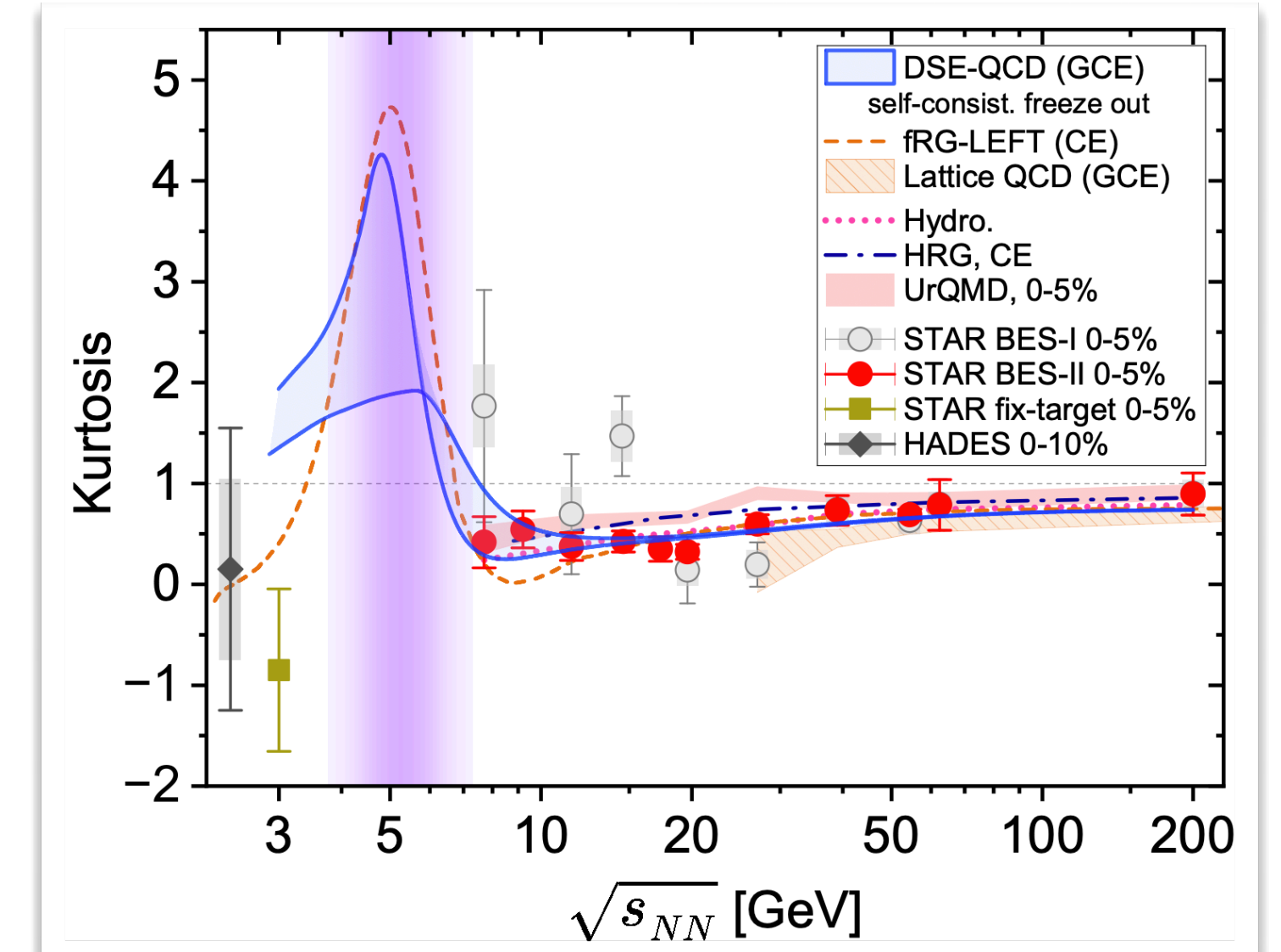
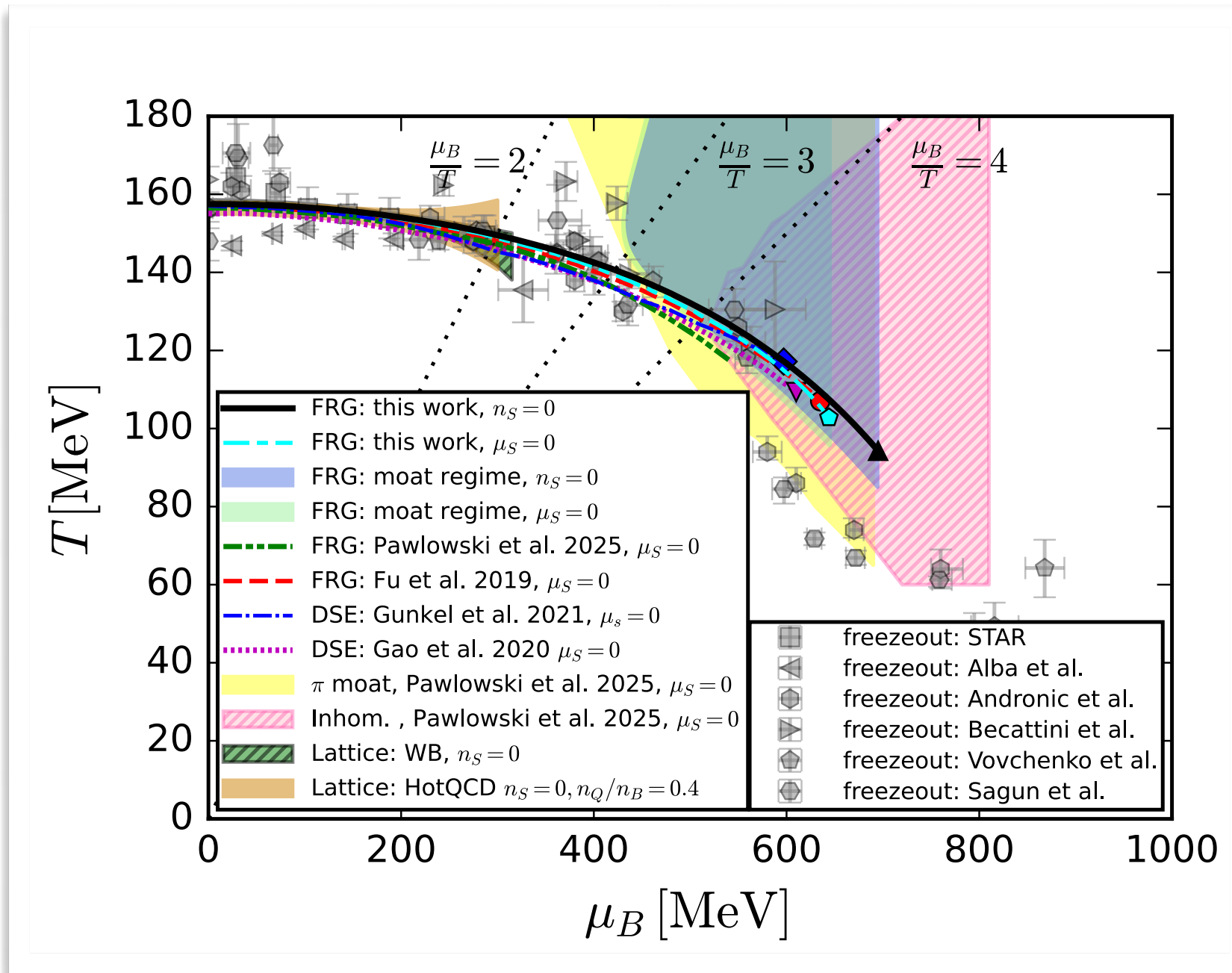
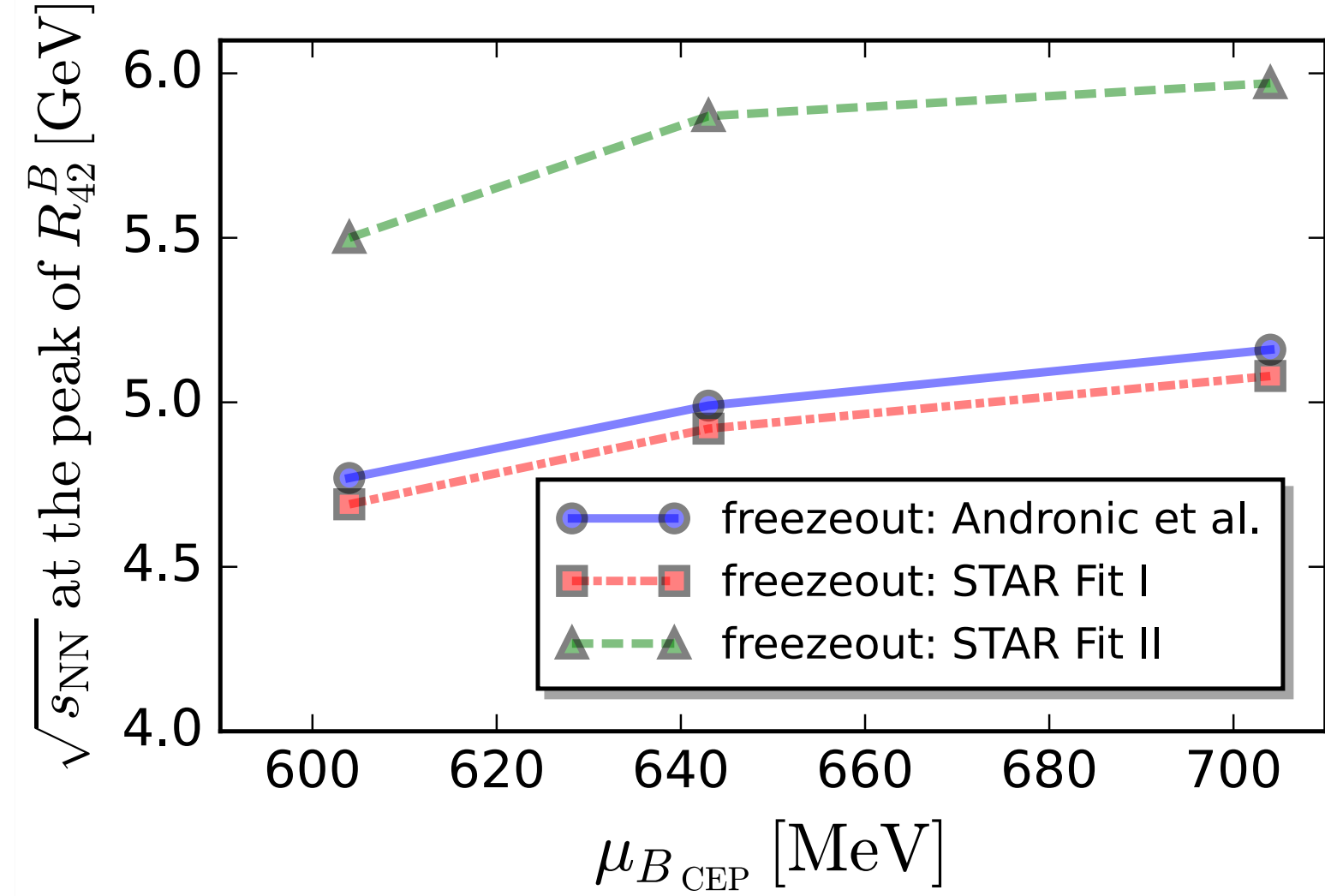
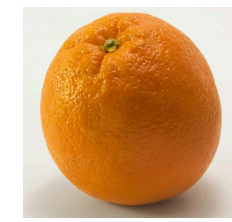
Soft(est) mode



$$k_{\text{on}} \lesssim 100 \text{ MeV}$$

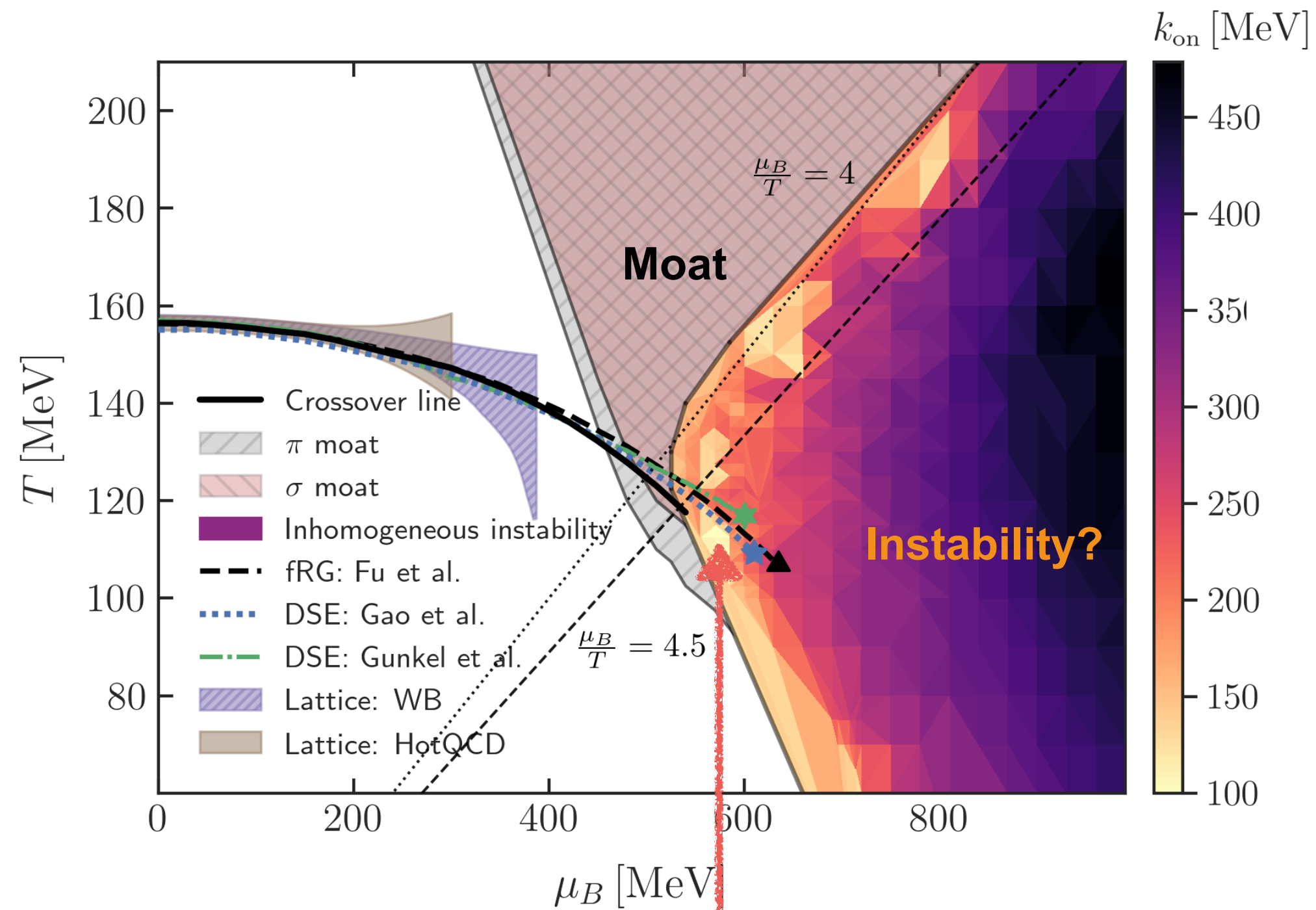


First functional shot on the experimental location of the peak



$$\sqrt{s_{\text{peak}}} \approx 5$$

Experimental signatures for the onset of new phases



The moat
&
the regime with new phases

are in the CBM regime
and
require high statistics

$$k_{\text{on}} \lesssim 100 \text{ MeV}$$

$$\sqrt{s_{\text{peak}}} \approx 5$$



!Go for it!

Summary

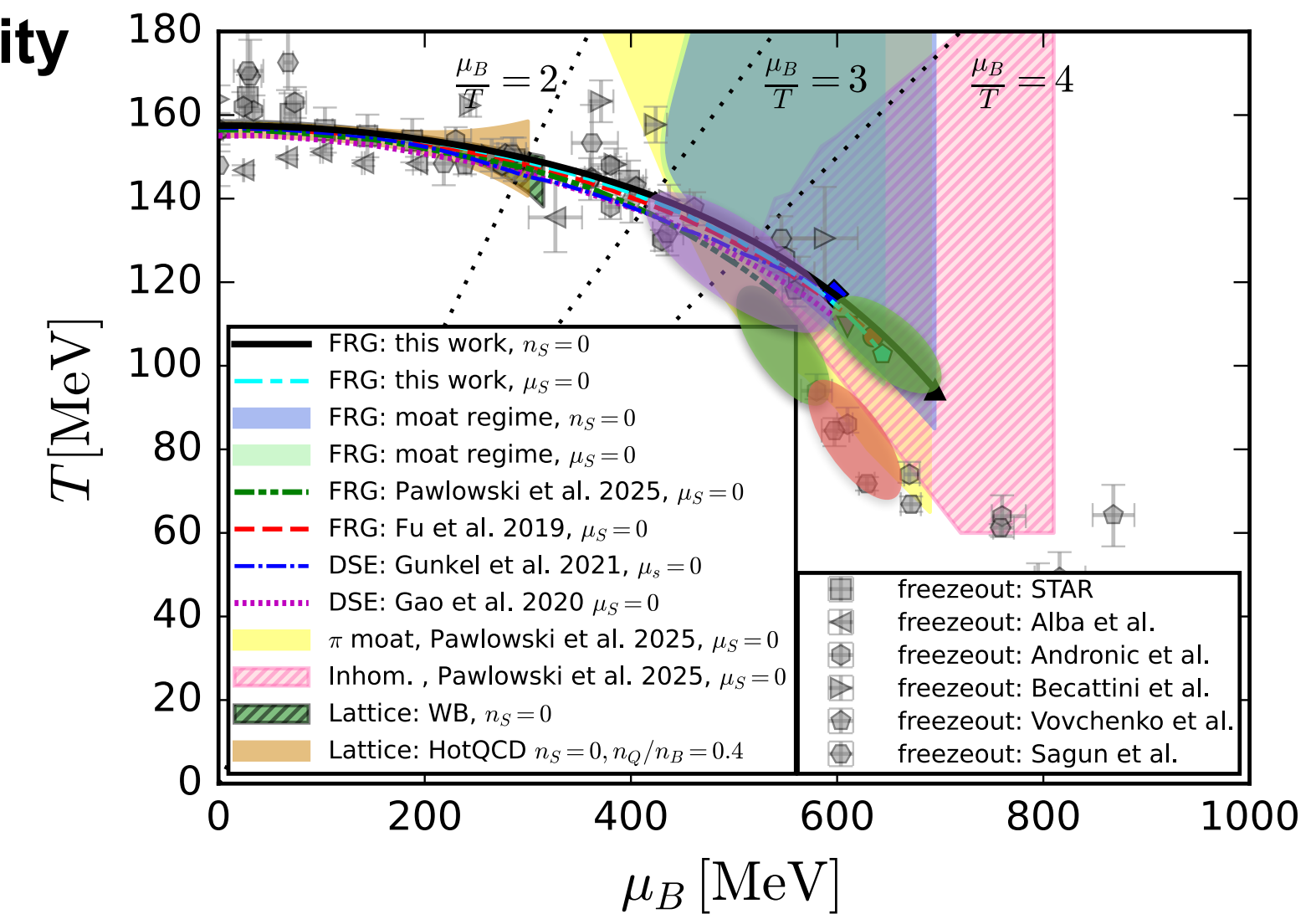
- Functional QCD provides direct 1st principle results for the phase structure at finite density

- Predictions: $\frac{\mu_B}{T} \lesssim 4.5$

- Estimates: $4.5 \lesssim \frac{\mu_B}{T} \lesssim 8$

- Soft modes are commonplace, critical regimes are small

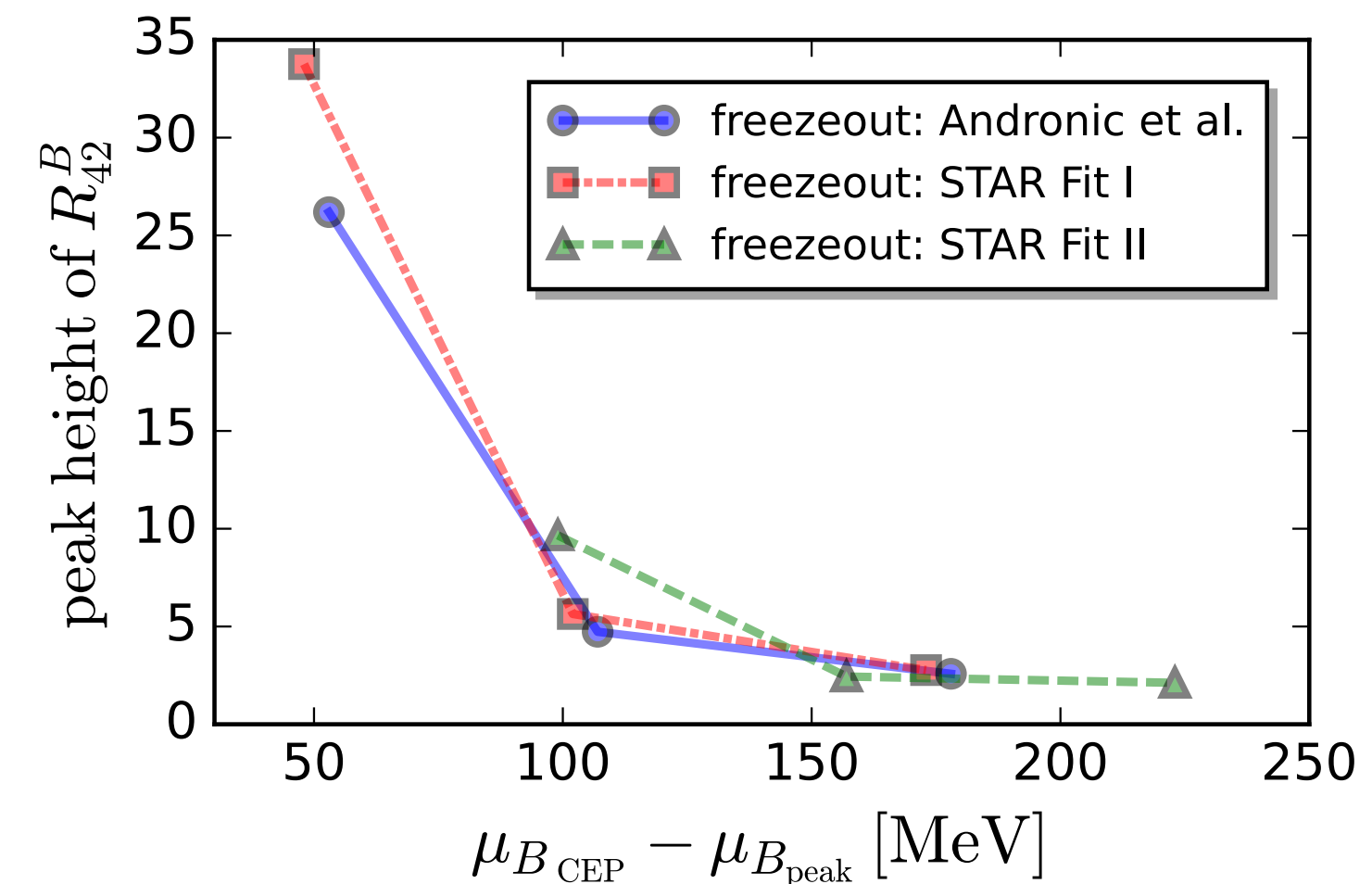
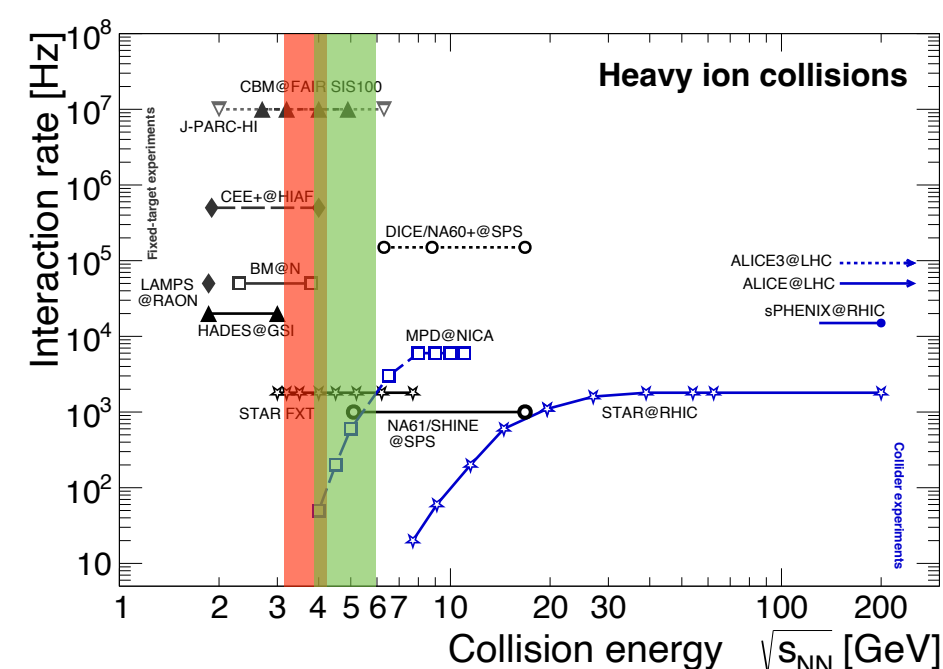
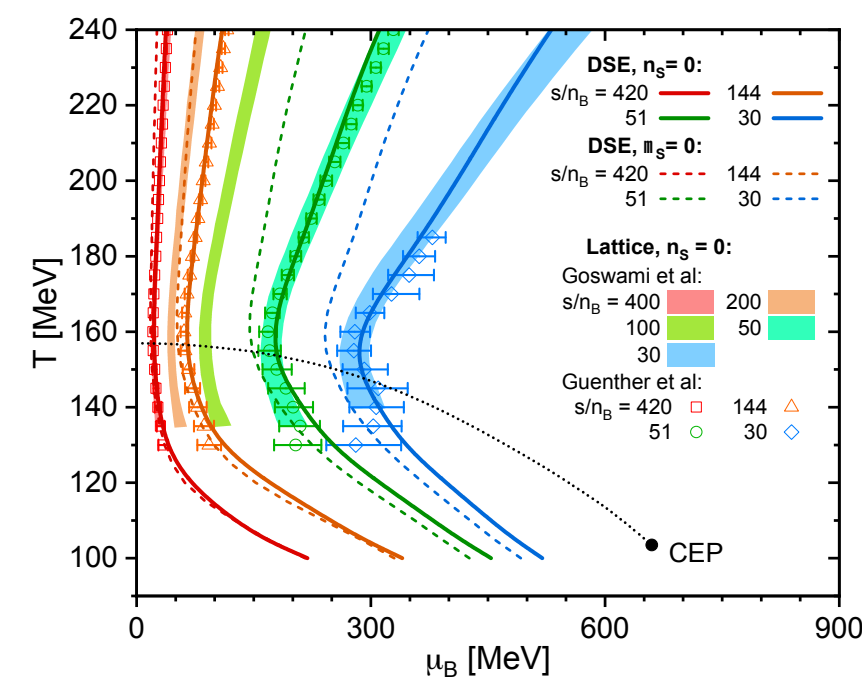
- Ripples of new phases aka of the critical end point



- Explanation for the convergence of CEP locations of extrapolation approaches

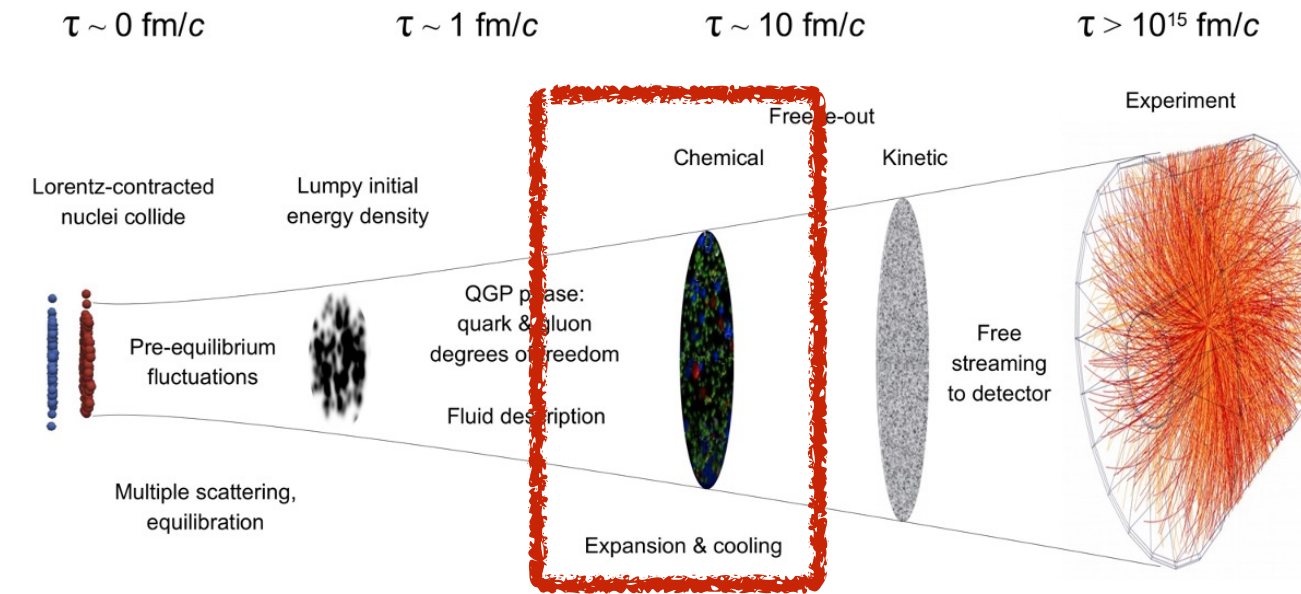
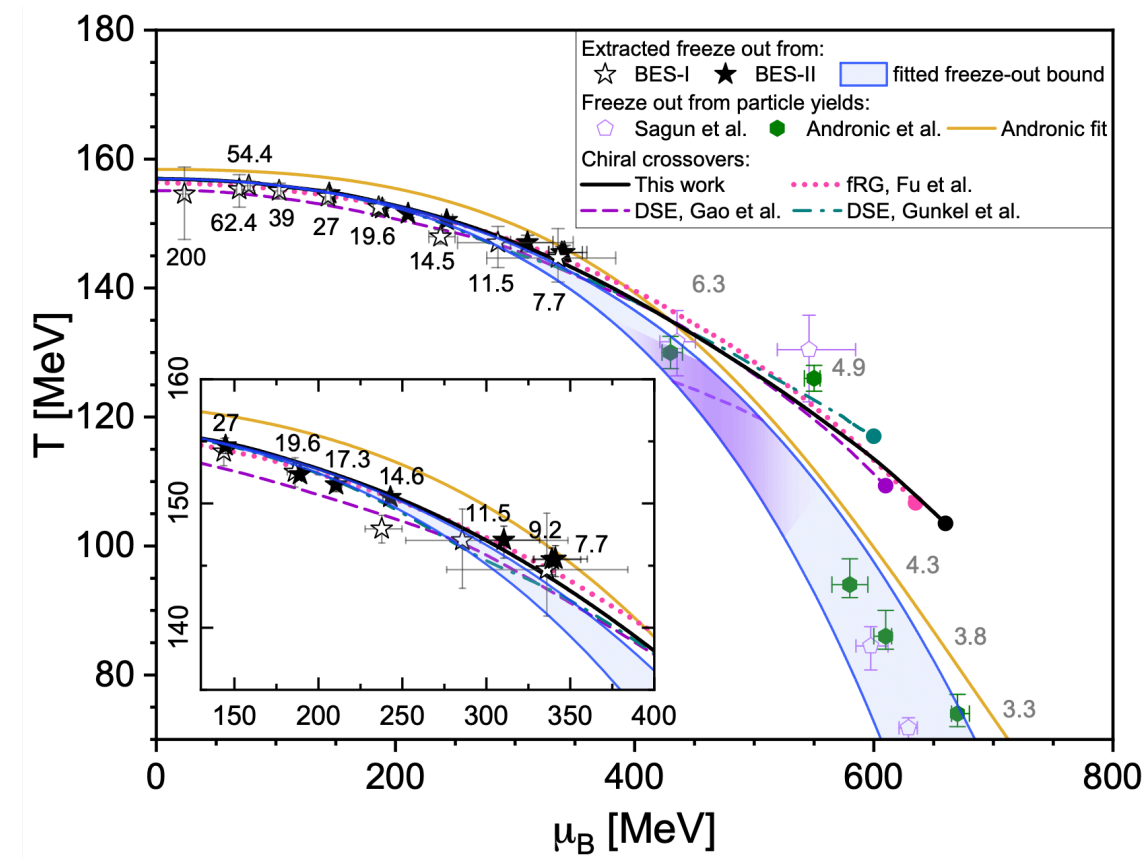
- Results & observables: EoS, fluctuations of conserved charges, tiny critical regime & onset of new phases; moat regime,

- Peak height of kurtosis carries the location of the CEP



Summary

Functional freeze out & towards real time dynamics



‘Combined unfolding’

$$\sqrt{s_{\text{peak}}} \approx 5$$

First steps in the QCD moat and inhomogeneous phases

